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# RNA design | objectives, solution landscapes and optimization methods

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# Design objectives for novel ncRNAs

- Combine functional components
- Gain novel functionality
- Respect biological target system

# Design methods

- Experimental selection/screening:
  - Desired functionality (experimental assay)
  - Selection/screening method
  - Candidate characterization
- Computational *de novo* design:
  - Desired functionality (*in silico* model)
  - Sampling/optimization method
  - Functional testing and characterization

# Rational *de novo* design

## 1) Design objective:

- Functionality of components (aptamer, terminator,...)
- Novel overall functionality
- Respect the biological target system

## 2) Sequence generation:

- Constraint sampling
- Weighted sampling

## 3) Optimization method

## 4) *In silico* filtering and characterization

# Single-state RNA devices

- Design objectives purely based on structure
- Positive design
  - Target structure must be thermodynamically stable
- Negative design
  - Contrary structures must be less stable and thus less

# Single-state objectives

- MFE defect
- Probability defect
- Element probability defect
- Enforced element probability defect
- Ensemble defect

# MFE defect

$$\cdot(((\dots)))\dots f(x) = 0$$

$$(((\dots)))\dots f(x) = 1$$

$$\cdot((\dots))\dots f(x) = 1$$

$$\cdot(((\dots)))(\dots) f(x) = 1$$

$$\cdot(((\dots))\cdot)\dots f(x) = 2$$

$$\dots(((\dots))) f(x) = 7$$

$$\dots\dots\dots f(x) = 3$$

$$f(x) \in [0, \infty)$$

$$f(x) = D(\phi_{\text{target}}, \phi_{\text{MFE}})$$

# Probability defect

- .(((.....)))..... 0.6
- ((((.....))))..... 0.1
- ..(((.....)))..... 0.1
- .((((.....)))(.....) 0.05
- .(((.....)).)..... 0.05
- .....((((.....)))) 0.05
- ..... 0.05

$$f(x) = 0.60 \in [0, 1]$$

$$f(x) = P(x|\phi_{\text{target}}) \propto G(x|\phi) - G(x|\Phi)$$

$$B(x|\phi) = \exp\left(-\frac{G(x|\phi)}{RT}\right)$$

$$Z(x) = \sum_{\phi \in \Phi} B(x|\phi)$$

$$P(x|\phi) = \frac{B(x|\phi)}{Z} = \exp\left(-\frac{G(x|\phi) - G(x|\Phi)}{RT}\right)$$

- $x$ ... Sequence
- $\phi$ ... Structure
- $\Phi$ ... Ensemble of structures
- $G$ ... Gibbs free energy
- $Z$ ... Partition function
- $B$ ... Boltzmann weight
- $R$ ... Gas constant
- $T$ ... Temperature



# Element probability defect

.(((.....)))..... 0.6

(((((.....))))..... 0.1

..(((.....))..... 0.1

.(((.....)))(.....) 0.05

.(((.....)).)..... 0.05

.....(((.....))) 0.05

..... 0.05

$f(x) = 0.90 \in [0, 1]$

$$f(x) = P(x|\Phi_{\text{target}}) \propto G(x|\Phi_{\text{target}}) - G(x|\Phi)$$

$$P(x|\Phi_{\text{target}}) = \exp\left(-\frac{G(x|\Phi_{\text{target}}) - G(x|\Phi)}{RT}\right)$$

# Enforced element probability defect

.(((.....)))..... 0.6

(((((.....))))..... 0.1

..(((.....))..... 0.1

.(((.....)))(.....) 0.05

.(((.....)).)..... 0.05

.....(((.....))) 0.05

..... 0.05

$f(x) = 0.75 \in [0, 1]$

$$f(x) = P(x|\Phi_{\text{target}}) \propto G(x|\Phi_{\text{target}}) - G(x|\Phi)$$

$$P(x|\Phi_{\text{target}}) = \exp\left(-\frac{G(x|\Phi_{\text{target}}) - G(x|\Phi)}{RT}\right)$$

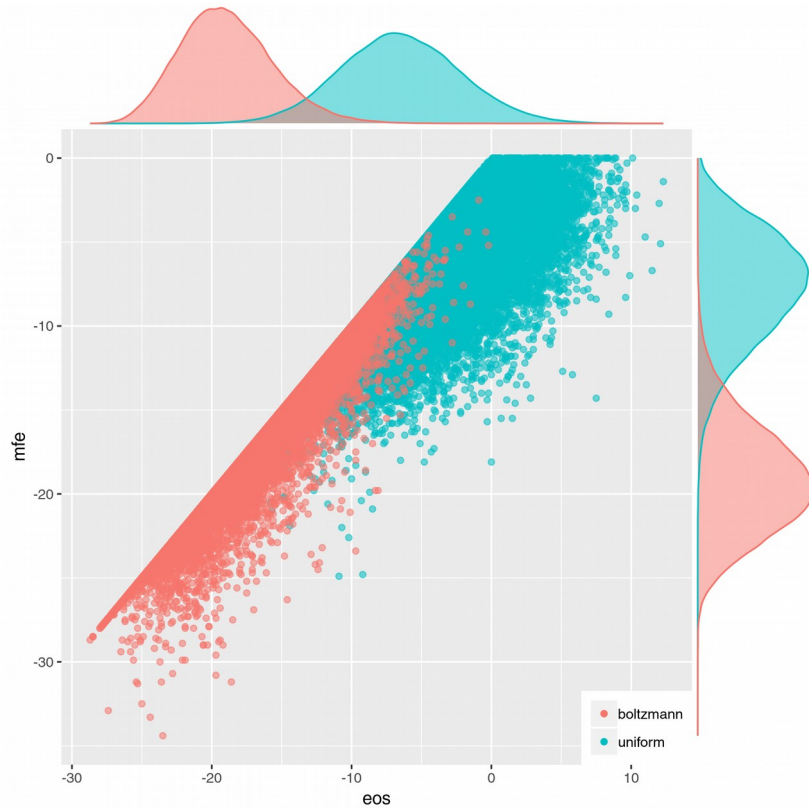
# Ensemble defect

.(((.....)))..... 0.6·0  
 ((((((.....))))))..... 0.1·1  
 ..(((.....))..... 0.1·1  
 .(((.....)))(.....) 0.05·1  
 .(((.....)).)..... 0.05·2  
 .....(((.....))) 0.05·7  
 ..... 0.05·3  
**f(x) = 0.85 ∈ [0, ∞)**

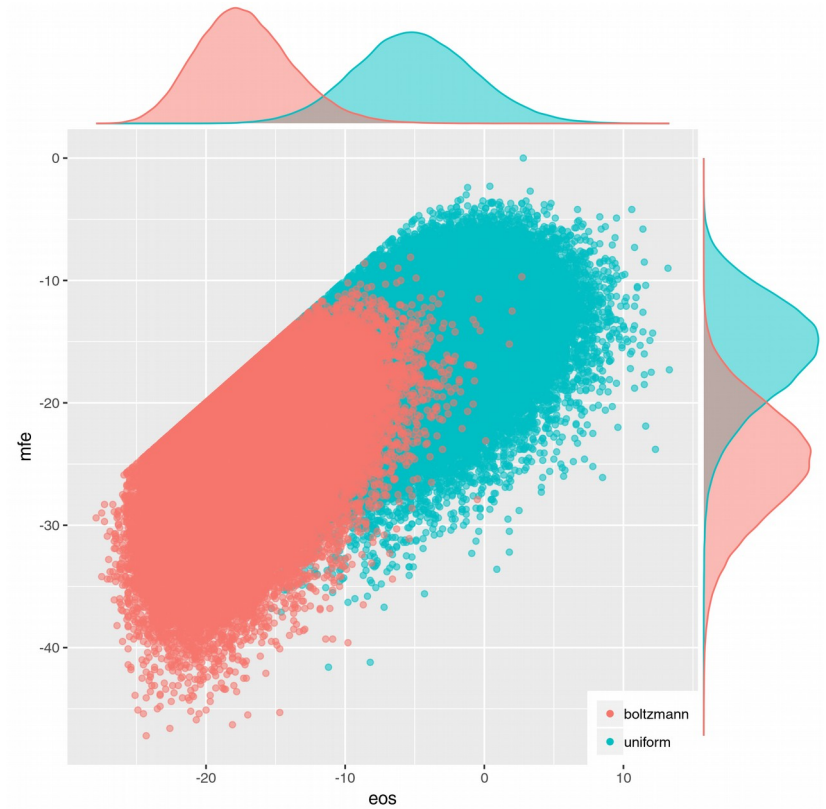
$$f(x) = \sum_{\phi \in \Phi} P(x|\phi_{\text{target}}) \times D(\phi, \phi_{\text{target}})$$

# Example solution Landscapes

(((((((.....)))))))((((((((.....))))))  
1e+4 from 1.42658e+14 sequences



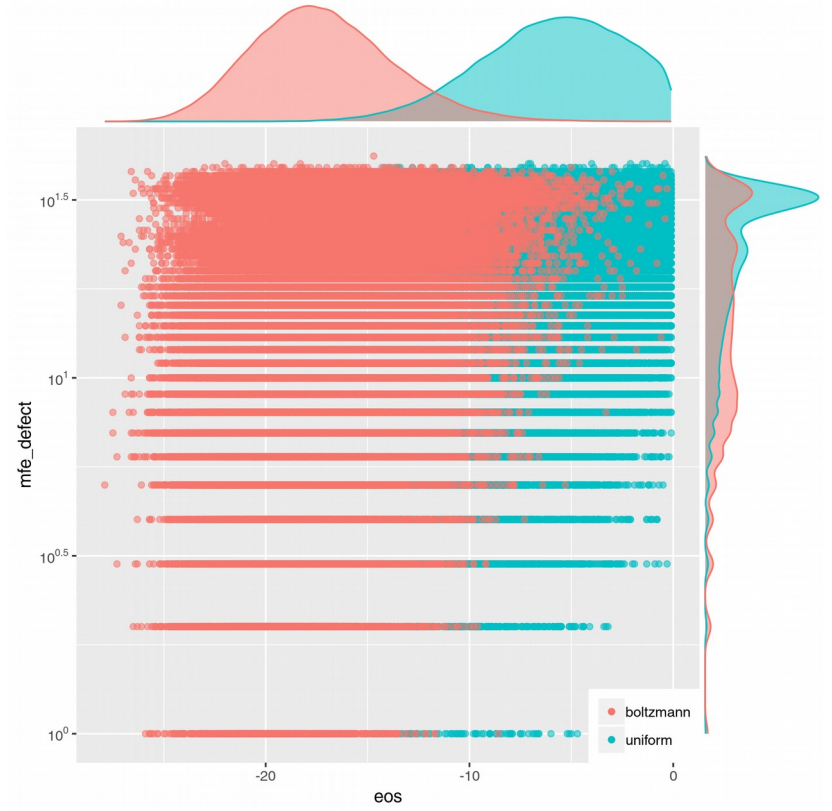
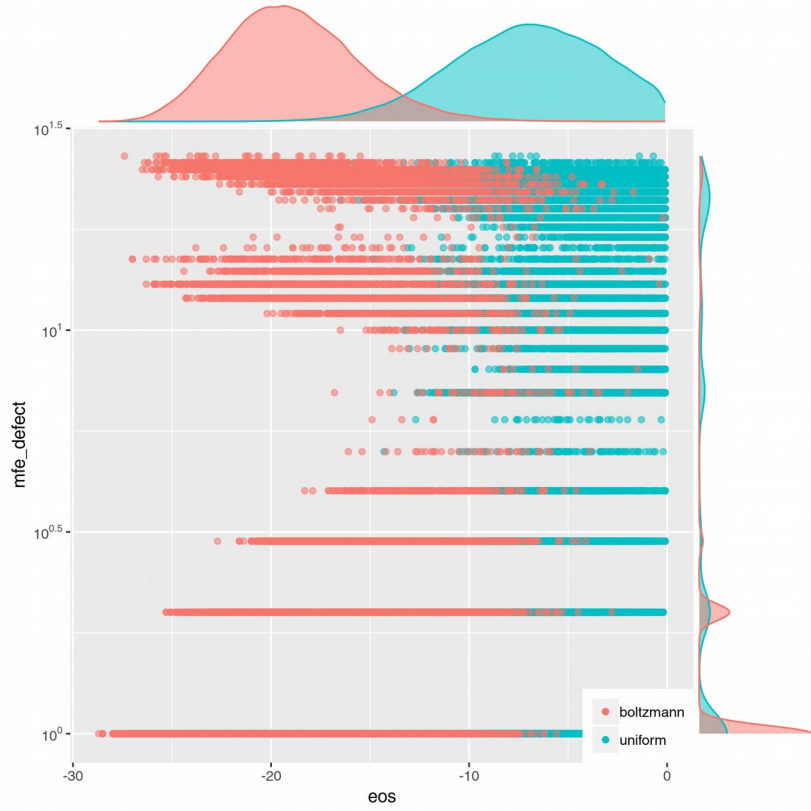
(((((((.....)))))))((((((((.....)))))).....  
1e+4 from 9.86838e+32 sequences



# MFE defect

(((((.....))))))(((.....))))))

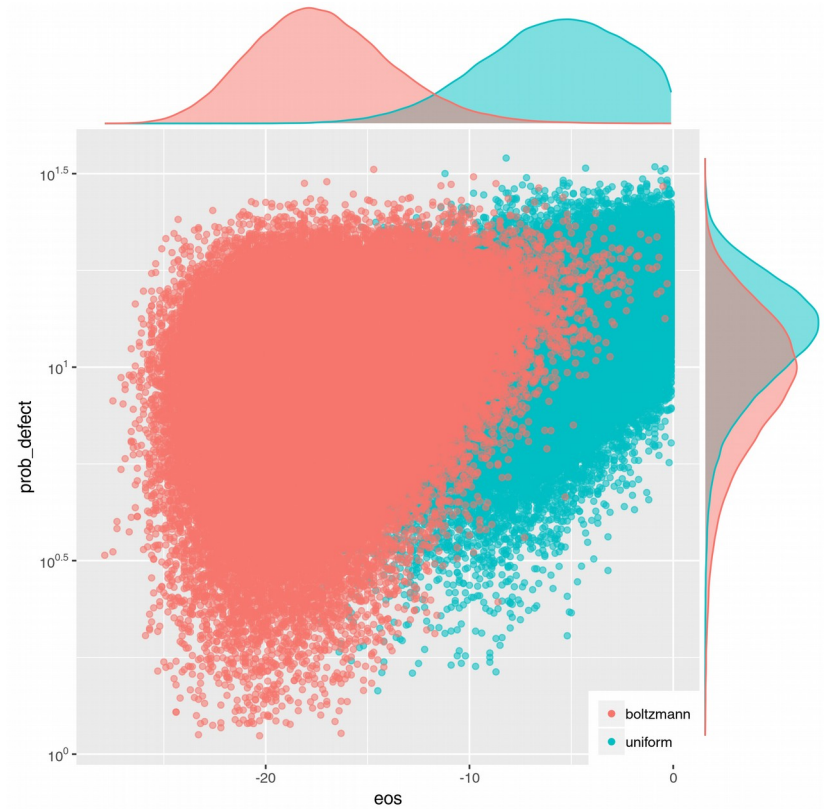
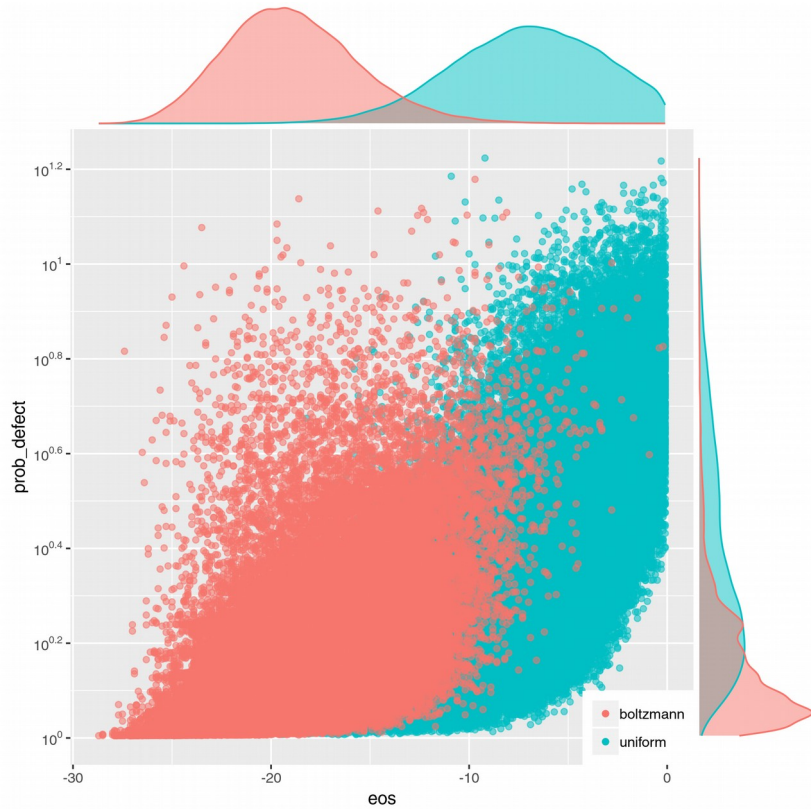
(((((.....))))))(((.....)))))).....



# Probability defect

(((((.....))))))(((.....))))))

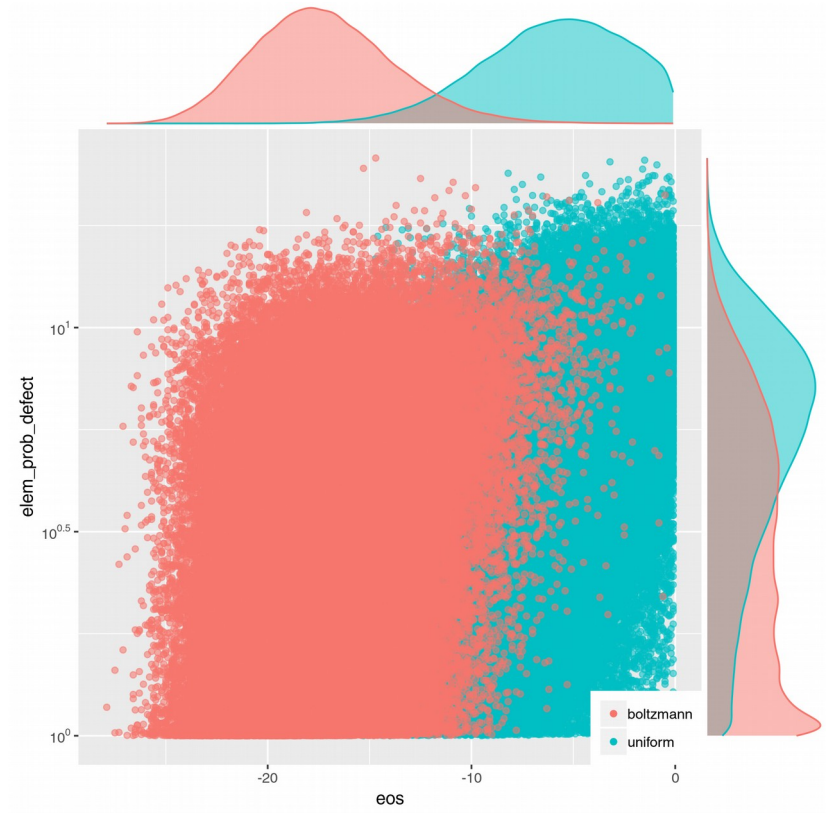
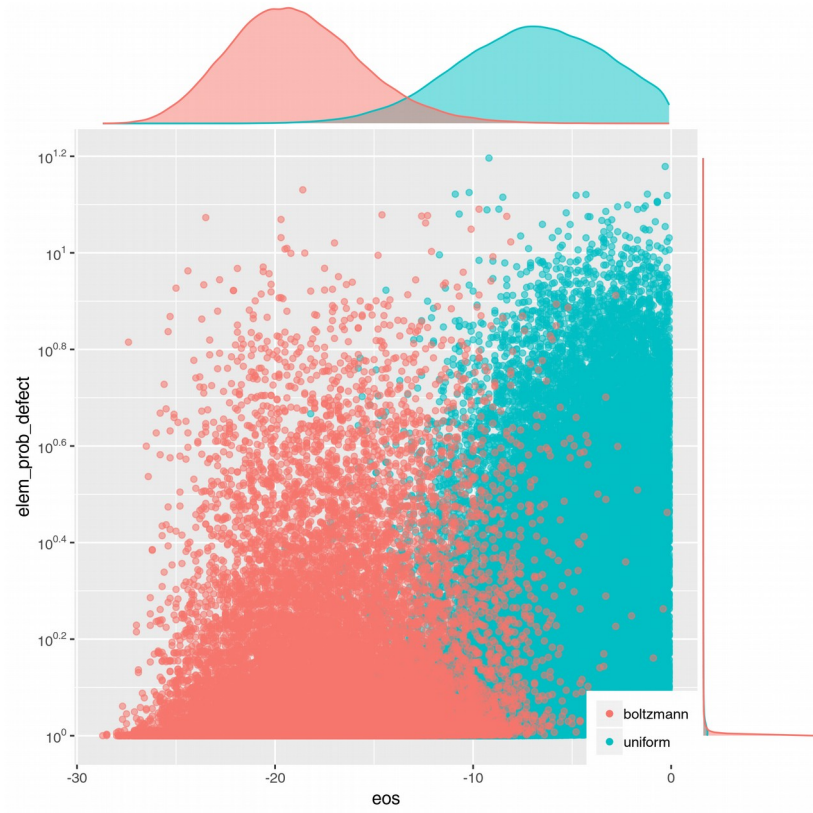
(((((.....))))))(((.....)))))).....



# Element probability defect

((((((....))))))((((((....))))))

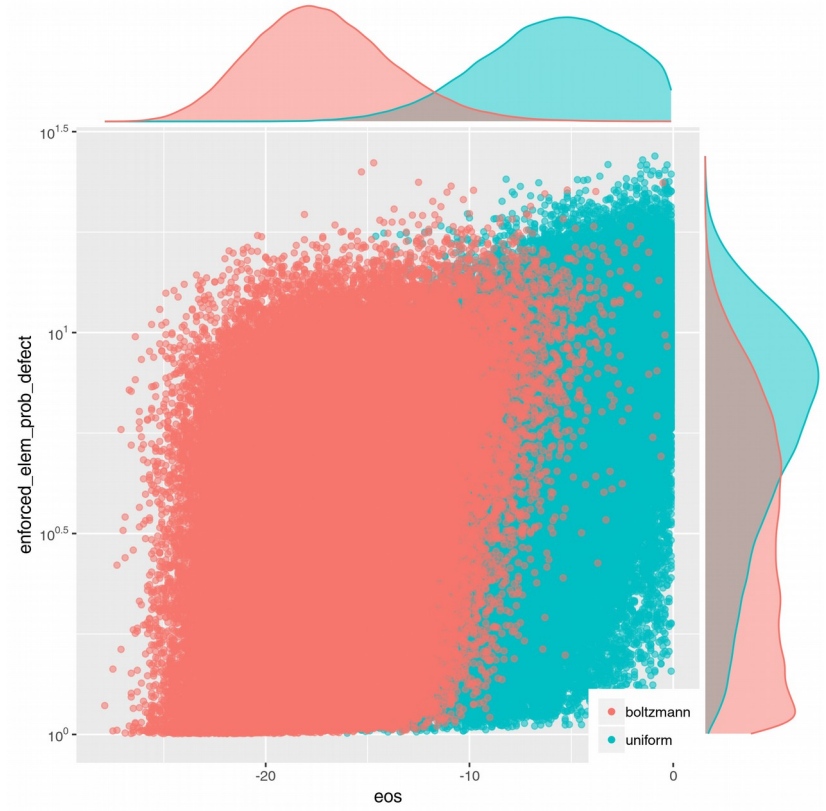
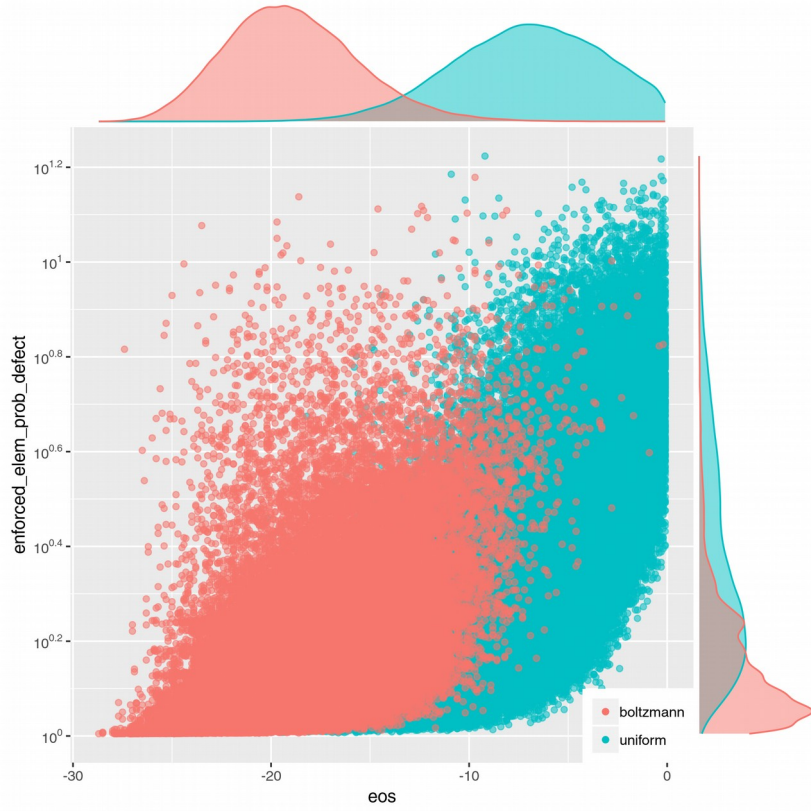
((((((....((((((((....))))))....))))....)))).....



# Enforced element probability defect

((((((....))))))((((((....))))))

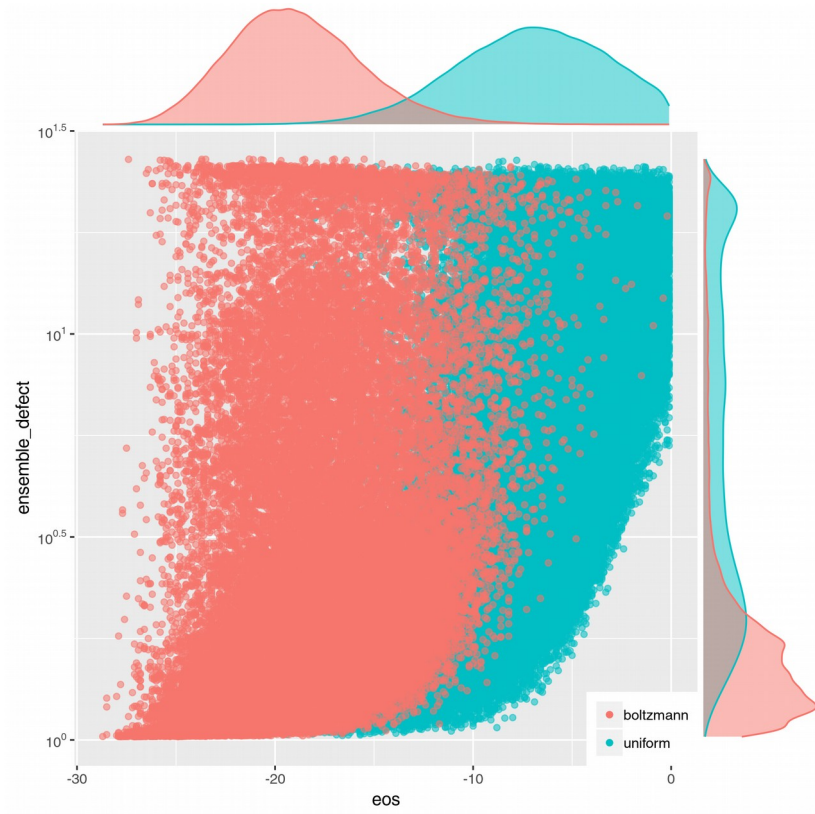
((((((....((((((((....))))))....))))....)))).....



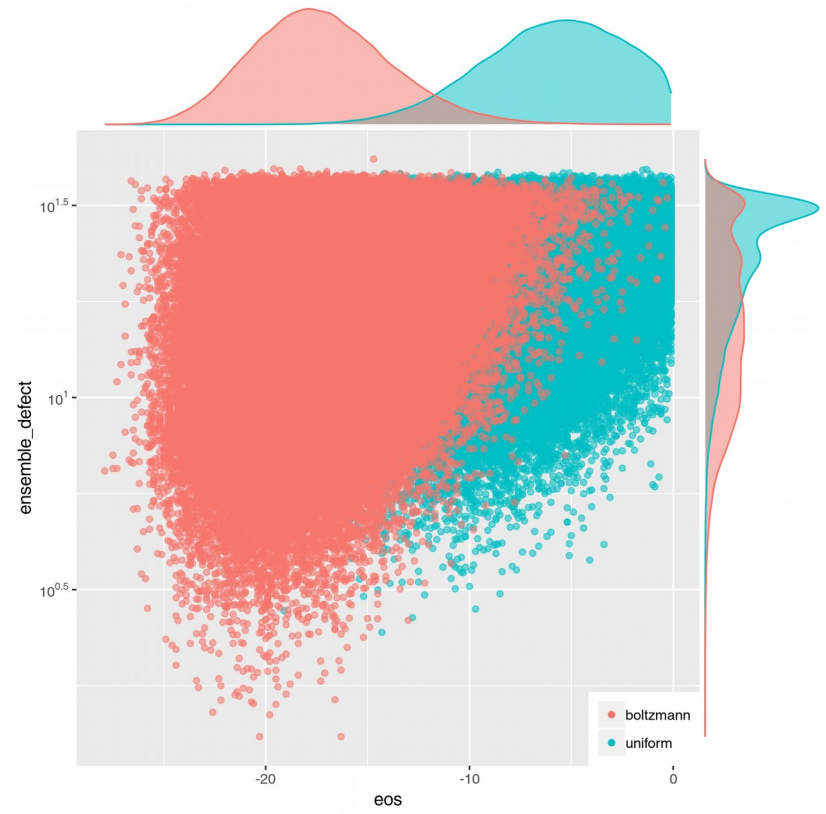


# Ensemble defect

(((((.....))))))(((.....))))))



(((((.....))))))(((.....)))))).....

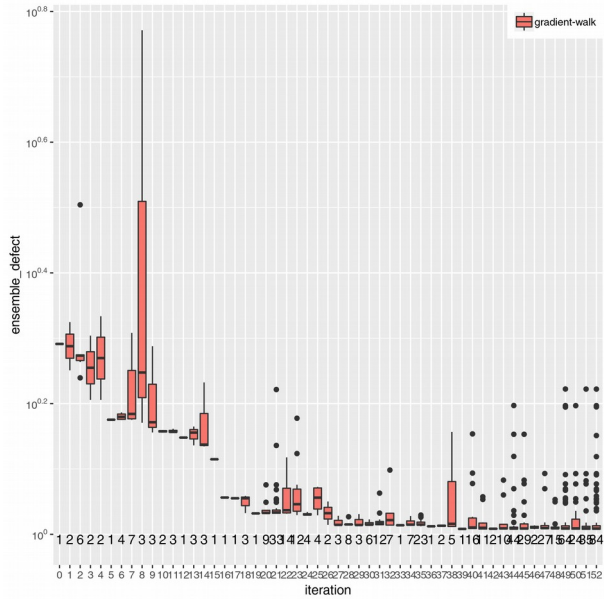


# Optimization methods

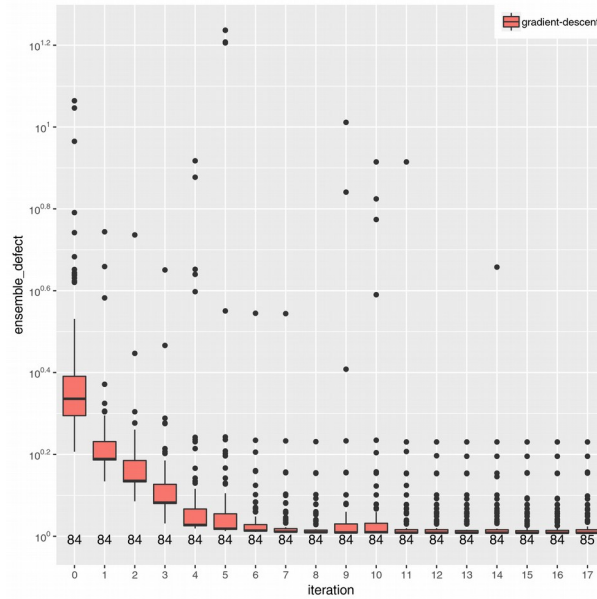
- Gradient walk
  - Accept first better solution
- Gradient descent
  - Accept best neighbouring solution
- Simulated annealing
  - Accept also worse solution with decreasing probability

# Comparison optimization methods

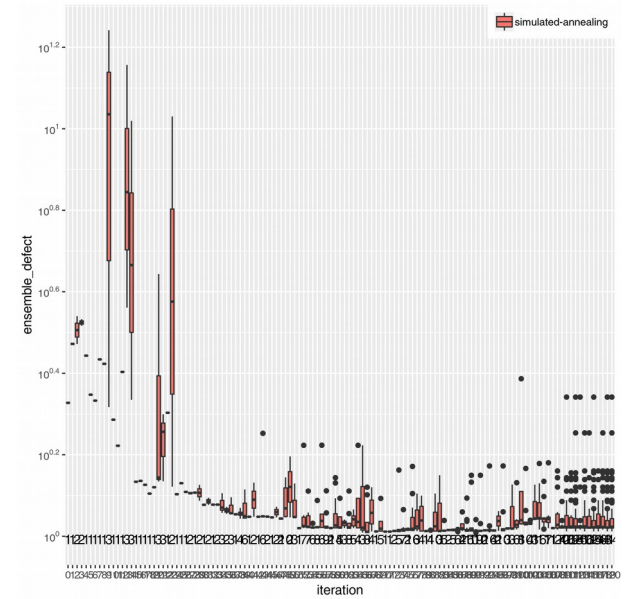
Gradient walk (N=~200)



Gradient descent (N=~1500)

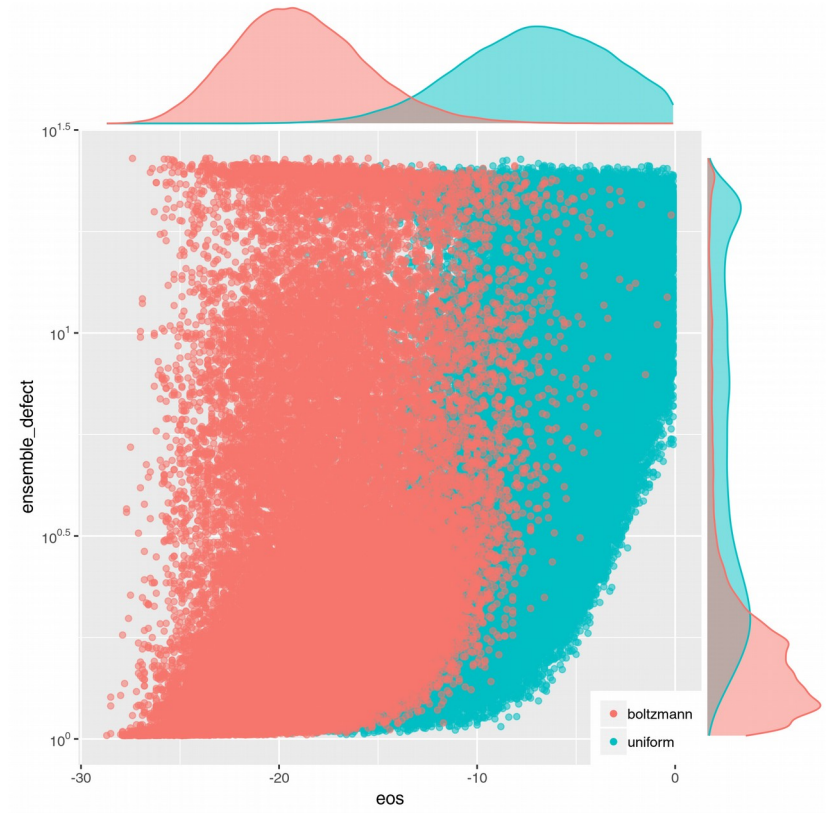
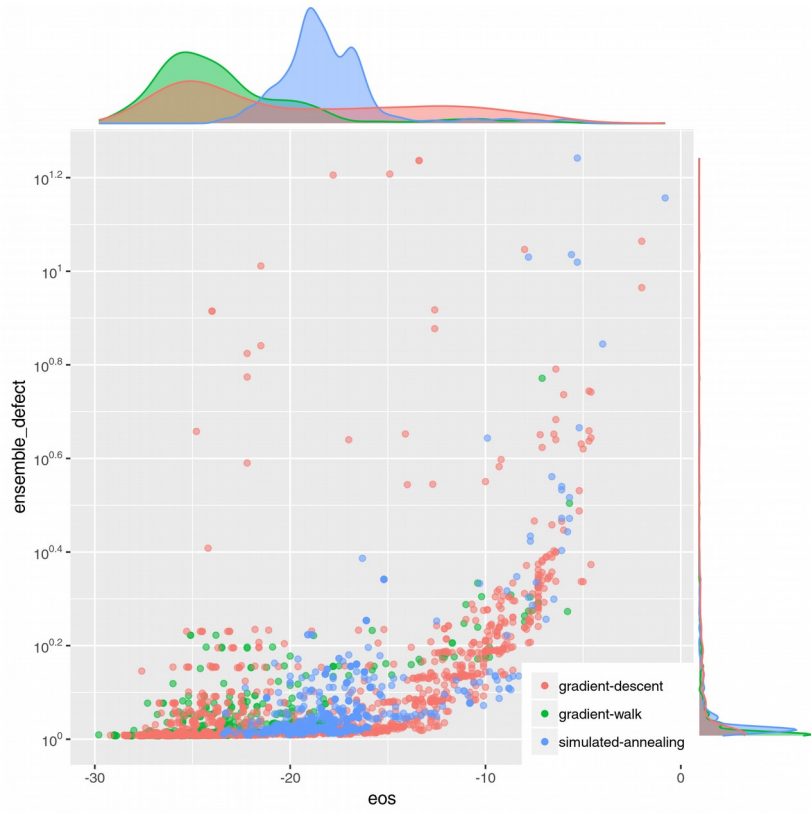


Simulated annealing (N=~200)



(((((((.....))))))(((((((.....))))))

# Comparison optimization methods



(((((((.....))))))(((((((.....))))))

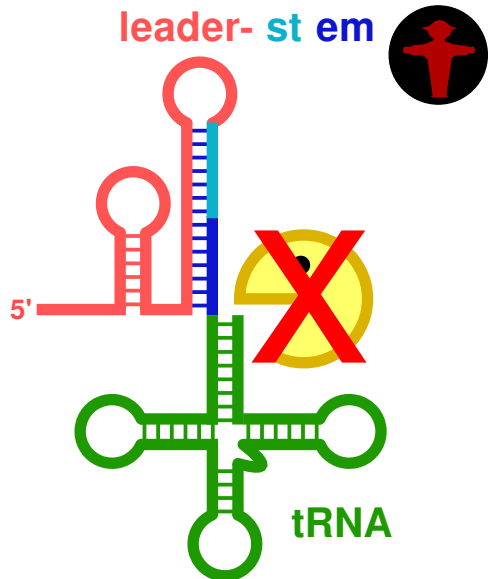
# Multi-state RNA devices

- Conditional states due to trigger:
  - Temperature
  - Ligand binding
  - RNA-RNA interaction
- Simultaneous states

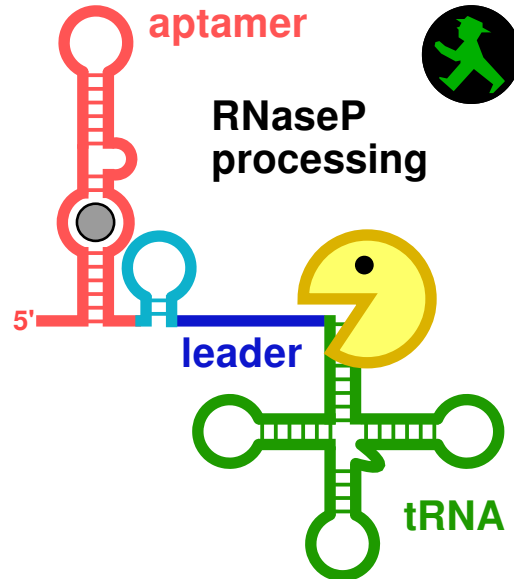
# Conditional states: RNaseP riboswitch

$$f(x) = f(x, \text{condition}_1) \cdot f(x, \text{condition}_2)$$

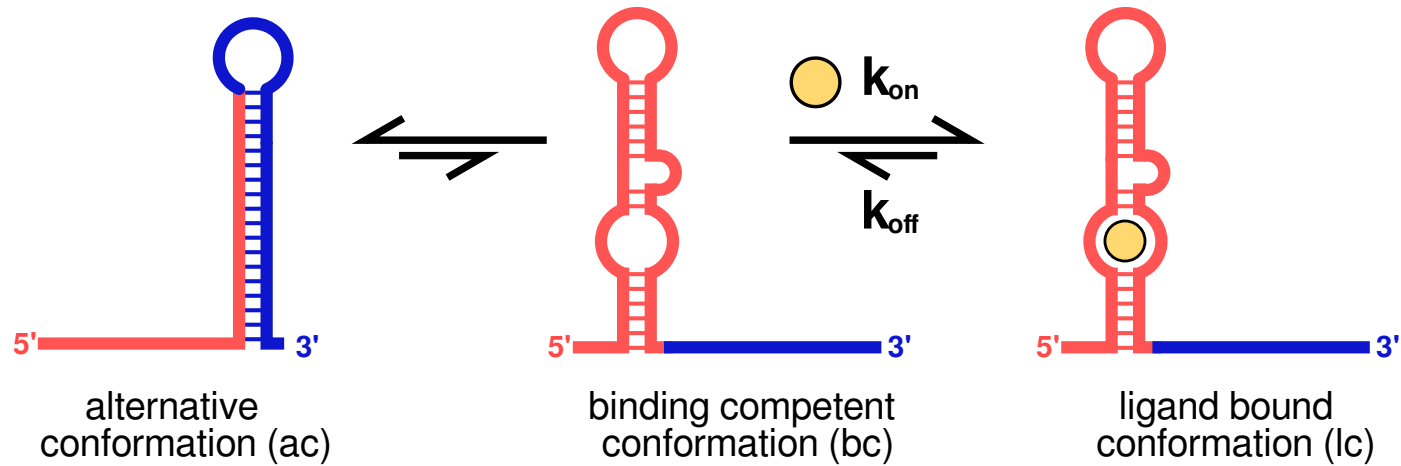
no theophylline



+ theophylline 



# Simultaneous states: Ligand dependent switch



$$f(x) = P(x|\Phi_{1c}) \cdot (1 - |a - P(x|\Phi_{ac})|) \cdot (1 - |b - P(x|\Phi_{bc})|)$$

$$a + b = 1$$

$$0 \leq a, b \leq 1$$

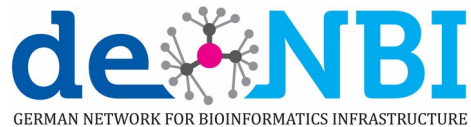
Findeiß, Sven, Stefan Hammer, Michael T. Wolfinger, Felix Kühnl, Christoph Flamm, and Ivo L. Hofacker. 2018. "In Silico Design of Ligand Triggered RNA Switches." *Methods*. <https://doi.org/10.1016/j.ymeth.2018.04.003>.

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<https://arxiv.org/abs/1902.01143>

# Evolving methods for rational *de novo* design of functional RNA molecules

Stefan Hammer, Christian Günzel, Mario Mörl,  
Sven Findeiß

Submitted to **METHODS**, Issue title: Chemical Biology of RNA, Guest  
Editor: Michael Ryckelynck, Jan 2019



# Gradient walk

- $s \leftarrow$  seed sequence
- `gradient_walk(s)`:
  - $\forall t \in \text{neighbours}(s)$ :
    - if  $f(t) < f(s)$ :
      - `gradient_walk(t)`
    - if we saw all neighbours(s):
      - `return(s)`

# Gradient descent

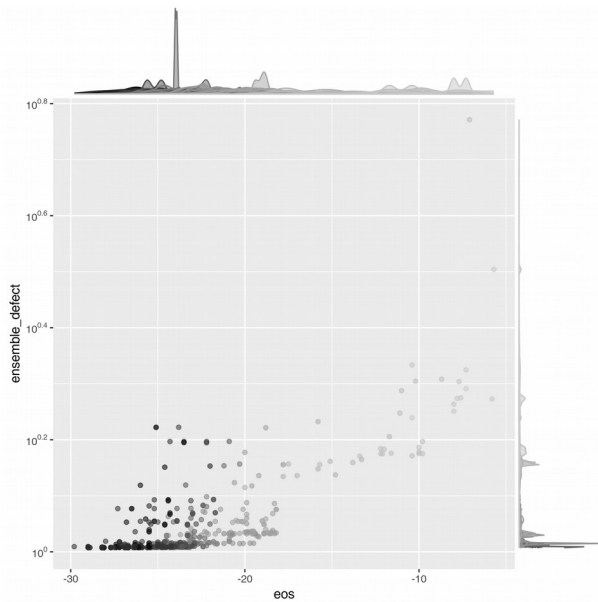
- $s \leftarrow$  seed sequence
- `gradient_descent(s)`:
  - if  $\min(f(t) \forall t \in \text{neighbours}(s)) < f(s)$ :
    - `gradient_descent(s)`
  - else:
    - `return(s)`

# Simulated annealing

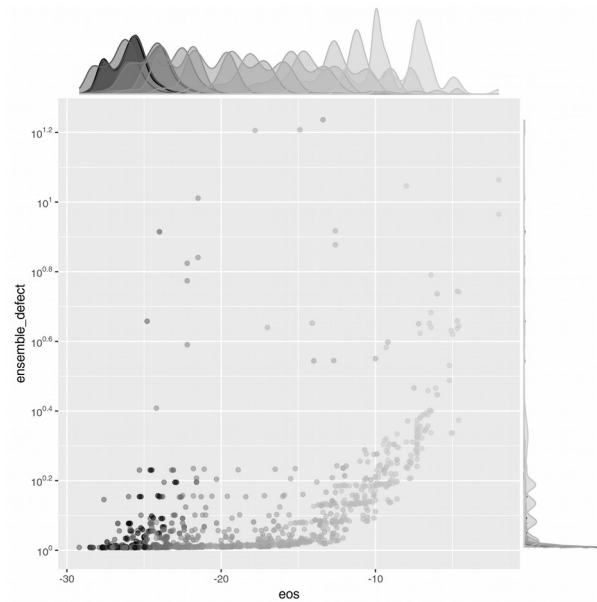
- $s \leftarrow$  seed sequence
- `simulated_annealing(s, temperature):`
  - $\forall t \in \text{neighbours}(s):$ 
    - $p \leftarrow e^{-1 \cdot (f(t) - f(s)) / \text{temperature}}$
    - $r \leftarrow \text{random}([0, 1])$
    - if  $r \leq p:$ 
      - `simulated_annealing(t, temperature*0.75)`
  - if we saw all neighbours(s):
    - `return(s)`

# Comparison optimization methods

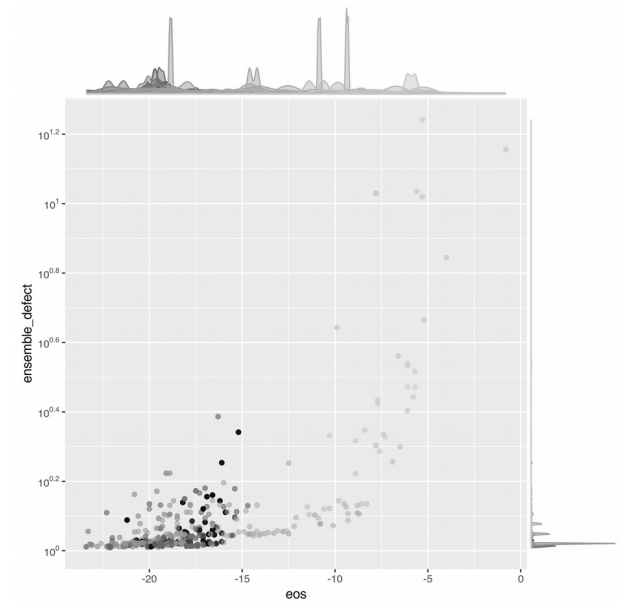
Gradient walk



Gradient descent



Simulated annealing



(((((((.....))))))(((((((.....))))))





