

# **Protein Folding by Robotics**

Motivation
 Motion Planning
 Protein Model
 Roadmaps
 Results
 Conclusion







# **Protein Folding by Robotics**

- Motivation
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Find good quality folding paths (into given native structure)
In structure prediction!

Predict formation orders (of secondary structure)









## Motion planning



February 21, 2006 Sebastian Will



#### Motion planning



Probabilistic roadmap planing





- Probabilistic roadmap planing
  - Sampling of configuration space Q





- Probabilistic roadmap planing
  - Sampling of configuration space Q
  - Connecting nearest configurations by a (simple) local planner





- Probabilistic roadmap planing
  - Sampling of configuration space Q
  - Connecting nearest configurations by a (simple) local planner
  - Apply graph algorithms to "roadmap": Find shortest path



# More on PRM for motion planning

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tree-like robots





tree-like robots (articulated robots)

Articulated Joint



tree-like robots (articulated robots)



tree-like robots (articulated robots)



confi guration = vector of angles

Confi guration space

 $Q = \{q \mid q \in S^n\}$ 

 $\mathbf{S}$  — set of angles

n — number of angles = degrees of freedom (dof)



Motivation
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 **3. Protein Model** 4. Roadmaps
 5. Results
 6. Conclusion

#### Obvious similarity





Motivation
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 Protein Model
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6. Conclusion

## Obvious similarity ;-)





Motivation
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#### Obvious similarity ;-)







Motivation
 Motion Planning
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 Roadmaps
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6. Conclusion

#### Obvious similarity ;-)



phi





psi



Motivation
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## Obvious similarity ;-)









Motivation
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#### no external obstacles, but

- self-avoidingness
- torsion angles

#### quality of paths

- Iow energy intermediate states
- kinetically prefered paths
- highly probable paths



method can use any potential



#### method can use any potential

## Our coarse potential

[Levitt. J.Mol.Biol., 1983.]

each sidechain by only one "atom" (zero dof)

 $U_{tot} =$ 



- method can use any potential
- Our coarse potential
  - [Levitt. J.Mol.Biol., 1983.]
  - each sidechain by only one "atom" (zero dof)

$$U_{tot} = \sum_{\text{restraints}} K_d \{ [(d_i - d_0)^2 + d_c^2]^{\frac{1}{2}} - d_c \}$$

first term favors known secondary structure through main chain hydrogen bonds and disulphide bonds



- method can use any potential
- Our coarse potential
  - [Levitt. J.Mol.Biol., 1983.]
  - each sidechain by only one "atom" (zero dof)

$$U_{tot} = \sum_{\text{restraints}} K_d \{ [(d_i - d_0)^2 + d_c^2]^{\frac{1}{2}} - d_c \} + E_{hp}$$

- first term favors known secondary structure through main chain hydrogen bonds and disulphide bonds
- second term hydrophobic effect



- method can use any potential
- Our coarse potential
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- Van der Waals interaction modeled by step function



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- first term favors known secondary structure through main chain hydrogen bonds and disulphide bonds
- second term hydrophobic effect
- Van der Waals interaction modeled by step function

## All-atom potential: EEF1

[Lazaridis, Karplus. Proteins, 1999.]



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Motivation
 Motion Planning
 **A Protein Model** Roadmaps
 Results
 Conclusion







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**TBI** Winterseminar 2006



Motivation
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Sampling

![](_page_30_Picture_7.jpeg)

Extracting

![](_page_31_Picture_0.jpeg)

# **Sampling — Node Generation**

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![](_page_31_Picture_4.jpeg)

![](_page_31_Picture_5.jpeg)

![](_page_31_Picture_6.jpeg)

Sampling 

![](_page_31_Picture_8.jpeg)

Extracting

![](_page_32_Picture_0.jpeg)

#### No uniform sampling

- configuration space too large
- $\mathbf{I} \Rightarrow$  need biased sampling strategy

![](_page_33_Picture_0.jpeg)

- No uniform sampling
  - configuration space too large
  - $\blacktriangleright$   $\Rightarrow$  need biased sampling strategy
- Gaussian sampling
  - centered around native conformation
  - Solution with different STDs  $5^{\circ}, 10^{\circ}, \dots, 160^{\circ}$
  - ensure representants for different numbers of native contacts

![](_page_34_Picture_0.jpeg)

- No uniform sampling
  - configuration space too large
  - $\Rightarrow$  need biased sampling strategy
- Gaussian sampling
  - centered around native conformation
  - Solution with different STDs  $5^{\circ}, 10^{\circ}, \dots, 160^{\circ}$
  - ensure representants for different numbers of native contacts

## Selection by energy

$$P(\text{accept } q) = \begin{cases} 1 & \text{if } E(q) < E_{\min} \\ \frac{E_{\max} - E(q)}{E_{\max} - E_{\min}} & \text{if } E_{\min} \leq E(q) \leq E_{\max} \\ 0 & \text{if } E(q) > E_{\max} \end{cases}$$

![](_page_35_Picture_0.jpeg)

## **More on Node Generation**

Motivation
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Visualization of Sampling Strategy

![](_page_35_Picture_4.jpeg)

![](_page_36_Picture_0.jpeg)

## **More on Node Generation**

1. Motivation Motivation
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## Visualization of Sampling Strategy

![](_page_36_Picture_4.jpeg)

#### Distribution

![](_page_36_Figure_6.jpeg)

RMSD vs. Energy

![](_page_37_Picture_0.jpeg)

## **Node Connection**

Motivation
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![](_page_37_Picture_3.jpeg)

![](_page_37_Picture_4.jpeg)

![](_page_37_Picture_5.jpeg)

![](_page_37_Picture_6.jpeg)

![](_page_37_Picture_7.jpeg)

Extracting

![](_page_38_Picture_0.jpeg)

- connect confi gurations in close distance
- generate N intermediary nodes by local planner

![](_page_39_Picture_0.jpeg)

- connect confi gurations in close distance
- generate N intermediary nodes by local planner

![](_page_40_Picture_0.jpeg)

![](_page_40_Picture_3.jpeg)

generate N intermediary nodes by local planner

![](_page_41_Picture_0.jpeg)

![](_page_41_Picture_3.jpeg)

generate N intermediary nodes by local planner

![](_page_42_Picture_0.jpeg)

![](_page_42_Picture_3.jpeg)

generate N intermediary nodes by local planner

![](_page_43_Picture_0.jpeg)

![](_page_43_Picture_3.jpeg)

generate N intermediary nodes by local planner

![](_page_43_Picture_5.jpeg)

![](_page_44_Picture_0.jpeg)

![](_page_44_Figure_3.jpeg)

$$\left( 1 \quad \text{if } \Delta E \leq 0 \right)$$

![](_page_45_Picture_0.jpeg)

![](_page_45_Figure_3.jpeg)

![](_page_46_Picture_0.jpeg)

- connect confi gurations in close distance
- generate N intermediary nodes by local planner

![](_page_46_Figure_5.jpeg)

#### assign weights to edges

$$P_i = \begin{cases} e^{-\frac{\Delta E}{kT}} & \text{if } \Delta E > 0\\ 1 & \text{if } \Delta E \le 0 \end{cases}$$

Weight = 
$$\sum_{i=0}^{N} -log(P_i)$$

![](_page_47_Picture_0.jpeg)

## **Extracting Paths**

Motivation
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![](_page_47_Picture_3.jpeg)

![](_page_47_Picture_4.jpeg)

![](_page_47_Picture_5.jpeg)

Sampling

![](_page_47_Picture_7.jpeg)

Extracting

![](_page_48_Picture_0.jpeg)

#### Shortest Path

- extract one shortest path
- from some starting conformation, one path at a time

![](_page_49_Picture_0.jpeg)

#### Shortest Path

- extract one shortest path
- from some starting conformation, one path at a time
- Single Source Shortest Paths (SSSP)
  - extract shortest paths from all starting conformation
  - compute paths simultaneously
  - generate tree of shortest paths (SSSP tree)

![](_page_50_Picture_0.jpeg)

## **Big Picture**

Motivation
 Motion Planning
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![](_page_50_Picture_3.jpeg)

![](_page_50_Picture_4.jpeg)

![](_page_50_Picture_5.jpeg)

Sampling

![](_page_50_Picture_7.jpeg)

![](_page_50_Picture_8.jpeg)

![](_page_51_Picture_0.jpeg)

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#### Overview of studied proteins, roadmap size, and construction times

pdb	Description	Length	SS	# Nodes	Time (h)
1gb1	Protein G domain B1	56	$1\alpha + 4\beta$	8 000	6.400
2crt	Cardiotoxin III	60	5β	8 000	6.430
1bdd	Staphylococcus protein A	60	3α	10 000	10.400
1shg	SH3 domain $\alpha$ -spectrin	62	5β	10 000	8.344
2ptl	Protein L, B1 domain	62	$1\alpha + 4\beta$	4 000	3.104
1coa	CI2	64	$1\alpha + 4\beta$	10 000	9.984
1srl	SH3 domain src	64	5β	8 000	5.990
1nyf	SH3 domain fyn	67	5β	10 000	8.418
2ait	Tendamistat	74	$7\beta$	10 000	13.327
1ubq	Ubiquitin	76	$1\alpha + 5\beta$	8 000	10.381
1pks	SH3 domain PI3 kinase	79	$1\alpha + 5\beta$	10 000	14.446
1pba	Procarboxypeptidase A2	81	$3\alpha + 3\beta$	8 000	10.845

![](_page_52_Picture_0.jpeg)

## formation order of secondary structure for verifying method

# formation orders can be determined experimentally

Li, Woodward. Protein Science, 1999.

Pulse labeling

Out-exchange

- prediction of formation orders
  - single paths
  - averaging over multiple paths (SSSP-tree)

![](_page_53_Picture_0.jpeg)

# **Timed Contact Maps**

![](_page_53_Figure_2.jpeg)

![](_page_53_Figure_3.jpeg)

![](_page_54_Picture_0.jpeg)

pdb	Out exchange	Pulse labeling	Our SS formation order	Comp.
1gb1	$[\alpha, \beta 1, \beta 3, \beta 4], \beta 2$	$[\alpha, \beta 4], [\beta 1, \beta 2, \beta 3]$	$\alpha, \beta 3 - \beta 4, \beta 1 - \beta 2, \beta 1 - \beta 4$	Agreed
2crt	$[\beta 3, \beta 4, \beta 5], [\beta 1, \beta 2]$	$\beta 5, \beta 3, \beta 4, [\beta 1, \beta 2]$	$\beta 1-\beta 2, \beta 3-\beta 4, \beta 3-\beta 5$	Not sure
1bdd	$[\alpha 2, \alpha 3], \alpha 1$	$[\alpha 1, \alpha 2, \alpha 3]$	$[\alpha 2, \alpha 3], \alpha 1, \alpha 2 - \alpha 3, \alpha 1 - \alpha 3$	Agreed
1shg	N/A	N/A	$\beta$ 3- $\beta$ 4, $\beta$ 2- $\beta$ 3, $\beta$ 1- $\beta$ 5, $\beta$ 1- $\beta$ 2	N/A
2ptl	$[\alpha, \beta 1, \beta 2, \beta 4], \beta 3$	$[\alpha, \beta 1], [\beta 2, \beta 3, \beta 4]$	$\alpha$ , $\beta 1$ – $\beta 2$ , $\beta 3$ – $\beta 4$ , $\beta 1$ – $\beta 4$	Agreed
1coa	$[\alpha, \beta 2, \beta 3], [\beta 1, \beta 4]$	N/A	$\alpha, \beta 3-\beta 4, \beta 2-\beta 3, \beta 1-\beta 4$	Agreed
1srl	N/A	N/A	$\beta$ 3- $\beta$ 4, $\beta$ 2- $\beta$ 3, $\beta$ 1- $\beta$ 5, $\beta$ 1- $\beta$ 2	N/A
1nyf	N/A	N/A	$\beta$ 3- $\beta$ 4, $\beta$ 2- $\beta$ 3, $\beta$ 1- $\beta$ 2, $\beta$ 1- $\beta$ 5	N/A
2ait	$[\beta 1, \beta 2], [\beta 3, \beta 4, \beta 5, \beta 6, \beta 7]$	N/A	$\beta 1-\beta 2, \beta 3-\beta 4, [\beta 2-\beta 5, \beta 3-\beta 6], \beta 3-\beta 5$	Agreed
1ubq	$[\alpha, \beta 1, \beta 2], [\beta 3, \beta 5], \beta 4$	N/A	$\alpha, \beta 3-\beta 4, \beta 1-\beta 2, \beta 3-\beta 5, \beta 1-\beta 5$	Agreed
1pks	N/A	N/A	$\beta 3-\beta 4, \beta 1-\beta 5, [\beta 1-\beta 2, \beta 2-\beta 3]$	N/A
1pba	N/A	N/A	$[\alpha 1, \alpha 3], [\beta 1 - \beta 2, \beta 1 - \beta 3]$	N/A

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![](_page_55_Picture_0.jpeg)

pdb	Out exchange	Pulse labeling	Our SS formation order	Comp.
1gb1	$[\alpha, \beta 1, \beta 3, \beta 4], \beta 2$	$[\alpha, \beta 4], [\beta 1, \beta 2, \beta 3]$	$\alpha, \beta 3 - \beta 4, \beta 1 - \beta 2, \beta 1 - \beta 4$	Agreed
2crt	$[\beta 3, \beta 4, \beta 5], [\beta 1, \beta 2]$	$\beta 5, \beta 3, \beta 4, [\beta 1, \beta 2]$	$\beta 1-\beta 2, \beta 3-\beta 4, \beta 3-\beta 5$	Not sure
1bdd	$[\alpha 2, \alpha 3], \alpha 1$	$[\alpha 1, \alpha 2, \alpha 3]$	$[\alpha 2, \alpha 3], \alpha 1, \alpha 2 - \alpha 3, \alpha 1 - \alpha 3$	Agreed
1shg	N/A	N/A	$\beta$ 3- $\beta$ 4, $\beta$ 2- $\beta$ 3, $\beta$ 1- $\beta$ 5, $\beta$ 1- $\beta$ 2	N/A
2ptl	$[\alpha, \beta 1, \beta 2, \beta 4], \beta 3$	$[\alpha, \beta 1], [\beta 2, \beta 3, \beta 4]$	$\alpha, \beta 1 - \beta 2, \beta 3 - \beta 4, \beta 1 - \beta 4$	Agreed
1coa	$[\alpha, \beta 2, \beta 3], [\beta 1, \beta 4]$	N/A	$\alpha, \beta 3 - \beta 4, \beta 2 - \beta 3, \beta 1 - \beta 4$	Agreed
1srl	N/A	N/A	$\beta$ 3- $\beta$ 4, $\beta$ 2- $\beta$ 3, $\beta$ 1- $\beta$ 5, $\beta$ 1- $\beta$ 2	N/A
1nyf	N/A	N/A	$\beta$ 3- $\beta$ 4, $\beta$ 2- $\beta$ 3, $\beta$ 1- $\beta$ 2, $\beta$ 1- $\beta$ 5	N/A
2ait	$[\beta 1, \beta 2], [\beta 3, \beta 4, \beta 5, \beta 6, \beta 7]$	N/A	$\beta 1-\beta 2, \beta 3-\beta 4, [\beta 2-\beta 5, \beta 3-\beta 6], \beta 3-\beta 5$	Agreed
1ubq	$[\alpha, \beta 1, \beta 2], [\beta 3, \beta 5], \beta 4$	N/A	$\alpha, \beta 3 - \beta 4, \beta 1 - \beta 2, \beta 3 - \beta 5, \beta 1 - \beta 5$	Agreed
1pks	N/A	N/A	$\beta 3-\beta 4, \beta 1-\beta 5, [\beta 1-\beta 2, \beta 2-\beta 3]$	N/A
1pba	N/A	N/A	$[\alpha 1, \alpha 3], [\beta 1 - \beta 2, \beta 1 - \beta 3]$	N/A

no (reported) contradictions between prediction and validation

different kind of information from experiment and prediction

![](_page_56_Picture_0.jpeg)

# The Proteins G and L

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- Studied in more detail
- good test case
- Structurally similar:  $1\alpha + 4\beta$

![](_page_56_Picture_6.jpeg)

- fold differently
  - **Protein G:**  $\beta$ -turn 2 forms first
  - Solution Protein L:  $\beta$ -turn 1 forms first

![](_page_57_Picture_0.jpeg)

## Comparison of Analysis Techniques β-Turn Formation

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3	Contacts	Fnerov	Secondary structure	Ana	lyze f	irst x%	% cont	acts
Name	considered	function	formation order	20	40	60	80	100
Protein G	All	Our	$\alpha$ , turn 2, turn 1	53	52	52	50	50
			turn 2, $\alpha$ , turn 1	15	9	17	22	22
			$\alpha$ , turn 1, turn 2	25	33	26	23	24
		All-atom	$\alpha$ , turn 2, turn 1	36	37	55	55	57
			turn 2, $\alpha$ , turn 1	3	0	0	0	0
			$\alpha$ , turn 1, turn 2	50	63	45	45	43
			turn 1, $\alpha$ , turn 2	12	0	0	0	0
	Hydrophobic	Our	$\alpha$ , turn 2, turn 1	96	96	85	96	87
			$\alpha$ , turn 1, turn 2	4	4	12	2	11
		All-atom	$\alpha$ , turn 2, turn 1	76	78	78	92	69
			$\alpha$ , turn 1, turn 2	24	22	22	8	31
Protein L	All	Our	$\alpha$ , turn 1, turn 2	24	30	37	38	41
			turn 1, $\alpha$ , turn 2	3	4	4	4	6
			$\alpha$ , turn 2, turn 1	73	63	60	48	39
		All-atom	$\alpha$ , turn 1, turn 2	25	25	48	43	41
			$\alpha$ , turn 2, turn 1	75	75	52	57	59
	Hydrophobic	Our	$\alpha$ , turn 1, turn 2	72	68	72	70	69
			turn 1, $\alpha$ , turn 2	5	9	5	7	15
			$\alpha$ , turn 2, turn 1	23	22	22	23	15
		All-atom	$\alpha$ , turn 1, turn 2	66	76	78	95	97
			turn 1, $\alpha$ , turn 2	3	0	0	0	0
			$\alpha$ , turn 2, turn 1	31	24	22	5	3

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![](_page_58_Picture_0.jpeg)

## Conclusion

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![](_page_59_Picture_0.jpeg)

![](_page_59_Picture_1.jpeg)

![](_page_59_Picture_3.jpeg)

## PRM can be applied to "realistic" protein models

![](_page_60_Picture_0.jpeg)

![](_page_60_Picture_3.jpeg)

Introduced method makes verifiable prediction

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![](_page_61_Picture_0.jpeg)

- PRM can be applied to "realistic" protein models
- Introduced method makes verifiable prediction
- Coarse potential is suffi cient

![](_page_62_Picture_0.jpeg)

- PRM can be applied to "realistic" protein models
- Introduced method makes verifiable prediction
- Coarse potential is suffi cient
- Predictions are in good accordance to experimental data

![](_page_63_Picture_0.jpeg)

- PRM can be applied to "realistic" protein models
- Introduced method makes verifiable prediction
- Coarse potential is suffi cient
- Predictions are in good accordance to experimental data
- Interesting relations to e.g. computation of barrier trees