

What we can Learn in Evolution from RNA Molecules

Peter Schuster

Institut für Theoretische Chemie
und Molekulare Strukturbiologie
Universität Wien, Austria

and The Santa Fe Institute
Santa Fe, New Mexico
USA



Lab Inauguration Meeting

Köln, 03.12.2004

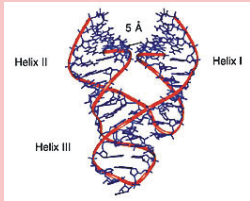
Web-Page for further information:

<http://www.tbi.univie.ac.at/~pks>

1. RNA and properties and function
2. RNA structures
3. Neutral networks and intersections
4. RNA evolution *in silico*
5. Intersection molecules and RNA switches
6. Neutrality in evolution and design

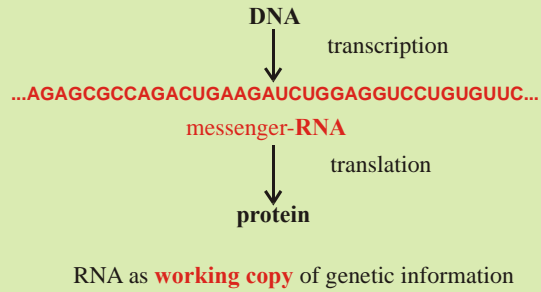
- 1. RNA and properties and function**
2. RNA structures
3. Neutral networks and intersections
4. RNA evolution *in silico*
5. Intersection molecules and RNA switches
6. Neutrality in evolution and design

RNA as catalyst

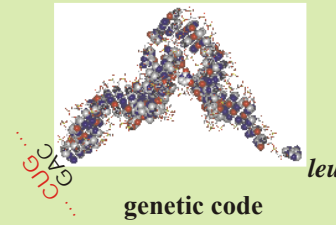


Ribozyme

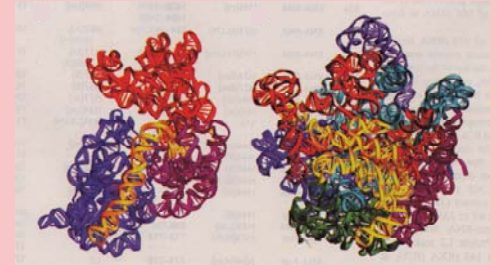
RNA as transmitter of genetic information



RNA as adapter molecule



RNA is the catalytic subunit in supramolecular complexes



The **ribosome** is a **ribozyme** !

The RNA world as a precursor of the current DNA + protein biology

RNA

RNA is modified by epigenetic control

RNA editing

Alternative splicing of messenger RNA

RNA as carrier of genetic information

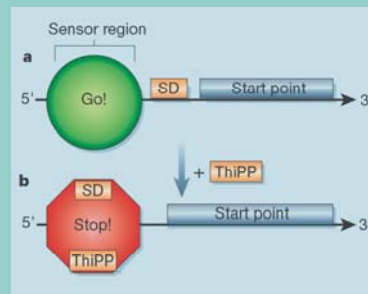
RNA viruses and retroviruses

RNA evolution *in vitro*

Evolutionary biotechnology

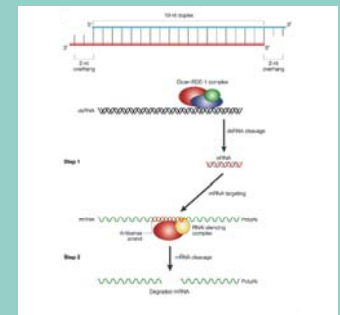
RNA aptamers, artificial ribozymes, allosteric ribozymes

Allosteric control of transcribed RNA



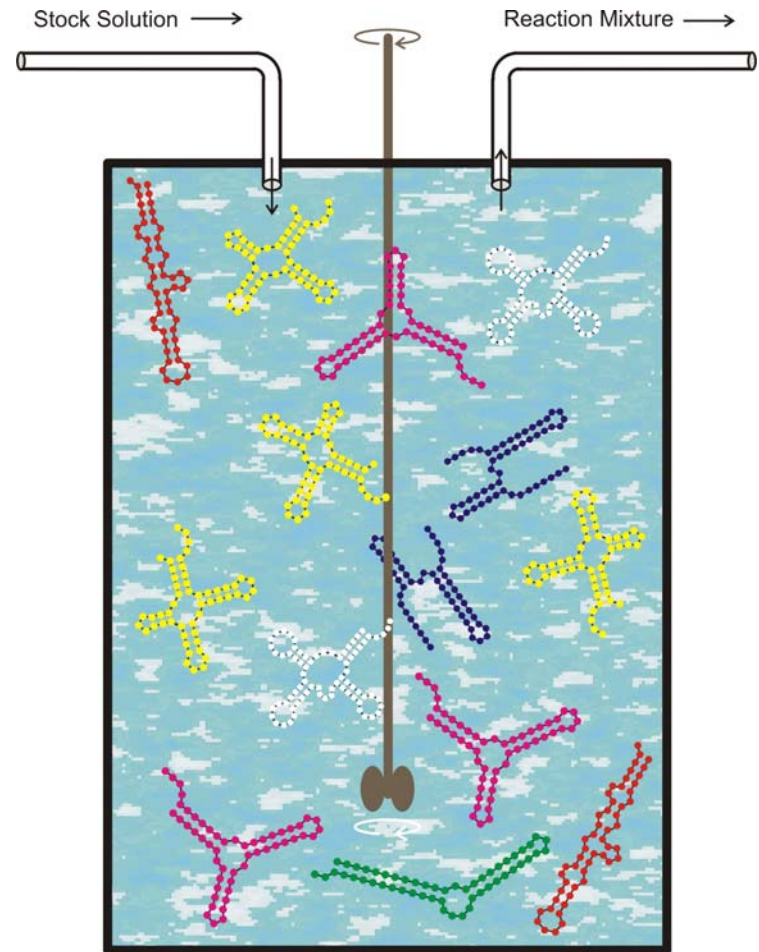
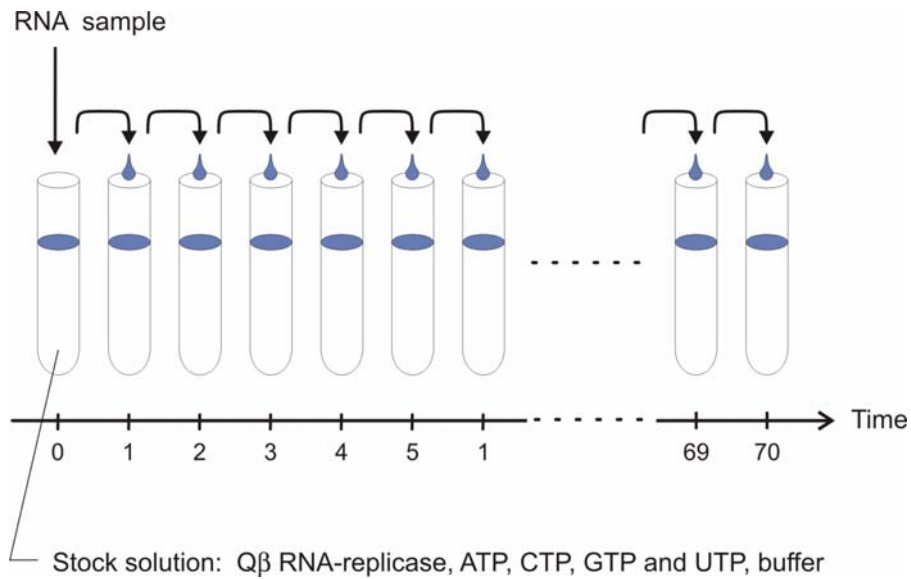
Riboswitches controlling transcription and translation through **metabolites**

RNA as regulator of gene expression

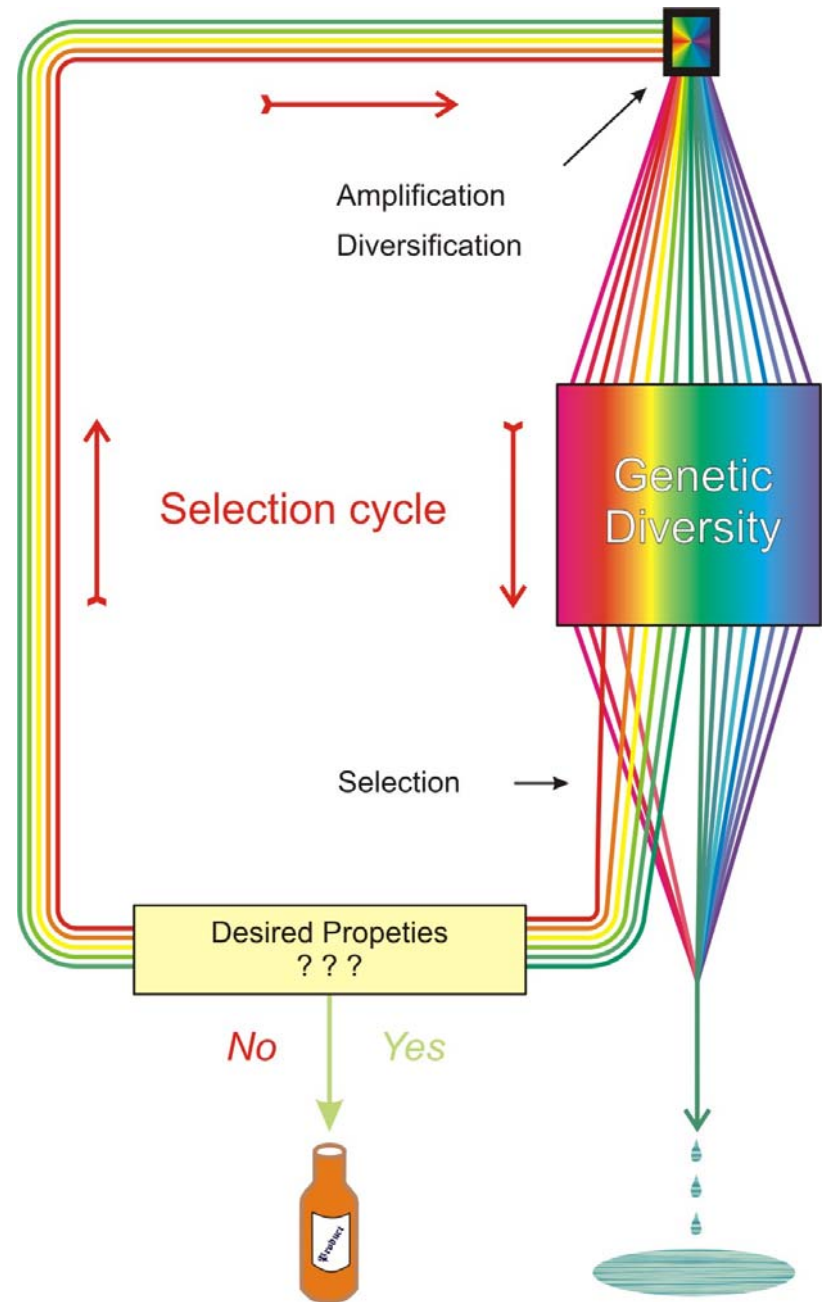


Gene silencing by small interfering RNAs

Functions of RNA molecules

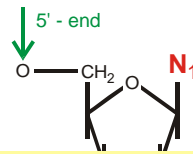


Examples of 'natural selection' with RNA molecules

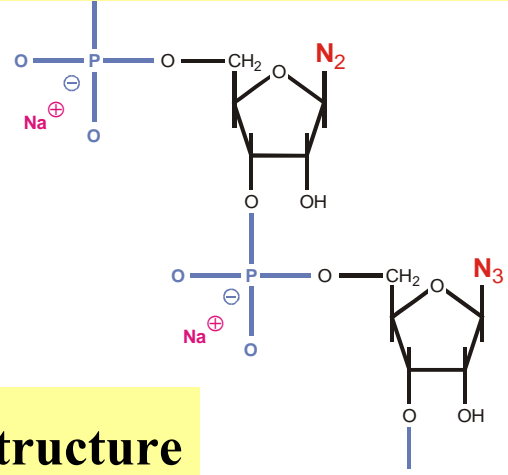


An example of 'artificial selection' with RNA molecules or 'breeding' of biomolecules

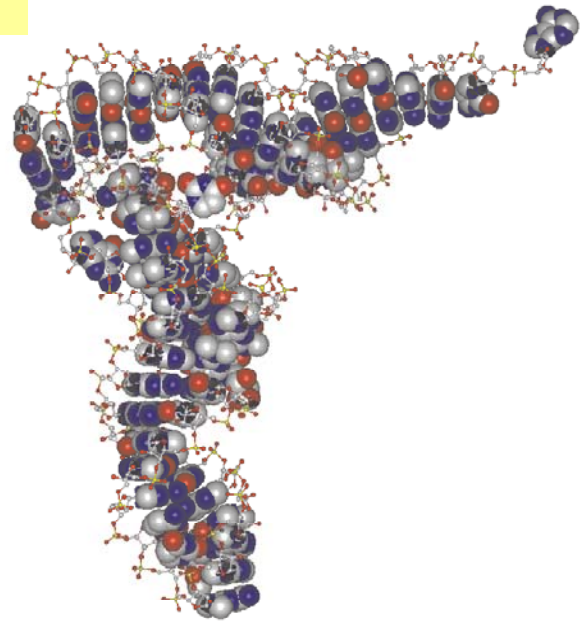
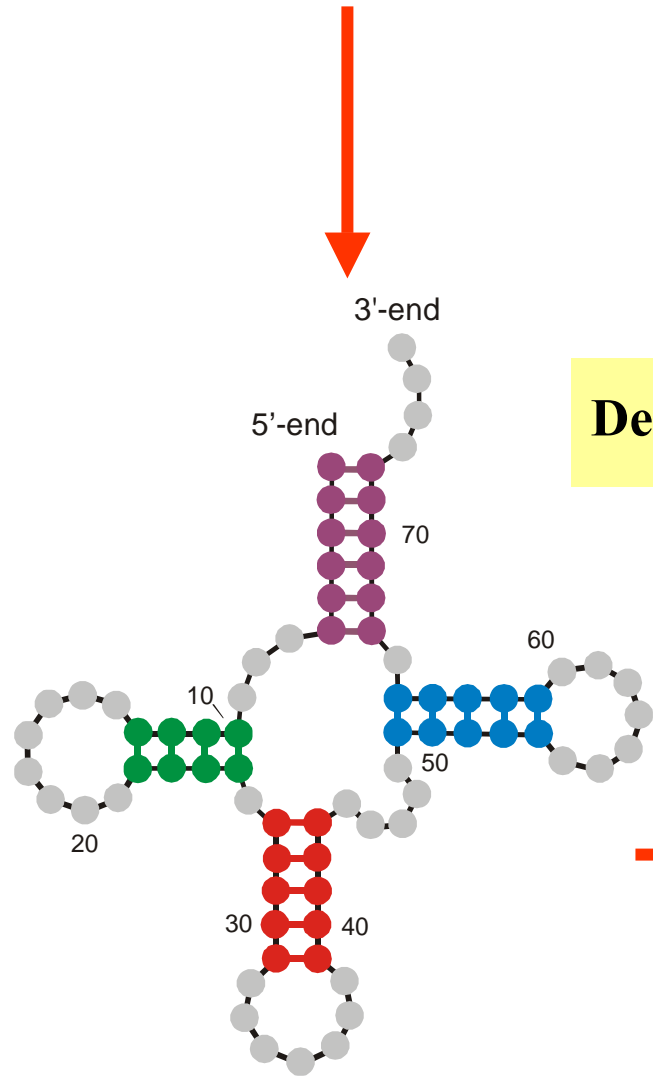
1. RNA and properties and function
- 2. RNA structures**
3. Neutral networks and intersections
4. RNA evolution *in silico*
5. Intersection molecules and RNA switches
6. Neutrality in evolution and design



5'-end **GCGGAUUUAGCUC**AGUUGGGAGAG**CGCCAGACUGAAGAUCUGG**AGGUC**CUGUGUUCGAUCCACAGAAUUCGCACCA** 3'-end



Definition of RNA structure



Definition and **physical relevance** of RNA secondary structures

RNA secondary structures are listings of Watson-Crick and GU wobble base pairs, which are free of knots and pseudoknots.

D.Thirumalai, N.Lee, S.A.Woodson, and D.K.Klimov.
Annu.Rev.Phys.Chem. **52**:751-762 (2001):

„Secondary structures are folding intermediates in the formation of full three-dimensional structures.“

Fast Folding and Comparison of RNA Secondary Structures

I. L. Hofacker^{1,*}, W. Fontana³, P. F. Stadler^{1,3}, L. S. Bonhoeffer⁴, M. Tacker¹
and P. Schuster^{1,2,3}

¹ Institut für Theoretische Chemie, Universität Wien, A-1090 Wien, Austria

² Institut für Molekulare Biotechnologie, D-07745 Jena, Federal Republic of Germany

³ Santa Fe Institute, Santa Fe, NM 87501, U.S.A.

⁴ Department of Zoology, University of Oxford, South Parks Road, Oxford OX1 3PS, U.K.

Summary. Computer codes for computation and comparison of RNA secondary structures, the Vienna RNA package, are presented, that are based on dynamic programming algorithms and aim at predictions of structures with minimum free energies as well as at computations of the equilibrium partition functions and base pairing probabilities.

An efficient heuristic for the inverse folding problem of RNA is introduced. In addition we present compact and efficient programs for the comparison of RNA secondary structures based on tree editing and alignment.

All computer codes are written in ANSI C. They include implementations of modified algorithms on parallel computers with distributed memory. Performance analysis carried out on an Intel Hypercube shows that parallel computing becomes gradually more and more efficient the longer the sequences are.

Keywords. Inverse folding; parallel computing; public domain software; RNA folding; RNA secondary structures; tree editing.

Schnelle Faltung und Vergleich von Sekundärstrukturen von RNA

Zusammenfassung. Die im Vienna RNA package enthaltenen Computer Programme für die Berechnung und den Vergleich von RNA Sekundärstrukturen werden präsentiert. Ihren Kern bilden Algorithmen zur Vorhersage von Strukturen minimaler Energie sowie zur Berechnung von Zustandssumme und Basenpaarungswahrscheinlichkeiten mittels dynamischer Programmierung.

Ein effizienter heuristischer Algorithmus für das inverse Faltungsproblem wird vorgestellt. Darüberhinaus präsentieren wir kompakte und effiziente Programme zum Vergleich von RNA Sekundärstrukturen durch Baum-Editierung und Alignierung.

Alle Programme sind in ANSI C geschrieben, darunter auch eine Implementation des Faltungsalgorithmus für Parallelrechner mit verteiltem Speicher. Wie Tests auf einem Intel Hypercube zeigen, wird das Parallelrechnen umso effizienter je länger die Sequenzen sind.

1. Introduction

Recent interest in RNA structures and functions was caused by their catalytic capacities [1, 2] as well as by the success of selection methods in producing RNA

The *Vienna RNA-Package*:

A library of routines for folding,
inverse folding, sequence and
structure alignment, cofolding,
kinetic folding, ...

RNA sequence

GUAUCGAAAUACGUAGCGUAUGGGGAUGCUGGACGGUCCCAUCGGUACUCCA

RNA folding:
Structural biology,
spectroscopy of
biomolecules,
understanding
molecular function

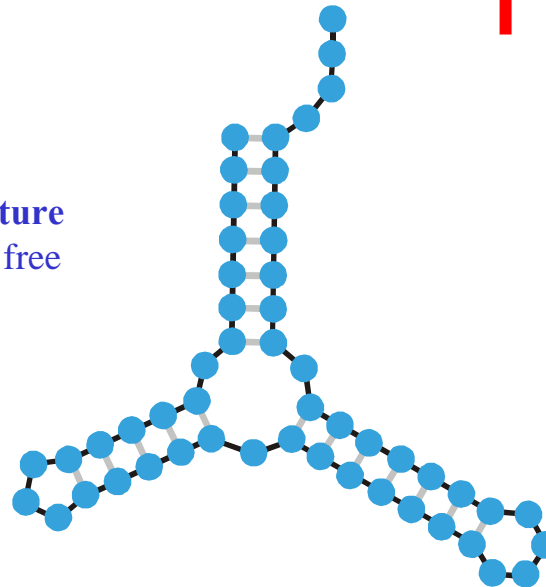
Biophysical chemistry:
thermodynamics and
kinetics



Empirical parameters

Inverse folding of RNA:
Biotechnology,
design of biomolecules
with predefined
structures and functions

RNA structure
of minimal free
energy

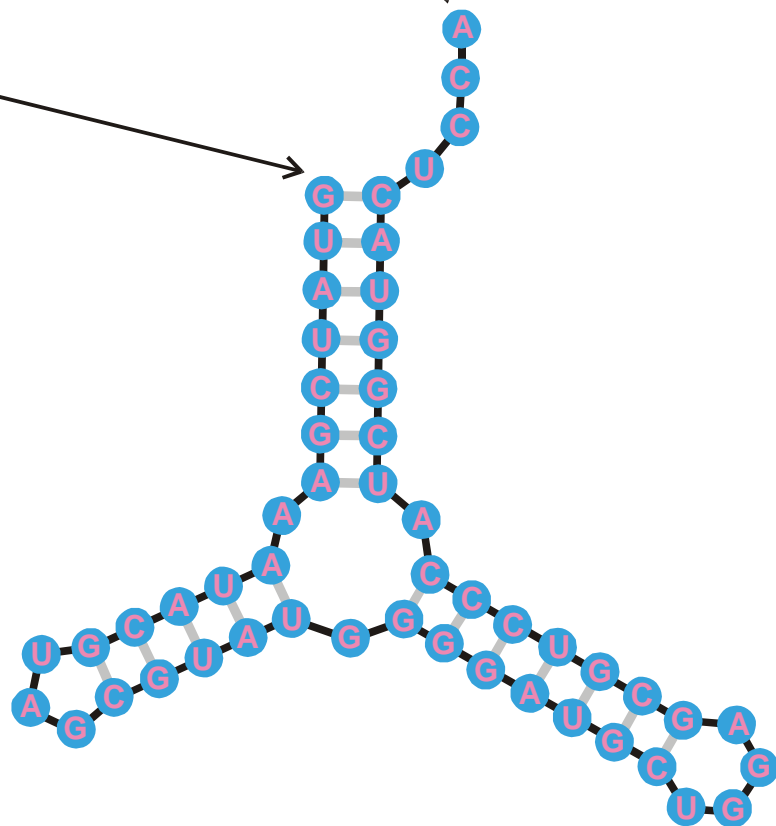
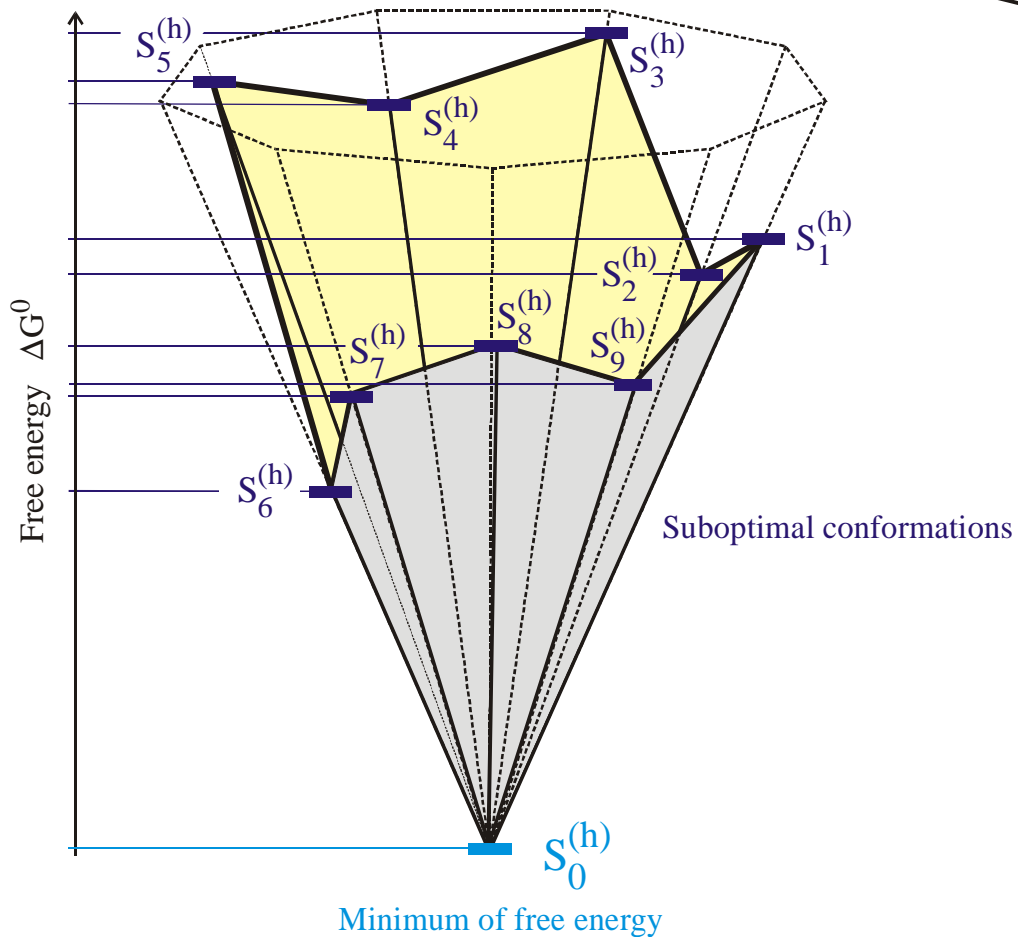


Sequence, structure, and design

5'-end

3'-end

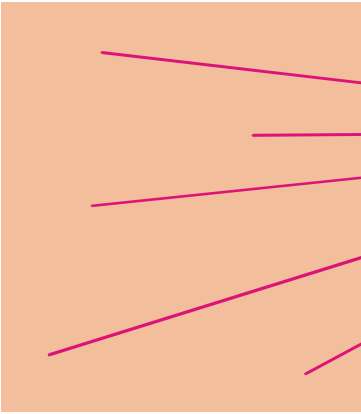
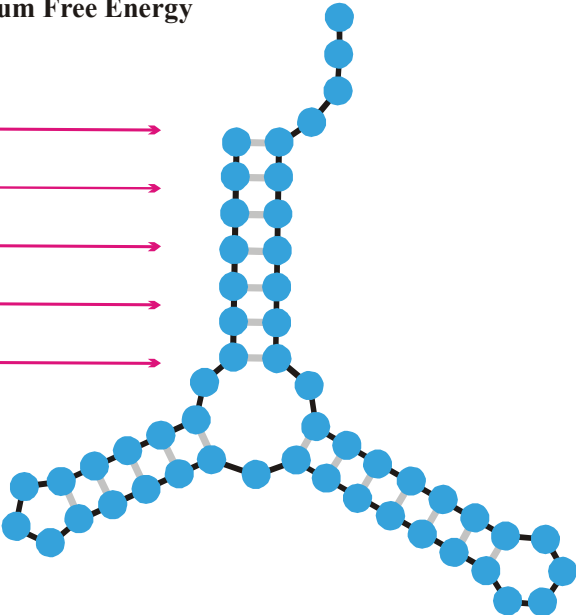
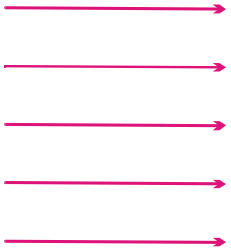
GUAUCGAAUACGUAGCGUAUGGGGAUGCUGGACGGUCCCAUCGGUACUCCA



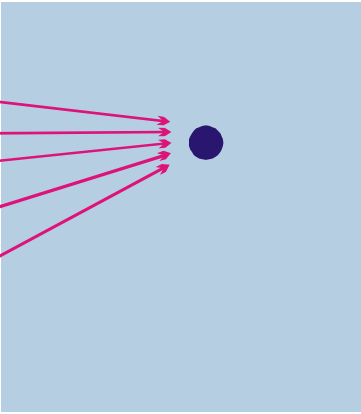
The minimum free energy structures on a discrete space of conformations

**Criterion of
Minimum Free Energy**

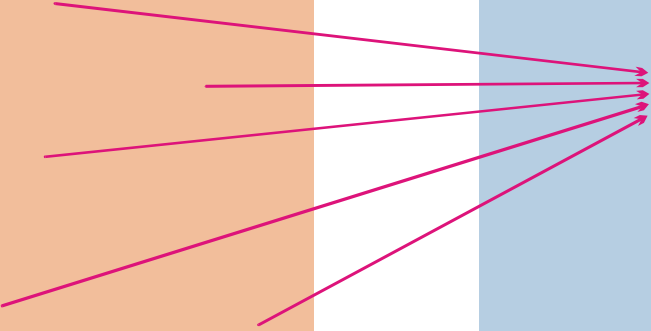
UUUAGCCAGCGCGAGUCGUGCGGACGGGUUAUCUCUGUCGGGCUAGGGCGC
GUGAGCGCGGGGCACAGUUUCUCAAGGAUGUAAGUUUUUGCCGUUUAUCUGG
UUAGCGAGAGAGGAGGCUUCUAGACCCAGCUCUCUGGGUCGUUGCUGAUGCG
CAUUGGUGCUAAUGAUUUAGGGCUGUAUUCUGUAUAGCGAUCAGUGUCCG
GUAGGCCUCUUGACAUAAGAUUUUUCCAUGGUGGGAGAUGGCCAUUGCAG



Sequence Space



Shape Space



From sequences to shapes and back: a case study in RNA secondary structures

PETER SCHUSTER^{1,2,3}, WALTER FONTANA³, PETER F. STADLER^{2,3}
AND IVO L. HOFACKER²

¹ Institut für Molekulare Biotechnologie, Beutenbergstrasse 11, PF 100813, D-07708 Jena, Germany

² Institut für Theoretische Chemie, Universität Wien, Austria

³ Santa Fe Institute, Santa Fe, U.S.A.

SUMMARY

RNA folding is viewed here as a map assigning secondary structures to sequences. At fixed chain length the number of sequences far exceeds the number of structures. Frequencies of structures are highly non-uniform and follow a generalized form of Zipf's law: we find relatively few common and many rare ones. By using an algorithm for inverse folding, we show that sequences sharing the same structure are distributed randomly over sequence space. All common structures can be accessed from an arbitrary sequence by a number of mutations much smaller than the chain length. The sequence space is percolated by extensive neutral networks connecting nearest neighbours folding into identical structures. Implications for evolutionary adaptation and for applied molecular evolution are evident: finding a particular structure by mutation and selection is much simpler than expected and, even if catalytic activity should turn out to be sparse in the space of RNA structures, it can hardly be missed by evolutionary processes.

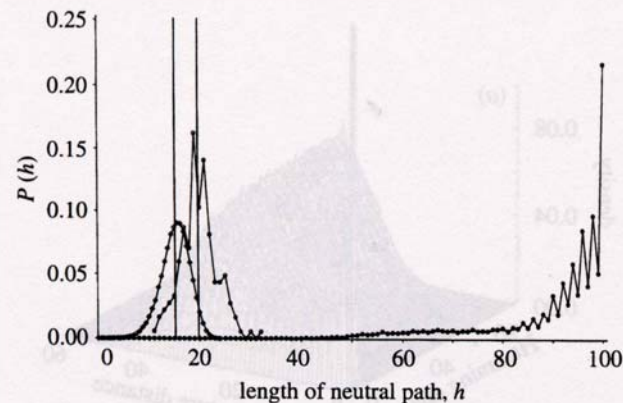
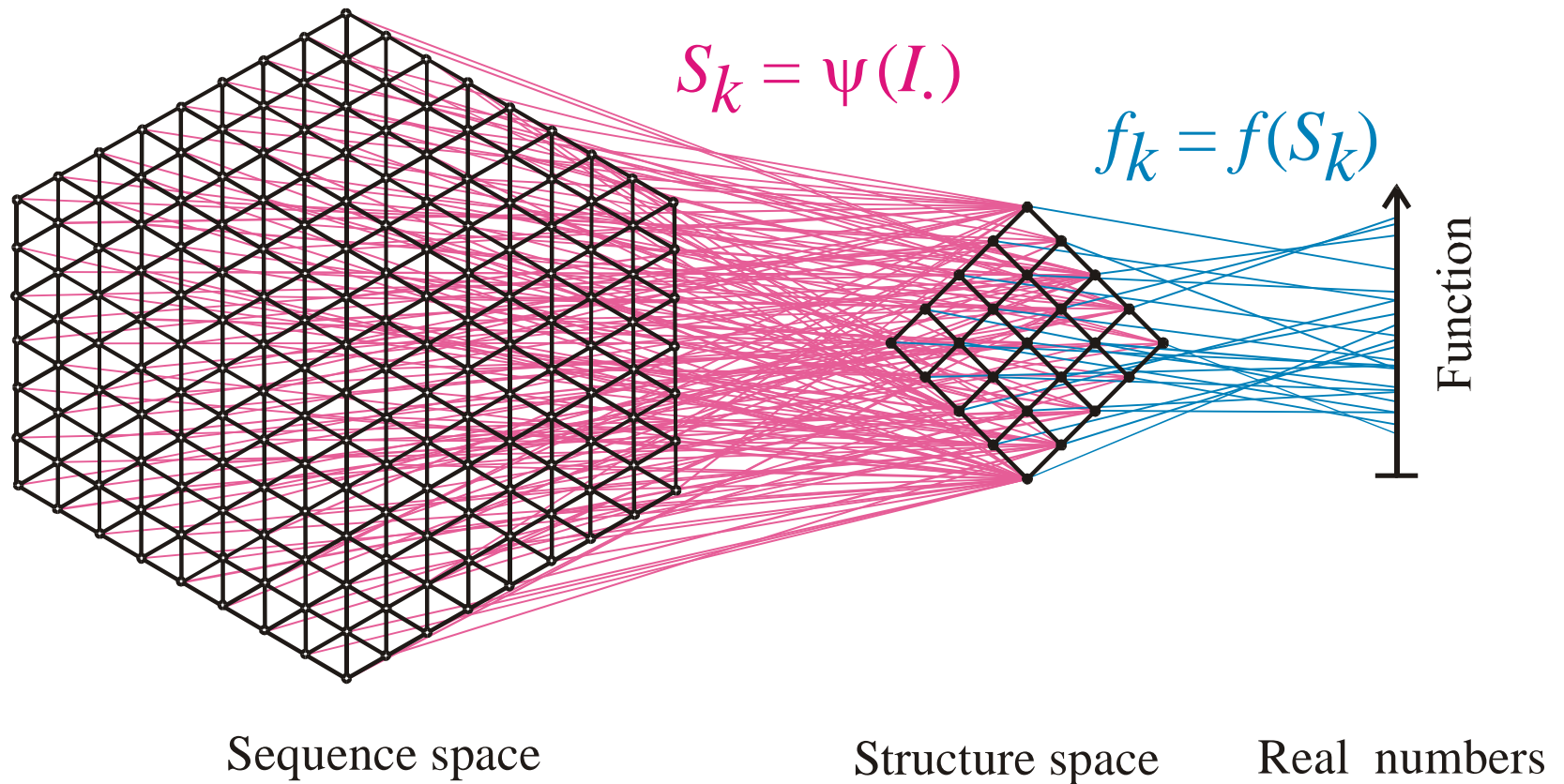
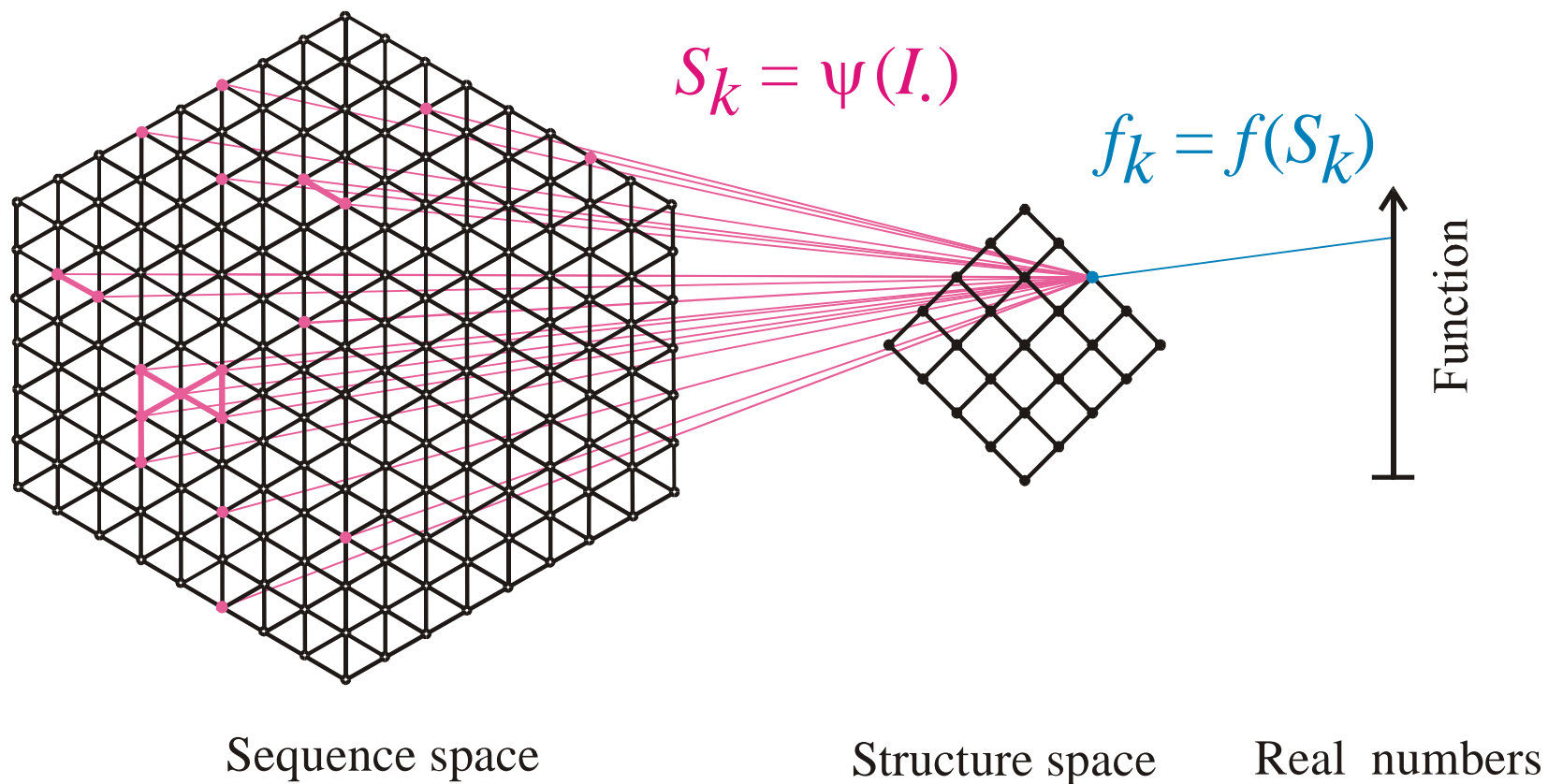


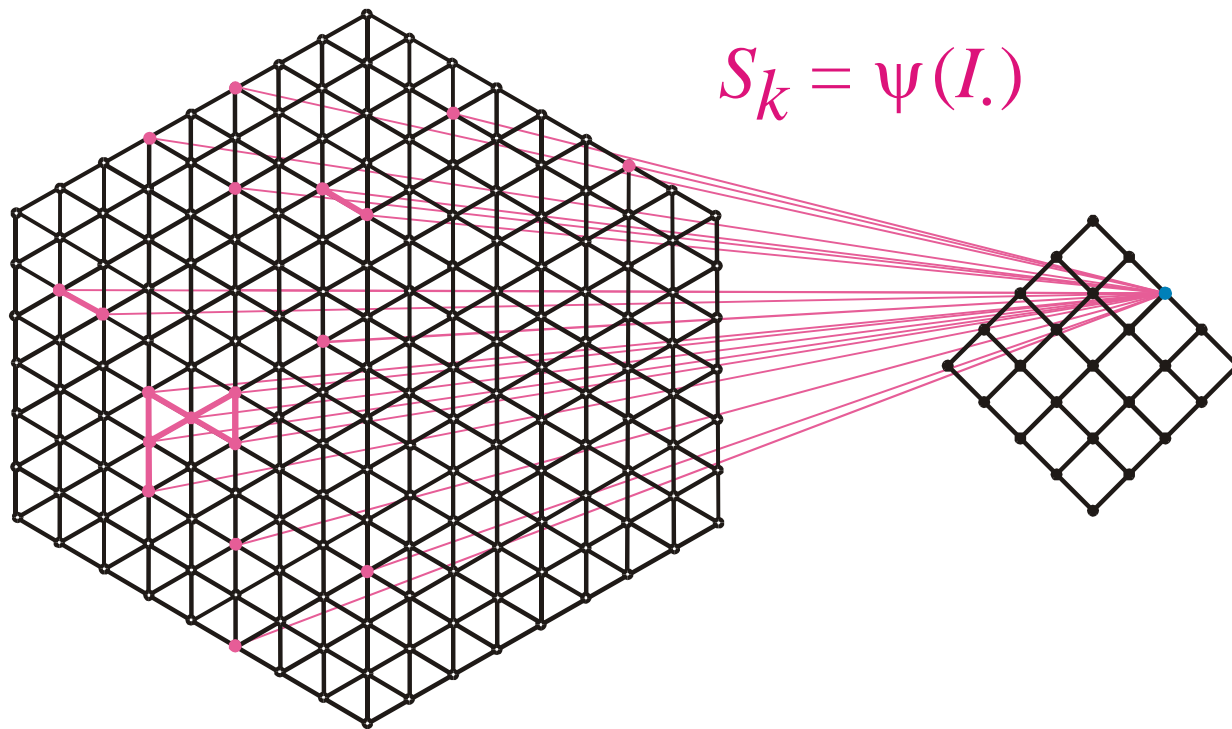
Figure 4. Neutral paths. A neutral path is defined by a series of nearest neighbour sequences that fold into identical structures. Two classes of nearest neighbours are admitted: neighbours of Hamming distance 1, which are obtained by single base exchanges in unpaired stretches of the structure, and neighbours of Hamming distance 2, resulting from base pair exchanges in stacks. Two probability densities of Hamming distances are shown that were obtained by searching for neutral paths in sequence space: (i) an upper bound for the closest approach of trial and target sequences (open circles) obtained as endpoints of neutral paths approaching the target from a random trial sequence (185 targets and 100 trials for each were used); (ii) a lower bound for the closest approach of trial and target sequences (open diamonds) derived from secondary structure statistics (Fontana *et al.* 1993a; see this paper, §4); and (iii) longest distances between the reference and the endpoints of monotonously diverging neutral paths (filled circles) (500 reference sequences were used).

1. RNA and properties and function
2. RNA structures
- 3. Neutral networks and intersections**
4. RNA evolution *in silico*
5. Intersection molecules and RNA switches
6. Neutrality in evolution and design



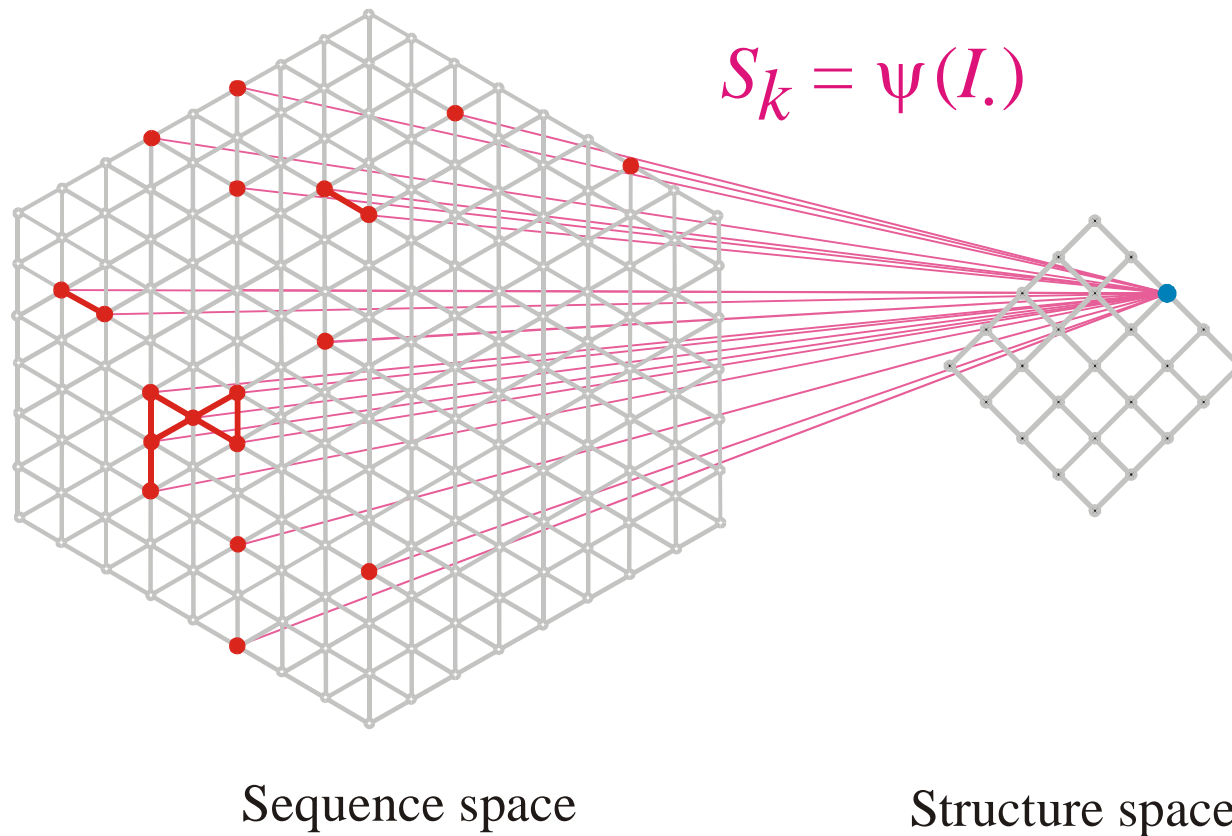
Mapping from sequence space into structure space and into function





Sequence space

Structure space



The pre-image of the structure S_k in sequence space is the **neutral network G_k**

I_1 : CGTCGTTACAATTTA **G**GTTATGTGCGAATTC **A**CAAATT **G**AAAA **T**ACAAGAG
 I_2 : CGTCGTTACAATTTA **A**GTTATGTGCGAATTC **C**CAAATT **A**AAAA **C**ACAAGAG

Hamming distance $d_H(I_1, I_2) = 4$

- (i) $d_H(I_1, I_1) = 0$
- (ii) $d_H(I_1, I_2) = d_H(I_2, I_1)$
- (iii) $d_H(I_1, I_3) \leq d_H(I_1, I_2) + d_H(I_2, I_3)$

The Hamming distance between genotypes induces a metric in sequence space

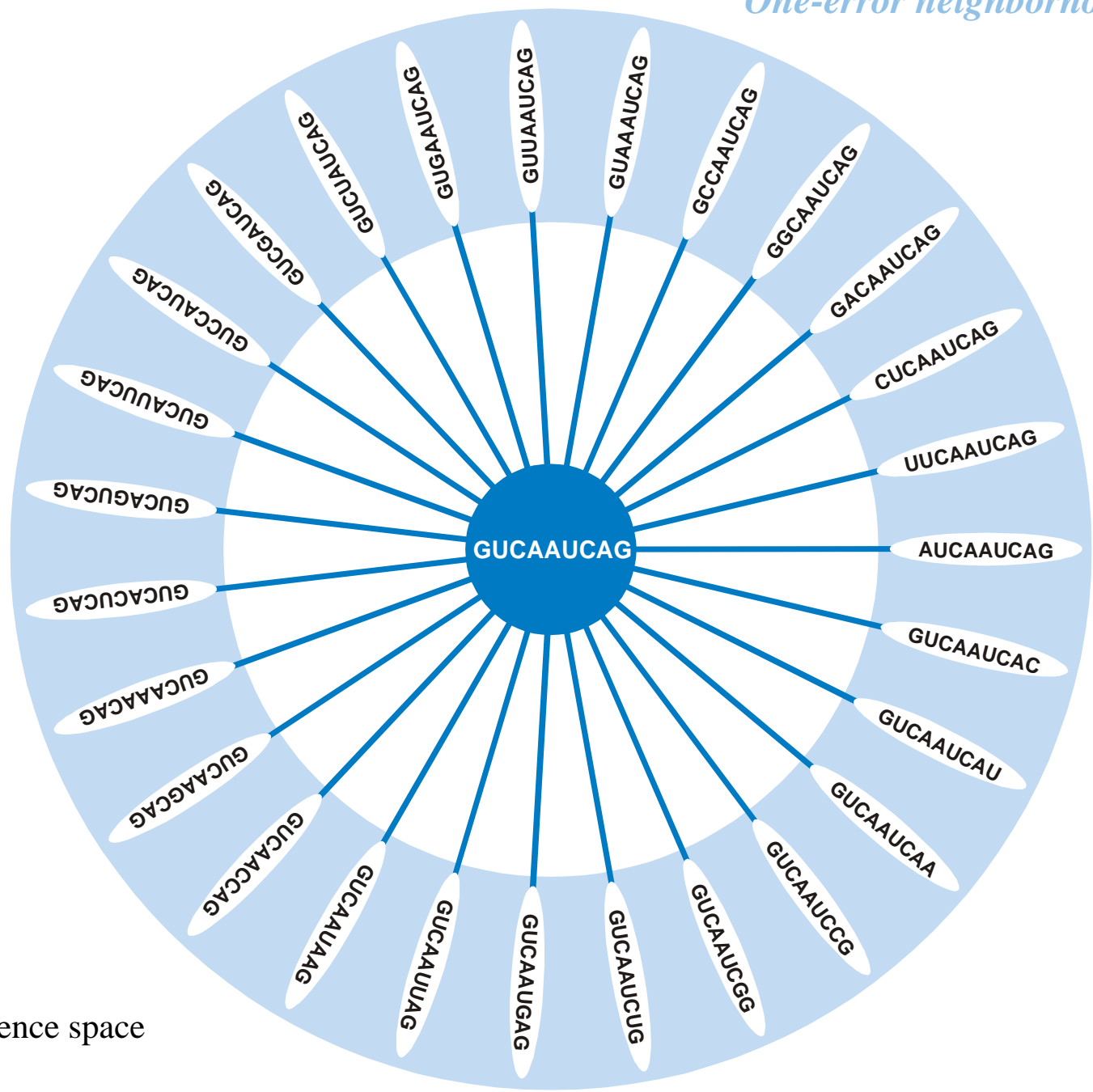
Neutral networks are sets of sequences forming the same object in a phenotype space. The neutral network \mathbf{G}_k is, for example, the pre-image of the structure S_k in sequence space:

$$\mathbf{G}_k = \Psi^{-1}(S_k) \quad \{\psi_j \mid \Psi(I_j) = S_k\}$$

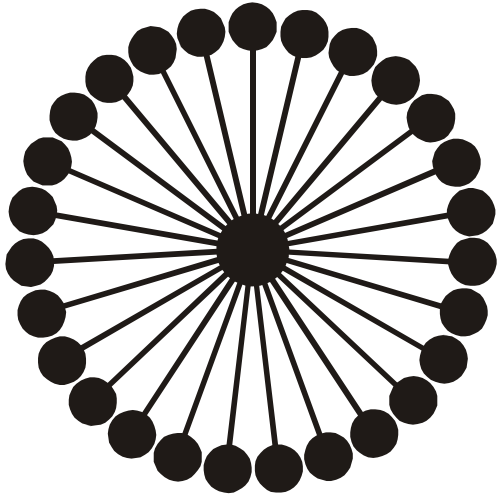
The set is converted into a graph by connecting all sequences of Hamming distance one.

Neutral networks of small biomolecules can be computed by exhaustive folding of complete sequence spaces, i.e. all RNA sequences of a given chain length. This number, $N=4^n$, becomes very large with increasing length, and is prohibitive for numerical computations.

Neutral networks can be modelled by **random graphs** in sequence space. In this approach, nodes are inserted randomly into sequence space until the size of the pre-image, i.e. the number of neutral sequences, matches the neutral network to be studied.

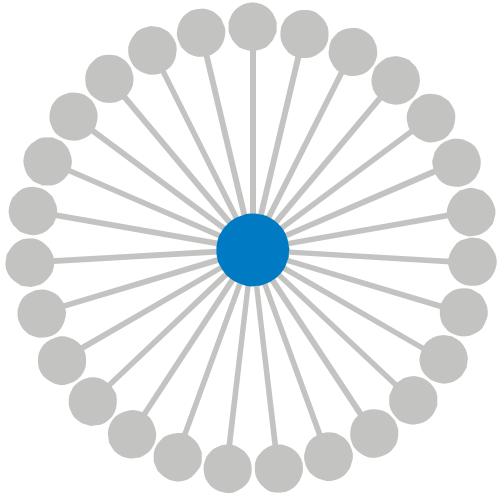


The surrounding of **GUCAAUCAG** in sequence space

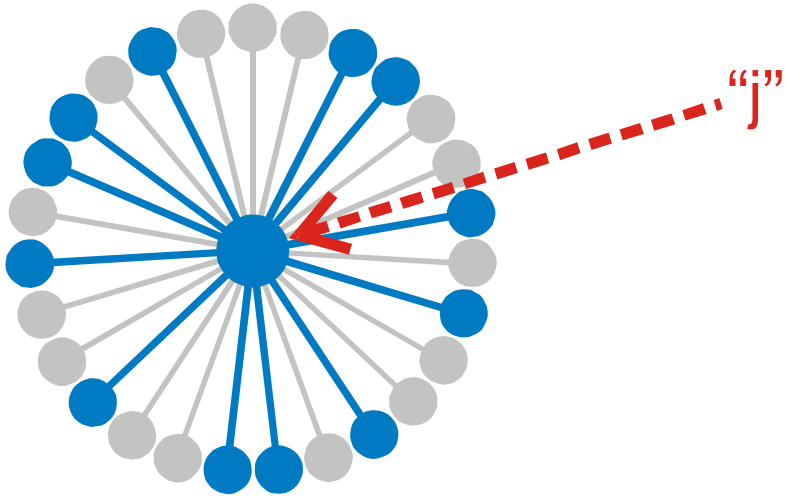


$$n = 9 ; 3n = 27$$

Degree of neutrality of neutral networks and the connectivity threshold

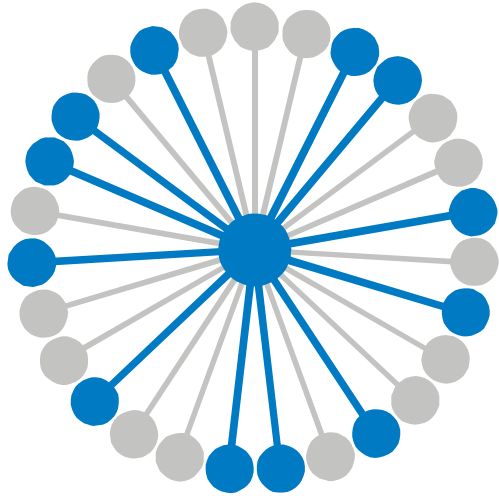


Degree of neutrality of neutral networks and the connectivity threshold



$$\lambda_j = 12 / 27 = 0.444$$

Degree of neutrality of neutral networks and the connectivity threshold

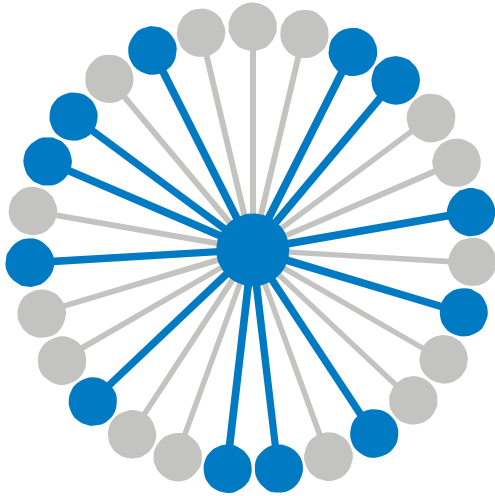


$$\mathbf{G}_k = \psi^{-1}(\mathbf{S}_k) \cup \{ \mathbf{I}_j \mid \psi(\mathbf{I}_j) = \mathbf{S}_k \}$$

$$\bar{\lambda}_k = \frac{\sum_{j \in |\mathbf{G}_k|} \lambda_j(k)}{|\mathbf{G}_k|}$$

$$\lambda_j = 12 / 27 = 0.444$$

Degree of neutrality of neutral networks and the connectivity threshold



$$\mathbf{G}_k = \psi^{-1}(\mathbf{S}_k) \cup \{ \mathbf{I}_j \mid \psi(\mathbf{I}_j) = \mathbf{S}_k \}$$

$$\bar{\lambda}_k = \frac{\sum_{j \in |\mathbf{G}_k|} \lambda_j(k)}{|\mathbf{G}_k|}$$

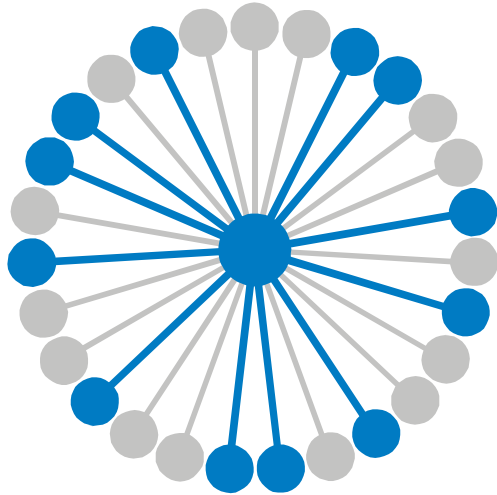
$$\lambda_j = 12 / 27 = 0.444$$

$\bar{\lambda}_k > \lambda_{cr}$ network \mathbf{G}_k is connected

$\bar{\lambda}_k < \lambda_{cr}$ network \mathbf{G}_k is **not** connected

Connectivity threshold: $\lambda_{cr} = 1 - \kappa^{-1/(\kappa-1)}$

Degree of neutrality of neutral networks and the connectivity threshold



$$\lambda_j = 12 / 27 = 0.444$$

$$\mathbf{G}_k = \psi^{-1}(\mathbf{S}_k) \cup \{ \mathbf{I}_j \mid \psi(\mathbf{I}_j) = \mathbf{S}_k \}$$

$$\bar{\lambda}_k = \frac{\sum_{j \in |\mathbf{G}_k|} \lambda_j(k)}{|\mathbf{G}_k|}$$

Alphabet size κ :

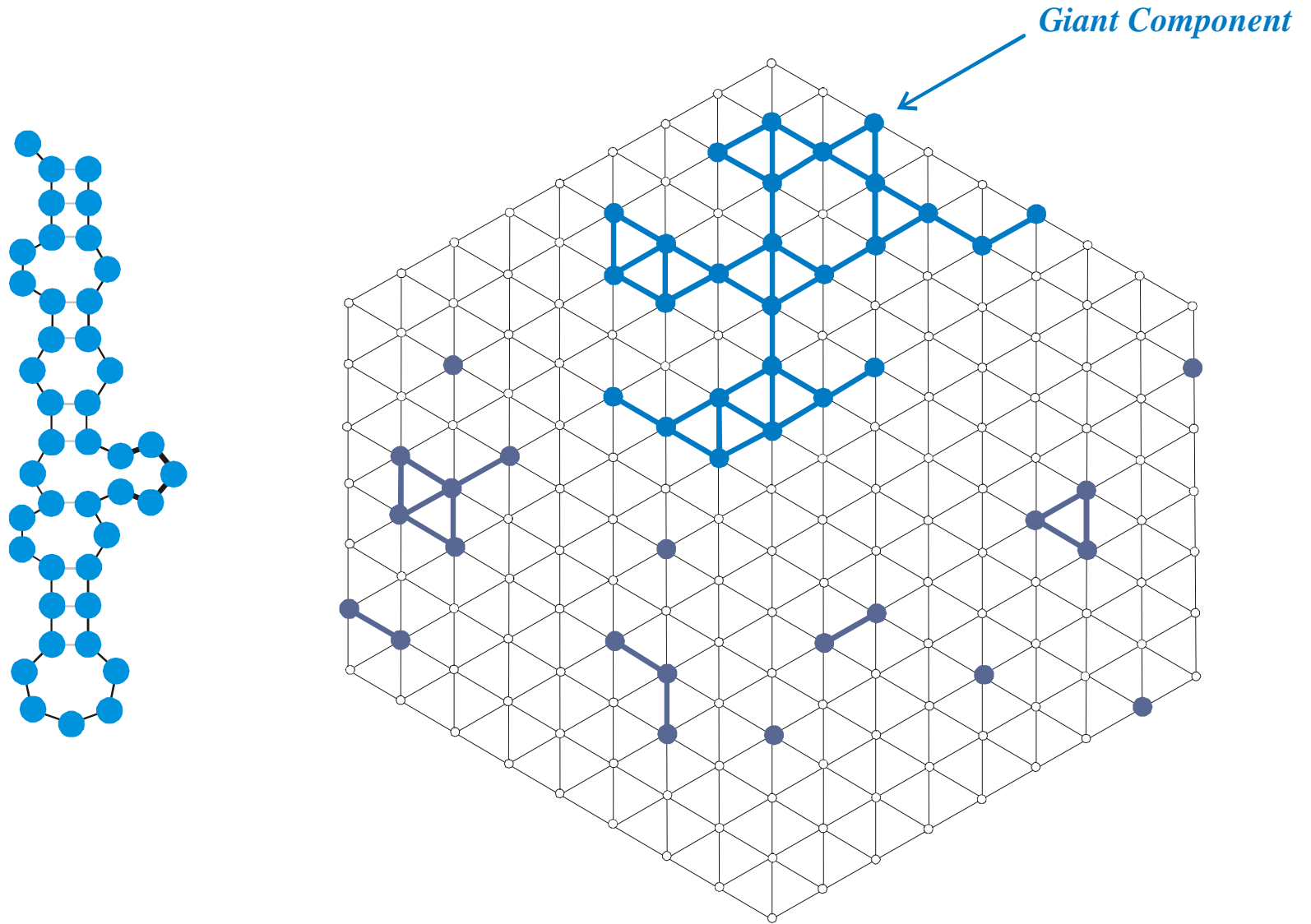
κ	λ_{cr}	
2	0.5	AU,GC,DU
3	0.423	AUG , UGC
4	0.370	AUGC

$\bar{\lambda}_k > \lambda_{cr}$ network \mathbf{G}_k is connected

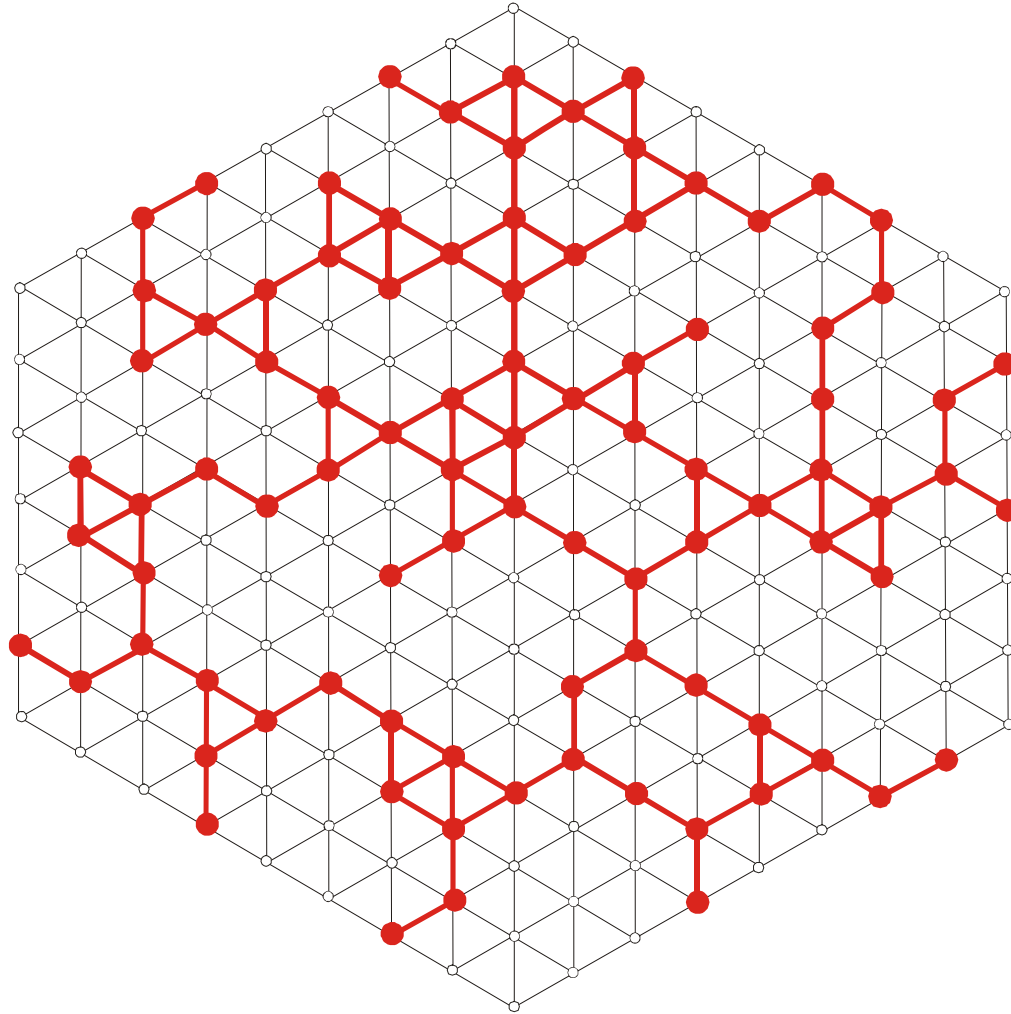
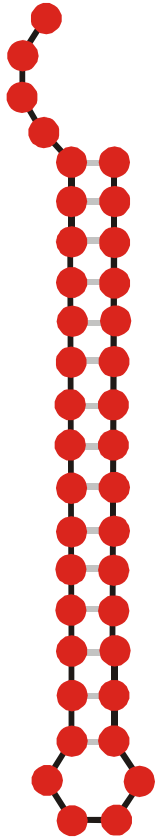
$\bar{\lambda}_k < \lambda_{cr}$ network \mathbf{G}_k is **not** connected

Connectivity threshold: $\lambda_{cr} = 1 - \kappa^{-1/(\kappa-1)}$

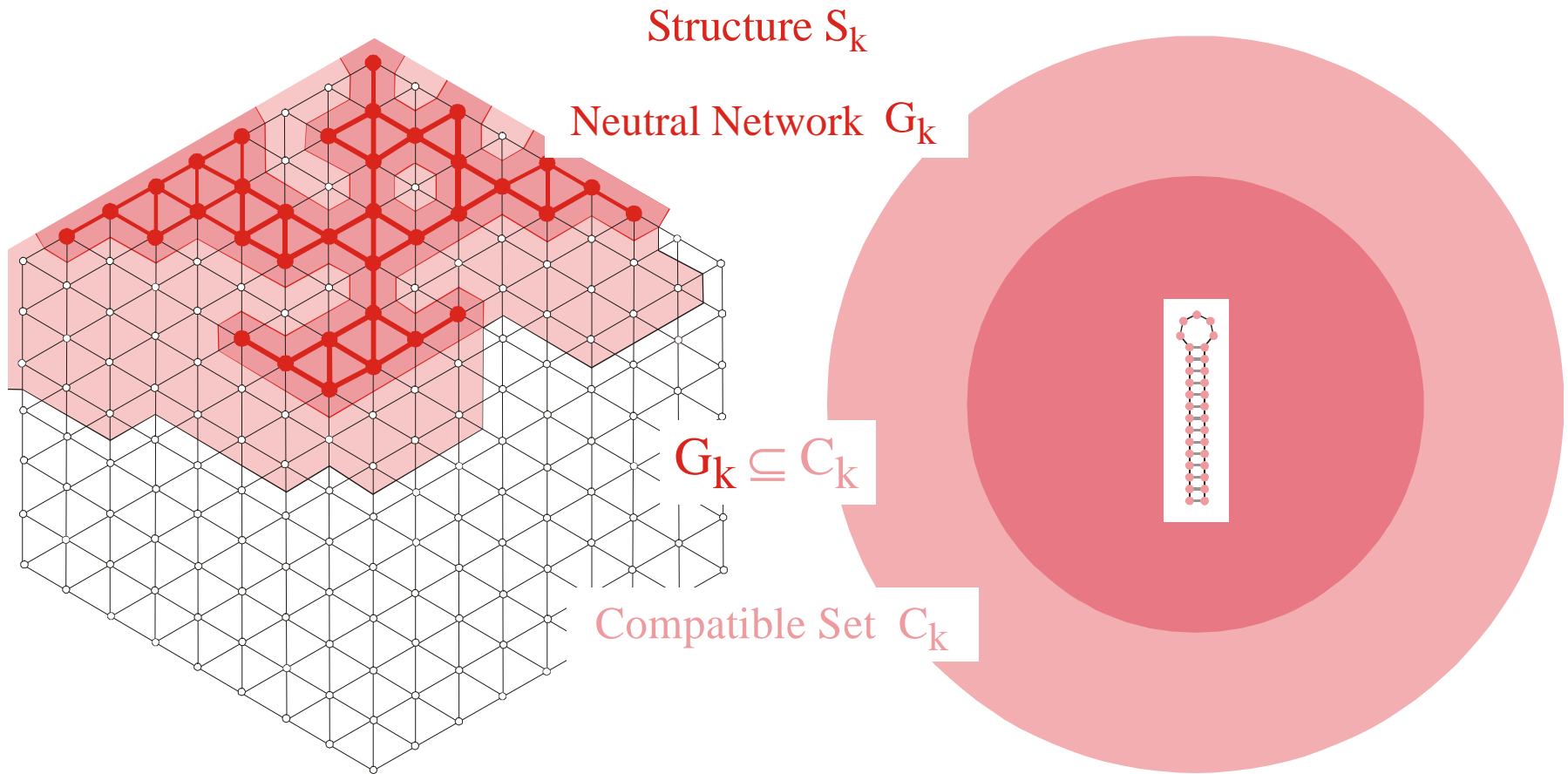
Degree of neutrality of neutral networks and the connectivity threshold



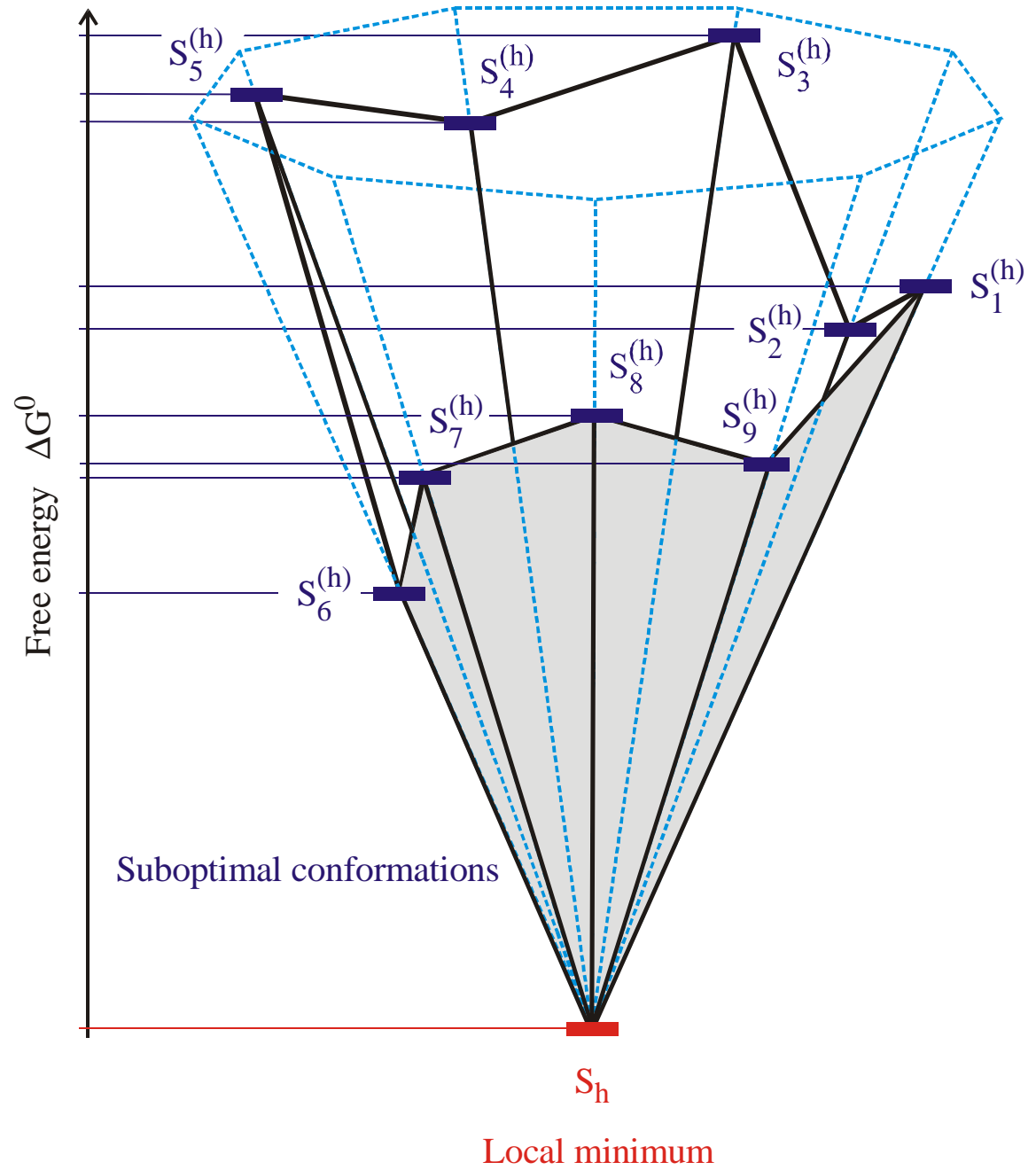
A multi-component neutral network formed by a rare structure



A connected neutral network formed by a common structure

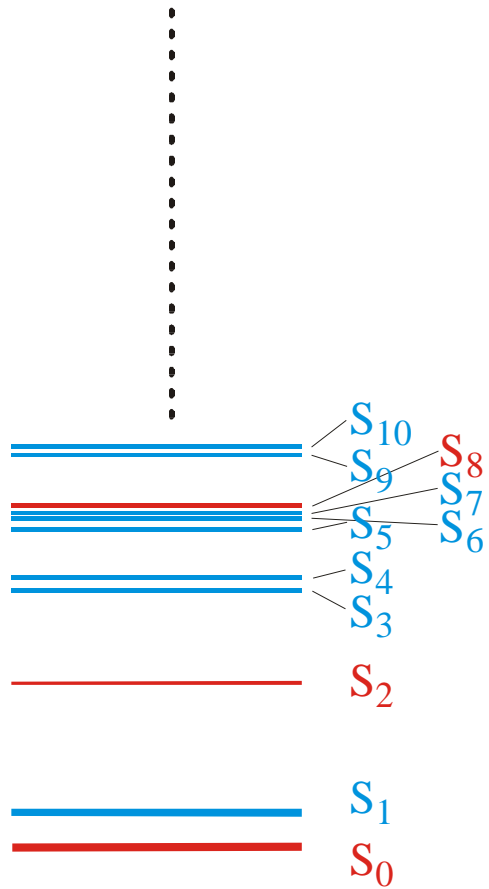


The **compatible set** C_k of a structure S_k consists of all sequences which form S_k as its minimum free energy structure (the **neutral network** G_k) or one of its suboptimal structures.



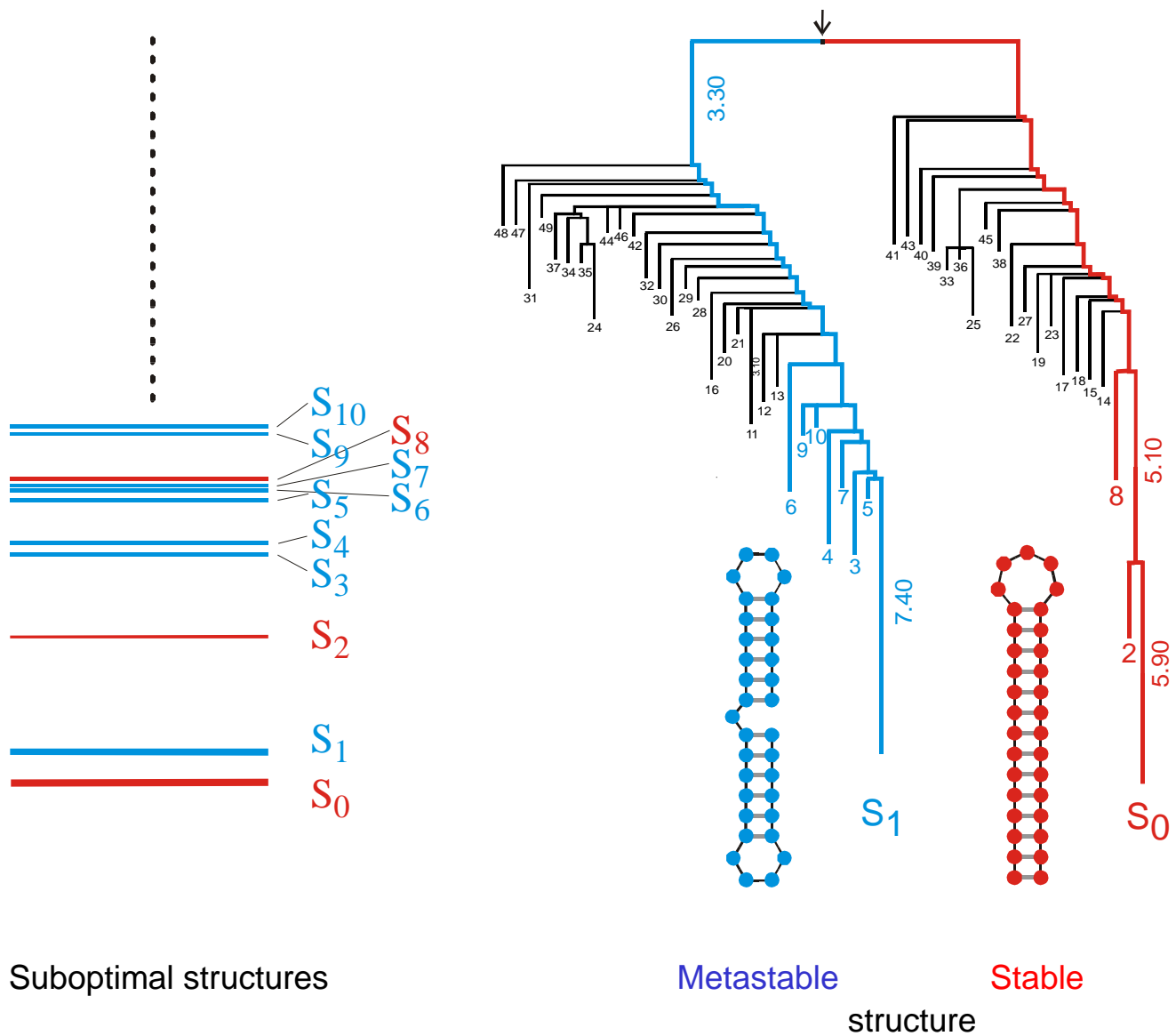
Search for local minima in conformation space

Local minimum

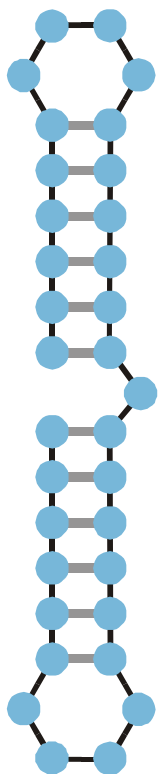


Suboptimal structures

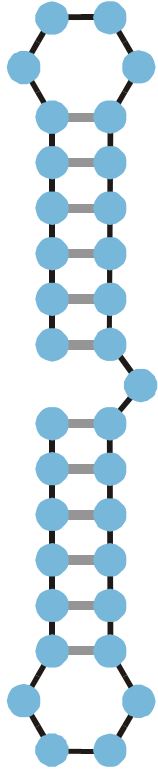
Suboptimal secondary structures of an RNA sequence



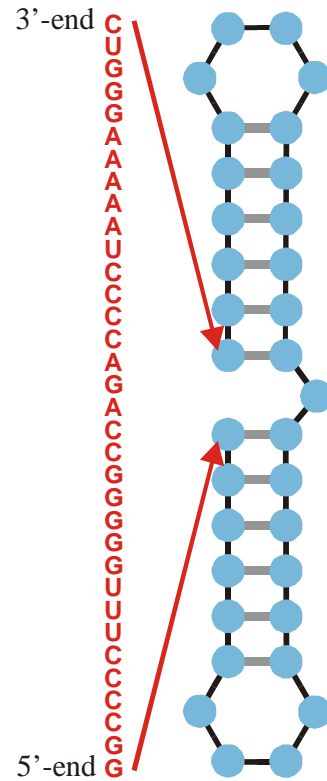
An RNA molecule with two (meta)stable conformations



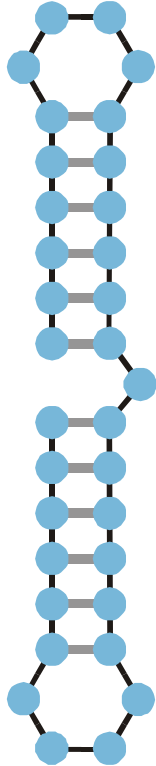
Structure



Structure

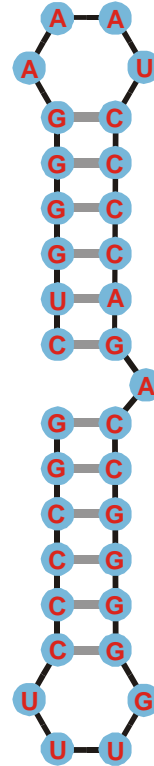


Compatible sequence

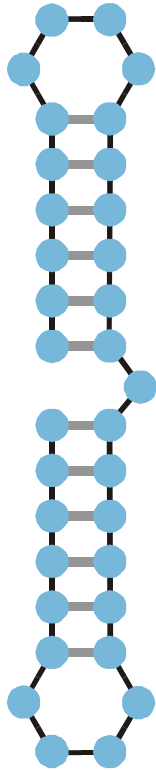


Structure

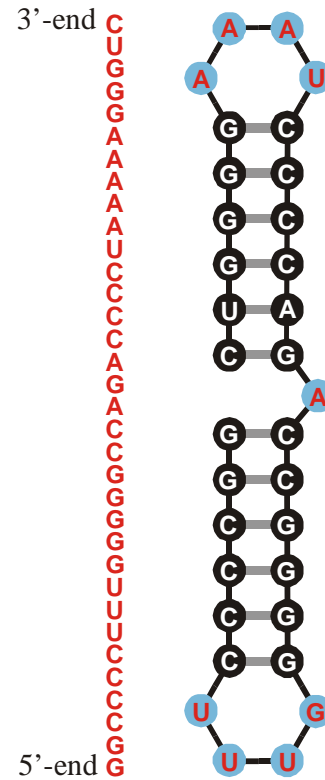
3'-end C
U
G
G
A
A
A
A
A
U
C
C
C
C
A
G
A
C
C
G
G
G
G
G
U
U
U
C
C
C
C
G
5'-end



Compatible sequence



Structure

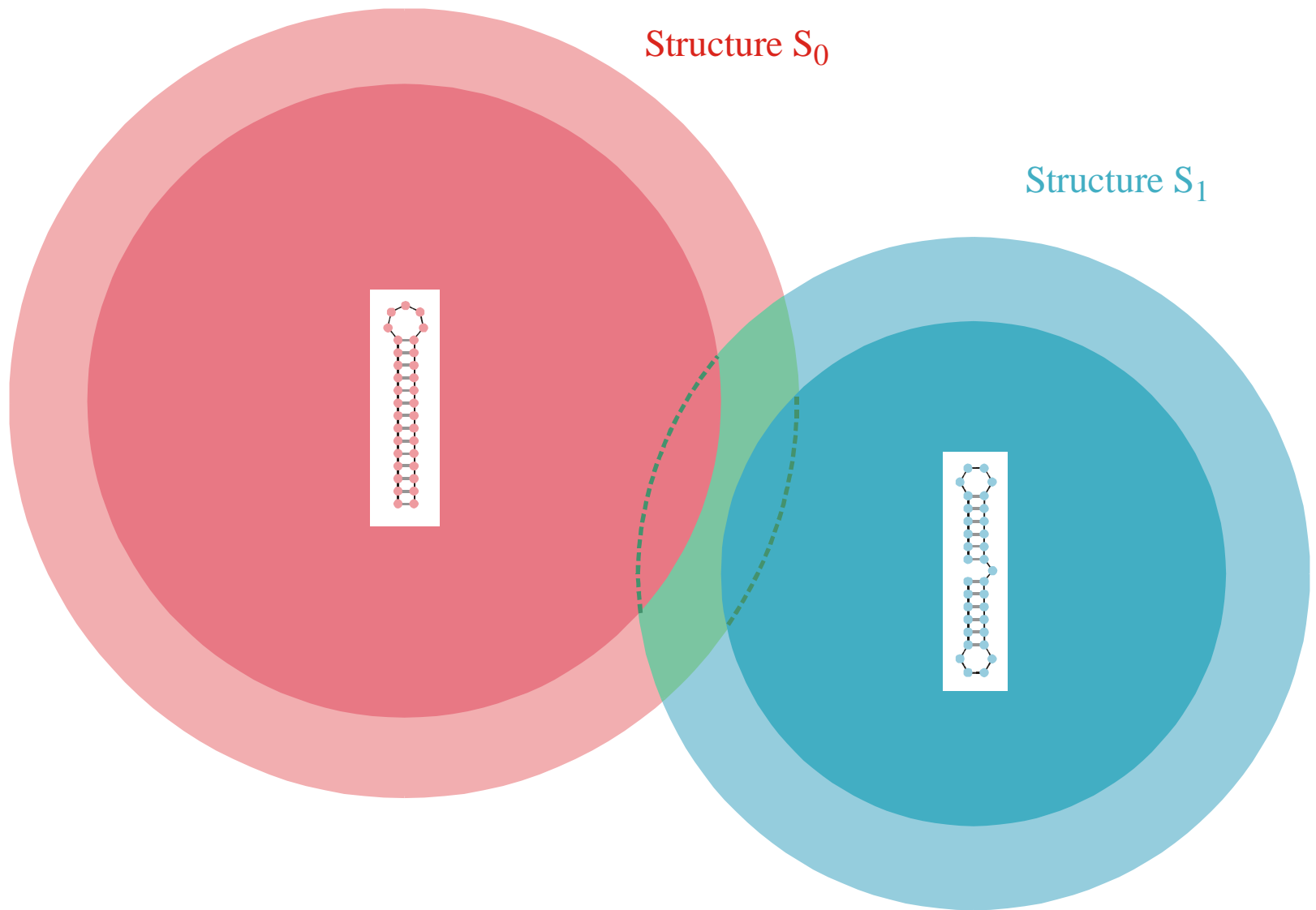


Compatible sequence

Base pairs:

**AU , UA
GC , CG
GU , UG**

Base pairs are varied in strict correlation



Intersection of two compatible sets: $C_0 \cap C_1$

The intersection of two compatible sets is always non empty: $C_0 \cap C_1 \neq \emptyset$



S0092-8240(96)00089-4

GENERIC PROPERTIES OF COMBINATORY MAPS: NEUTRAL NETWORKS OF RNA SECONDARY STRUCTURES¹

■ CHRISTIAN REIDYS*, †, PETER F. STADLER*, ‡
 and PETER SCHUSTER*, ‡, §, ¶²

*Santa Fe Institute,
 Santa Fe, NM 87501, U.S.A.

†Los Alamos National Laboratory,
 Los Alamos, NM 87545, U.S.A.

‡Institut für Theoretische Chemie der Universität Wien,
 A-1090 Wien, Austria

§Institut für Molekulare Biotechnologie,
 D-07708 Jena, Germany

(E-mail: pks@tbi.univie.ac.at)

Random graph theory is used to model and analyse the relationships between sequences and secondary structures of RNA molecules, which are understood as mappings from sequence space into shape space. These maps are non-invertible since there are always many orders of magnitude more sequences than structures. Sequences folding into identical structures form *neutral networks*. A neutral network is embedded in the set of sequences that are *compatible* with the given structure. Networks are modeled as graphs and constructed by random choice of vertices from the space of compatible sequences. The theory characterizes neutral networks by the mean fraction of neutral neighbors (λ). The networks are connected and percolate sequence space if the fraction of neutral nearest neighbors exceeds a threshold value ($\lambda > \lambda^*$). Below threshold ($\lambda < \lambda^*$), the networks are partitioned into a largest “giant” component and several smaller components. Structures are classified as “common” or “rare” according to the sizes of their pre-images, i.e. according to the fractions of sequences folding into them. The neutral networks of any pair of two different common structures almost touch each other, and, as expressed by the conjecture of *shape space covering* sequences folding into almost all common structures, can be found in a small ball of an arbitrary location in sequence space. The results from random graph theory are compared to data obtained by folding large samples of RNA sequences. Differences are explained in terms of specific features of RNA molecular structures. © 1997 Society for Mathematical Biology

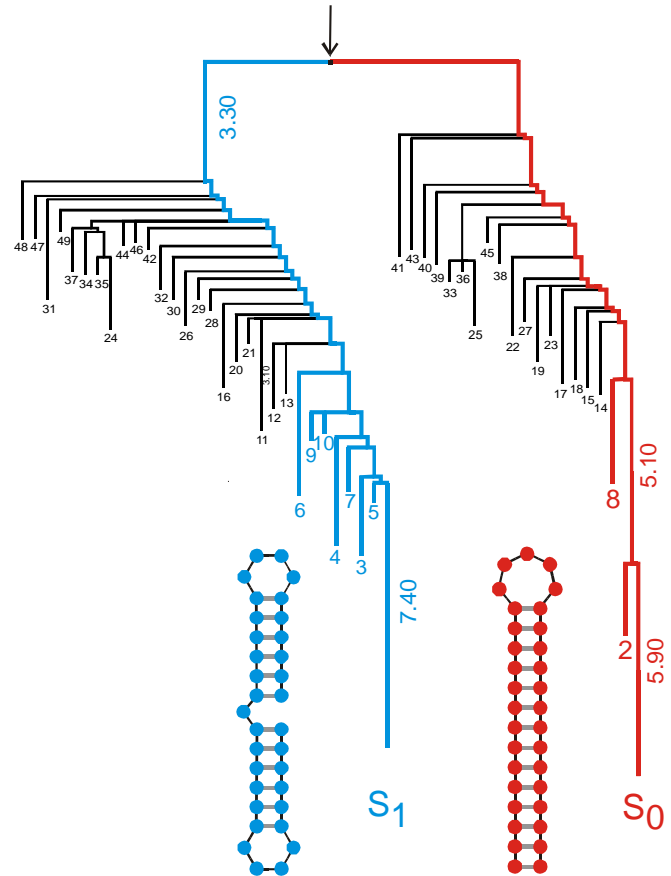
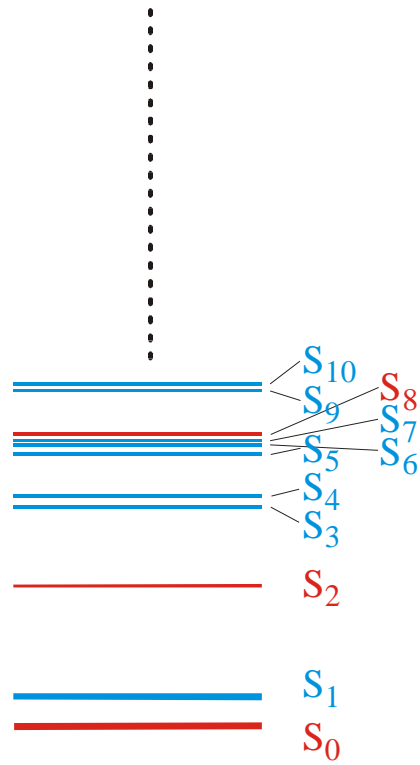
THEOREM 5. INTERSECTION-THEOREM. *Let s and s' be arbitrary secondary structures and $C[s], C[s']$ their corresponding compatible sequences. Then,*

$$C[s] \cap C[s'] \neq \emptyset.$$

Proof. Suppose that the alphabet admits only the complementary base pair $[XY]$ and we ask for a sequence x compatible to both s and s' . Then $f(s, s') \cong D_m$ operates on the set of all positions $\{x_1, \dots, x_n\}$. Since we have the operation of a dihedral group, the orbits are either cycles or chains and the cycles have even order. A constraint for the sequence compatible to both structures appears only in the cycles where the choice of bases is not independent. It remains to be shown that there is a valid choice of bases for each cycle, which is obvious since these have even order. Therefore, it suffices to choose an alternating sequence of the pairing partners X and Y . Thus, there are at least two different choices for the first base in the orbit. ■

Remark. A generalization of the statement of theorem 5 to three different structures is false.

Reference for the definition of the intersection and the proof of the [intersection theorem](#)



A typical energy landscape of a sequence with two (meta)stable conformations

1. RNA and properties and function
2. RNA structures
3. Neutral networks and intersections
- 4. RNA evolution *in silico***
5. Intersection molecules and RNA switches
6. Neutrality in evolution and design

Computer simulation of RNA optimization

Walter Fontana and Peter Schuster,
Biophysical Chemistry 26:123-147, 1987

Walter Fontana, Wolfgang Schnabl, and
Peter Schuster, Phys.Rev.A 40:3301-3321, 1989

PHYSICAL REVIEW A

VOLUME 40, NUMBER 6

SEPTEMBER 15, 1989

Physical aspects of evolutionary optimization and adaptation

Walter Fontana, Wolfgang Schnabl, and Peter Schuster*

Institut für Theoretische Chemie der Universität Wien, Währingerstrasse 17, A-1090 Wien, Austria

(Received 2 February 1989; revised manuscript received 5 May 1989)

A model of an objective function based on polynucleotide folding is used to investigate the dynamics of evolutionary adaptation in finite populations. Binary sequences are optimized with respect to their kinetic properties through a stochastic process involving mutation and selection. The objective function consists in a mapping from the set of all binary strings with given length into a set of two-dimensional structures. These structures then encode the kinetic properties, expressed in terms of parameters of reaction probability distributions. The objective function obtained thereby represents a realistic example of a highly "rugged landscape." Ensembles of molecular strings adapting to this landscape are studied by tracing their escape path from local optima and by applying multivariate analysis. Effects of small population numbers in the tail of the sequence distribution are discussed quantitatively. Close upper bounds to the number of distinct values produced by our objective function are given. The distribution of values is explored by means of simulated annealing and reveals a random scatter in the locations of optima in the space of all sequences. The genetic optimization protocol is applied to the "traveling salesman" problem.

Biophysical Chemistry 26 (1987) 123-147

Elsevier

123

BPC 01133

A computer model of evolutionary optimization

Walter Fontana and Peter Schuster

Institut für theoretische Chemie und Strahlenchemie der Universität Wien, Währingerstraße 17, A-1090 Wien, Austria

Accepted 27 February 1987

Molecular evolution; Optimization; Polyribonucleotide folding; Quasi-species; Selective value; Stochastic reaction kinetics

Molecular evolution is viewed as a typical combinatorial optimization problem. We analyse a chemical reaction model which considers RNA replication including correct copying and point mutations together with hydrolytic degradation and the dilution flux of a flow reactor. The corresponding stochastic reaction network is implemented on a computer in order to investigate some basic features of evolutionary optimization dynamics. Characteristic features of real molecular systems are mimicked by folding binary sequences into unknotted two-dimensional structures. Selective values are derived from these molecular 'phenotypes' by an evaluation procedure which assigns numerical values to different elements of the secondary structure. The fitness function obtained thereby contains nontrivial long-range interactions which are typical for real systems. The fitness landscape also reveals quite involved and bizarre local topologies which we consider also representative of polynucleotide replication in actually occurring systems. Optimization operates on an ensemble of sequences via mutation and natural selection. The strategy observed in the simulation experiments is fairly general and resembles closely a heuristic widely applied in operations research areas. Despite the relative smallness of the system - we study 2000 molecules of chain length $r = 70$ in a typical simulation experiment - features typical for the evolution of real populations are observed as there are error thresholds for replication, evolutionary steps and quasistationary sequence distributions. The relative importance of selectively neutral or almost neutral variants is discussed quantitatively. Four characteristic ensemble properties, entropy of the distribution, ensemble correlation, mean Hamming distance and diversity of the population, are computed and checked for their sensitivity in recording major optimization events during the simulation.

1. Molecular evolution and optimization

Conventional population genetics treats mutation as an external stochastic source. Moreover, mutations are considered as very rare events. In the absence of genetic recombination populations of haploid organisms are expected to be usually homogeneous. Experimental evidence on viral and bacterial populations is available now and it contradicts these expectations. Mutations appear much more frequently than was originally assumed.

Dedicated to Professor Manfred Eigen on the occasion of his 60th birthday.

Correspondence address: P. Schuster, Institut für theoretische Chemie und Strahlenchemie der Universität Wien, Währingerstraße 17, A-1090 Wien, Austria.

The molecular approach considers error-free replication and mutation as parallel reactions within the same mechanism. Detailed information on the molecular mechanisms of polynucleotide replication provides direct insight into the nature of mutations and their role in evolution. Several classes of mutations are properly distinguished: point mutations, deletions and insertions. Point mutations are of special importance: they represent the most frequent mutations and are easily incorporated into theoretical models of molecular evolution. This does not mean, however, that the other classes of mutations are not important in evolution. To give an example: there is a general belief that insertions leading to gene duplication played a major role in the development of present day enzyme families.

The first theoretical model of molecular evolu-

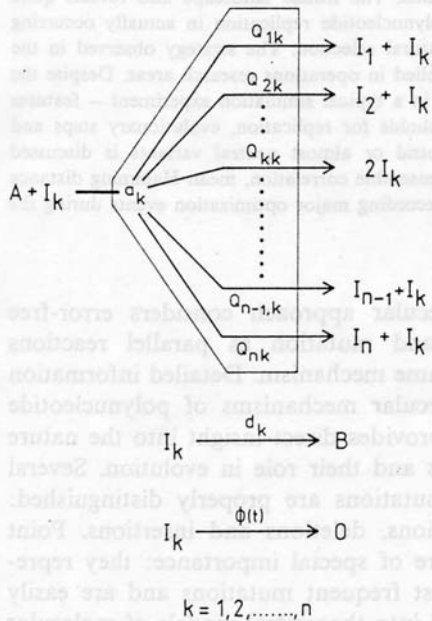
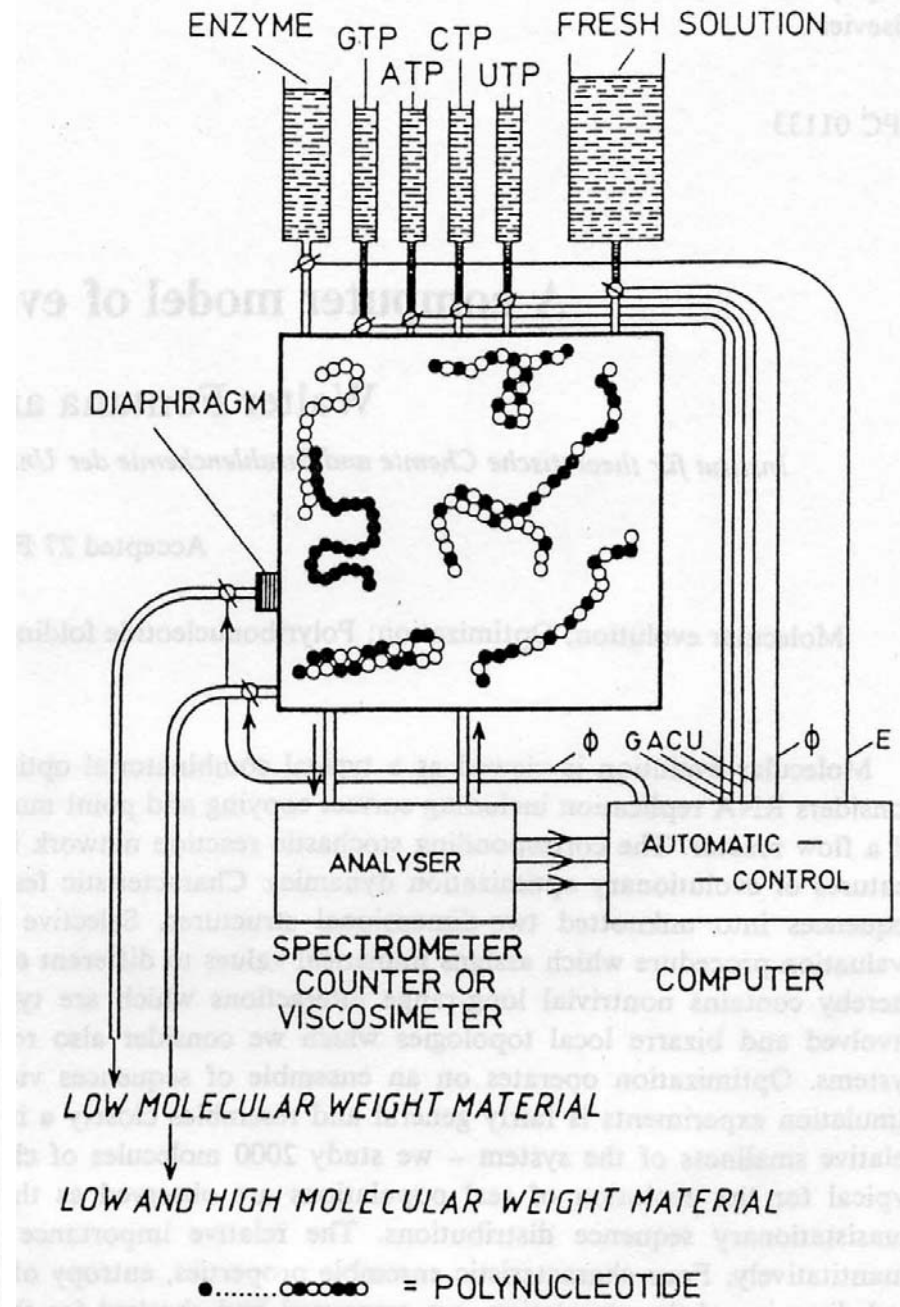
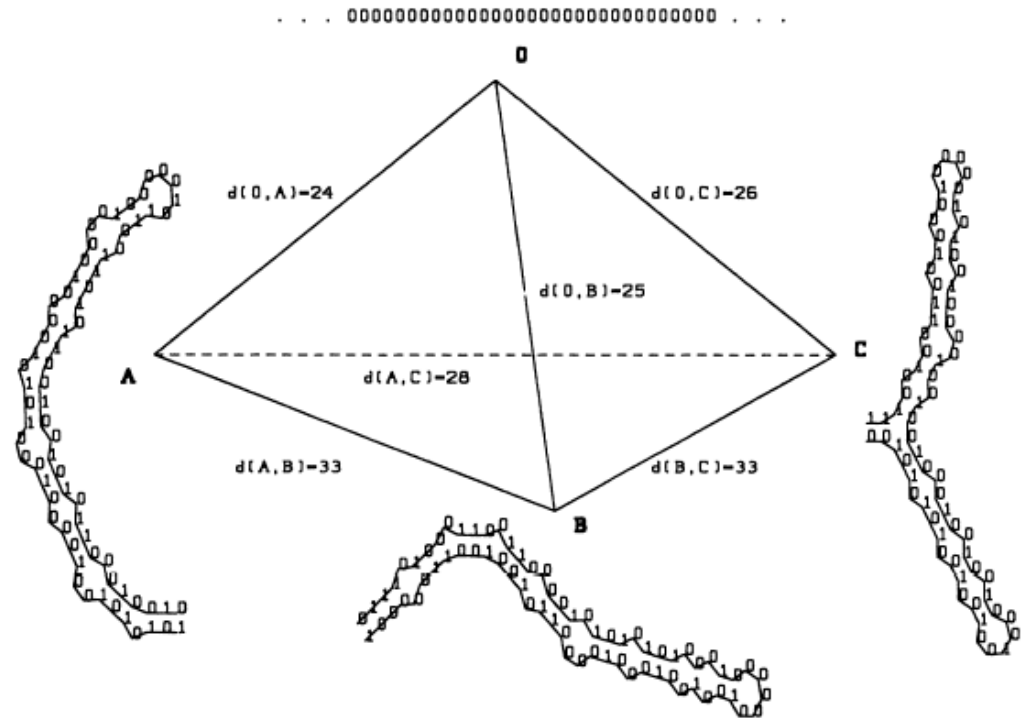
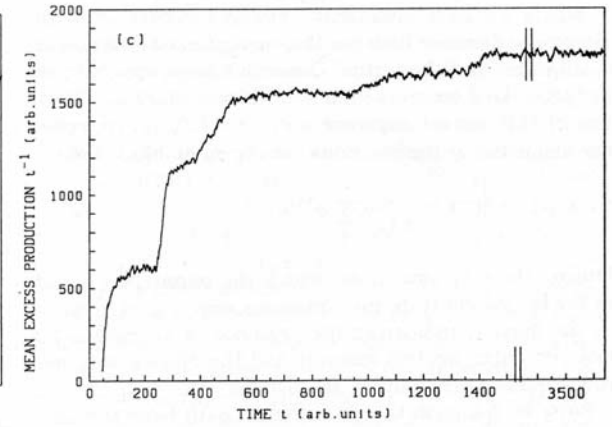
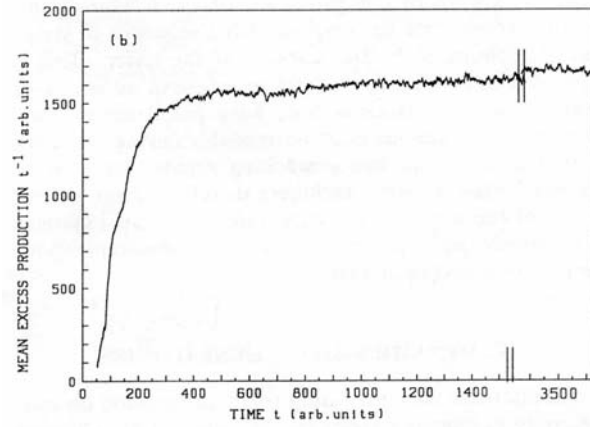
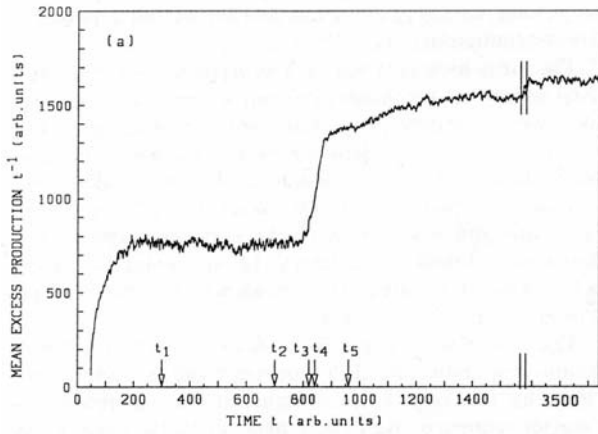


Fig. 1. The reaction network. Synthesis on template I_k proceeds with the rate constant a_k and leads with frequency Q_{ik} to a new template I_i , preserving the old copy. Materials A needed for polymerization are assumed to be buffered. Degradation to waste products B occurs with rate d_k and a controlled unspecific flux $\Phi(t)$ removes templates from the system.

Fig. 2. The evolution reactor. This kind of flow reactor consists of a reaction vessel which allows for temperature and pressure control. Its walls are impermeable to polynucleotides. Energy-rich material is poured from the environment into the reactor. The degradation products are removed steadily. Material transport is adjusted in such a way that the concentration of monomers is constant in the reactor. A dilution flux Φ is installed in order to remove excess of polynucleotides produced by replication. Thus, the sum of the numbers of individual particles $\sum_i X_i(t) = N(t)$ may be controlled by the flux Φ . Under 'constant organization' Φ is adjusted such that $N(t) = \Theta$ is essentially constant. By this we indicate that fluctuations with standard deviation $\sigma = \sqrt{N}$ occur regularly. The regulation of Φ requires internal control, which can be achieved by logistic coupling.



●.....●●●●●● = POLYNUCLEOTIDE



Walter Fontana, Wolfgang Schnabl, and Peter Schuster, Phys.Rev.A 40:3301-3321, 1989

random individuals. The primer pair used for genomic DNA amplification is 5'-TCTCCCTGGATTCT-CATTTA-3' (forward) and 5'-TCTTTGTCTTCTGT-TGCACC-3' (reverse). Reactions were performed in 25 μ l using 1 unit of Taq DNA polymerase with each primer at 0.4 μ M, 200 μ M each dATP, dTTP, dCTP, and dGTP, and PCR buffer [10 mM Tris-HCl (pH 8.3), 50 mM KCl, 1.5 mM MgCl₂] in a cycle condition of 94°C for 1 min and then 35 cycles of 94°C for 30 s, 55°C for 30 s, and 72°C for 30 s followed by 72°C for 6 min. PCR products were purified (Qiagen), digested with Xmn I, and separated in a 2% agarose gel.

32. A nonsense mutation may affect mRNA stability and result in degradation of the transcript [L. Maquat, *Am. J. Hum. Genet.* **59**, 279 (1996)].

33. Data not shown; a dot blot with poly (A)⁺ RNA from 50 human tissues (The Human RNA Master Blot, 7770-1, Clontech Laboratories) was hybridized with a probe from exons 29 to 47 of *MYO15* using the same condition as Northern blot analysis (13).

34. Smith-Magenis syndrome (SMS) is due to deletions of 17p11.2 of various sizes, the smallest of which includes *MYO15* and perhaps 20 other genes [6]; K-S Chen, L. Potocki, J. R. Lupski, *MROD Res. Rev.* **2**, 122 (1996)]. *MYO15* expression is easily detected in the pituitary gland (data not shown). Haploinsufficiency for *MYO15* may explain a portion of the SMS

phenotype such as short stature. Moreover, a few SMS patients have sensorineural hearing loss, possibly because of a point mutation in *MYO15* in trans to the SMS 17p11.2 deletion.

35. R. A. Fiedel, data not shown.

36. K. B. Avraham *et al.*, *Nature Genet.* **11**, 369 (1995); X-Z. Liu *et al.*, *ibid.* **17**, 268 (1997); F. Gibson *et al.*, *Nature* **374**, 62 (1995); D. Weil *et al.*, *ibid.*, p. 60.

37. RNA was extracted from cochlea (membranous labyrinth) obtained from human fetuses at 18 to 22 weeks of development in accordance with guidelines established by the Human Research Committee at the Brigham and Women's Hospital. Only samples without evidence of degradation were pooled for poly (A)⁺ selection over oligo(dT) columns. First-strand cDNA was prepared using an Advantage RT-for-PCR kit (Clontech Laboratories). A portion of the first-strand cDNA (4%) was amplified by PCR with Advantage cDNA polymerase mix (Clontech Laboratories) using human *MYO15*-specific oligonucleotide primers (forward, 5'-GCATGACCTGCGGGTAAT-GCG-3'; reverse, 5'-CTCAAGGCTTCTGGCATGGT-GCTCGCTGCG-3'). Cycling conditions were 40 s at 94°C, 40 s at 66°C (3 cycles), 60°C (5 cycles), and 55°C (29 cycles); and 45 s at 68°C. PCR products were visualized by ethidium bromide staining after fractionation in a 1% agarose gel. A 688-bp PCR

product is expected from amplification of the human *MYO15* cDNA. Amplification of human genomic DNA with this primer pair would result in a 2903-bp fragment.

38. We are grateful to the people of Bengkala, Bali, and the two families from India. We thank J. R. Lupski and K.-S. Chen for providing the human chromosome 17 cosmid library. For technical and computational assistance, we thank N. Dietrich, M. Ferguson, A. Gupta, E. Sorbello, R. Torkzadeh, C. Varner, M. Walker, G. Bouffard, and S. Beckstrom-Stenberg (National Institutes of Health Intramural Sequencing Center). We thank J. T. Hinnant, I. N. Arhya, and S. Winata for assistance in Bali, and T. Barber, S. Sullivan, E. Green, D. Drayna, and J. Battey for helpful comments on this manuscript. Supported by the National Institute on Deafness and Other Communication Disorders (NIDCD) (Z01 DC 00335-01 and Z01 DC 00338-01 to T.B.F. and E.R.W. and R01 DC 03402 to C.G.M.), the National Institute of Child Health and Human Development (R01 HD30428 to S.A.C.) and a National Science Foundation Graduate Research Fellowship to F.J.P. This paper is dedicated to J. B. Snow Jr. on his retirement as the Director of the NIDCD.

9 March 1998; accepted 17 April 1998

Continuity in Evolution: On the Nature of Transitions

Walter Fontana and Peter Schuster

To distinguish continuous from discontinuous evolutionary change, a relation of nearness between phenotypes is needed. Such a relation is based on the probability of one phenotype being accessible from another through changes in the genotype. This nearness relation is exemplified by calculating the shape neighborhood of a transfer RNA secondary structure and provides a characterization of discontinuous shape transformations in RNA. The simulation of replicating and mutating RNA populations under selection shows that sudden adaptive progress coincides mostly, but not always, with discontinuous shape transformations. The nature of these transformations illuminates the key role of neutral genetic drift in their realization.

A much-debated issue in evolutionary biology concerns the extent to which the history of life has proceeded gradually or has been punctuated by discontinuous transitions at the level of phenotypes (1). Our goal is to make the notion of a discontinuous transition more precise and to understand how it arises in a model of evolutionary adaptation.

We focus on the narrow domain of RNA secondary structure, which is currently the simplest computationally tractable, yet realistic phenotype (2). This choice enables the definition and exploration of concepts that may prove useful in a wider context. RNA secondary structures represent a coarse level of analysis compared with the three-dimensional structure at atomic resolution. Yet, secondary structures are empir-

ically well defined and obtain their biophysical and biochemical importance from being a scaffold for the tertiary structure. For the sake of brevity, we shall refer to secondary structures as "shapes." RNA combines in a single molecule both genotype (replicable sequence) and phenotype (selectable shape), making it ideally suited for in vitro evolution experiments (3, 4).

To generate evolutionary histories, we used a stochastic continuous time model of an RNA population replicating and mutating in a capacity-constrained flow reactor under selection (5, 6). In the laboratory, a goal might be to find an RNA aptamer binding specifically to a molecule (4). Although in the experiment the evolutionary end product was unknown, we thought of its shape as being specified implicitly by the imposed selection criterion. Because our intent is to study evolutionary histories rather than end products, we defined a target shape in advance and assumed the replication rate of a sequence to be a function of

the similarity between its shape and the target. An actual situation may involve more than one best shape, but this does not affect our conclusions.

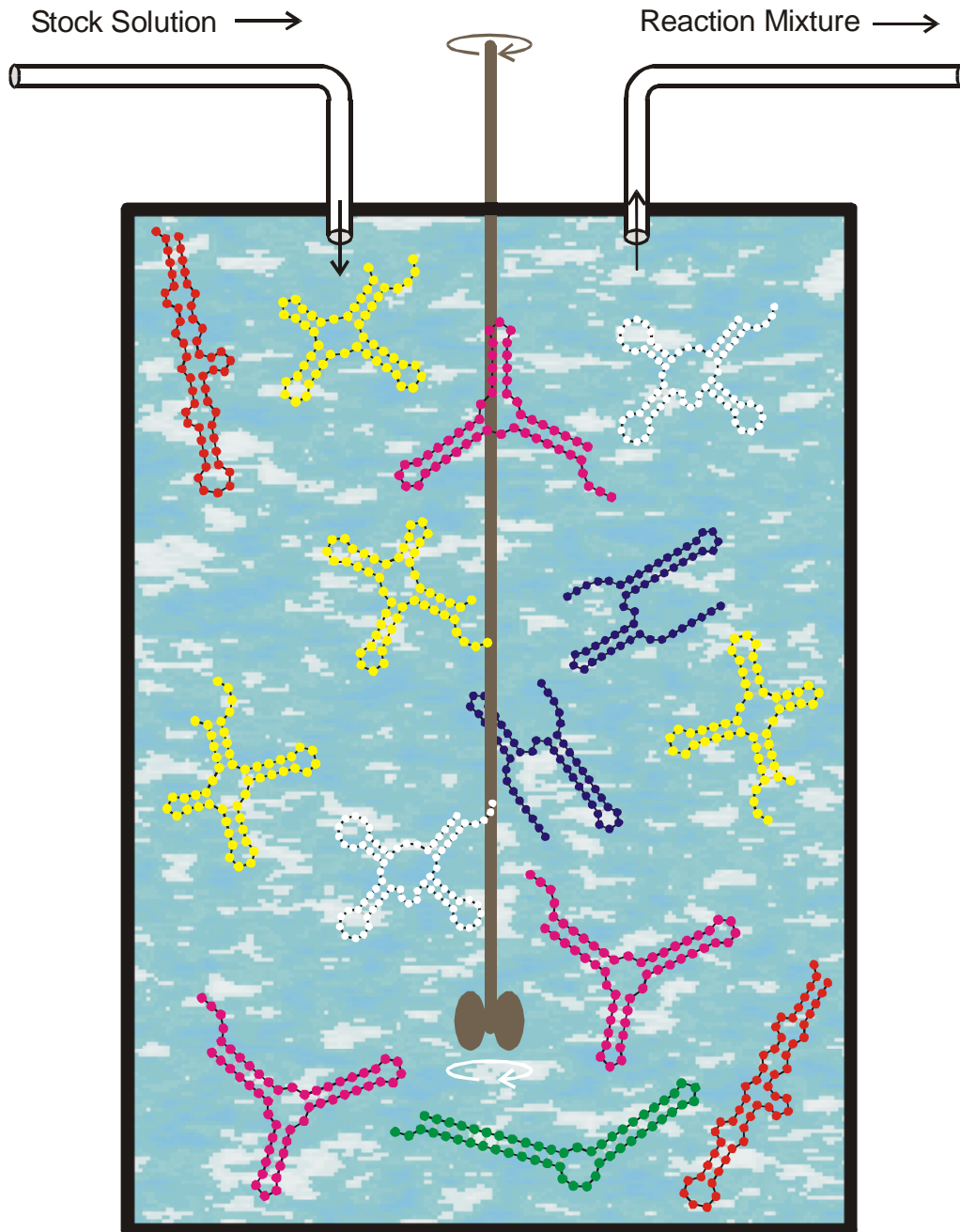
An instance representing in its qualitative features all the simulations we performed is shown in Fig. 1A. Starting with identical sequences folding into a random shape, the simulation was stopped when the population became dominated by the target, here a canonical tRNA shape. The black curve traces the average distance to the target (inversely related to fitness) in the population against time. Aside from a short initial phase, the entire history is dominated by steps, that is, flat periods of no apparent adaptive progress, interrupted by sudden approaches toward the target structure (7). However, the dominant shapes in the population not only change at these marked events but undergo several fitness-neutral transformations during the periods of no apparent progress. Although discontinuities in the fitness trace are evident, it is entirely unclear when and on the basis of what the series of successive phenotypes itself can be called continuous or discontinuous.

A set of entities is organized into a (topological) space by assigning to each entity a system of neighborhoods. In the present case, there are two kinds of entities: sequences and shapes, which are related by a thermodynamic folding procedure. The set of possible sequences (of fixed length) is naturally organized into a space because point mutations induce a canonical neighborhood. The neighborhood of a sequence consists of all its one-error mutants. The problem is how to organize the set of possible shapes into a space. The issue arises because, in contrast to sequences, there are

Evolution *in silico*

W. Fontana, P. Schuster,
Science **280** (1998), 1451-1455

Institut für Theoretische Chemie, Universität Wien, Währingerstrasse 17, A-1090 Wien, Austria, Santa Fe Institute, 1399 Hyde Park Road, Santa Fe, NM 87501, USA, and International Institute for Applied Systems Analysis (IIASA), A-2361 Laxenburg, Austria.



Replication rate constant:

$$f_k = \gamma / [\alpha + \Delta d_S^{(k)}]$$

$$\Delta d_S^{(k)} = d_H(S_k, S_\tau)$$

Selection constraint:

Population size, $N = \#$ RNA molecules, is controlled by the flow

$$N(t) \approx \bar{N} \pm \sqrt{\bar{N}}$$

Mutation rate:

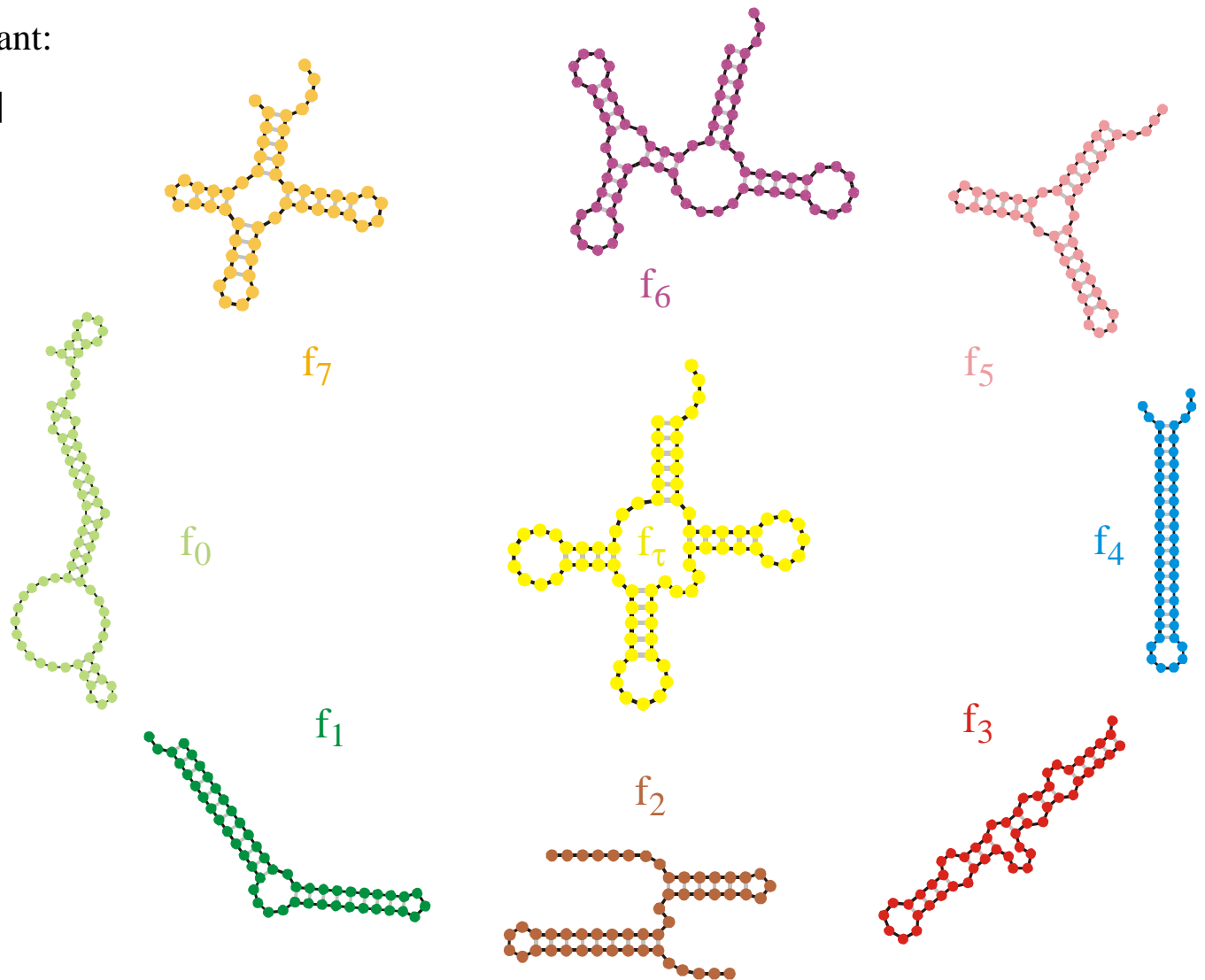
$$p = 0.001 / \text{site} \times \text{replication}$$

The flowreactor as a device for **studies** of evolution *in vitro* and *in silico*

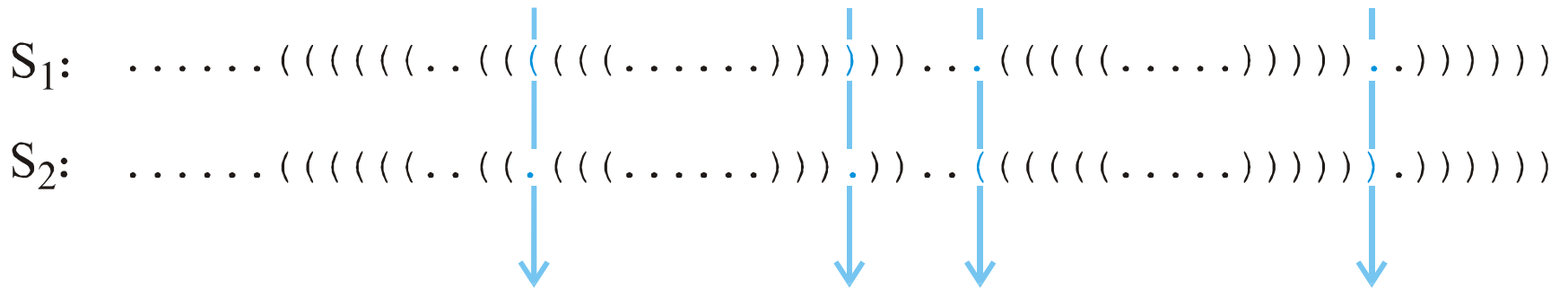
Replication rate constant:

$$f_k = \gamma / [\alpha + \Delta d_S^{(k)}]$$

$$\Delta d_S^{(k)} = d_H(S_k, S_\tau)$$



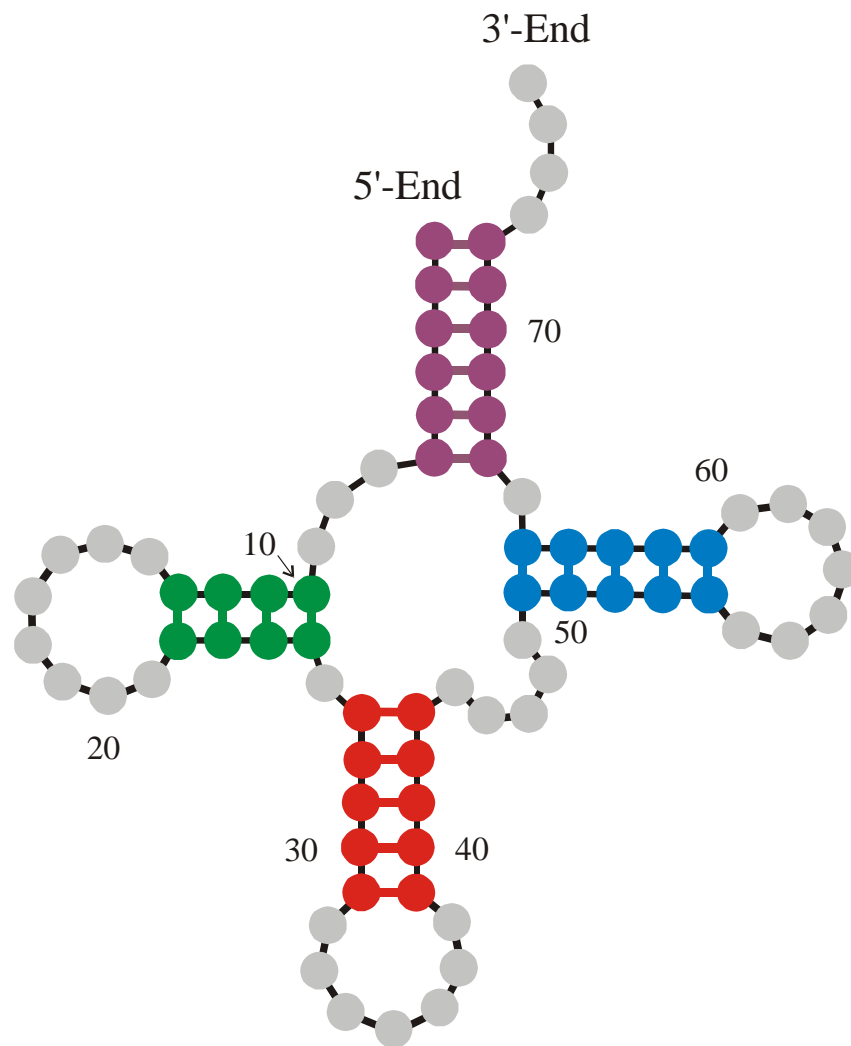
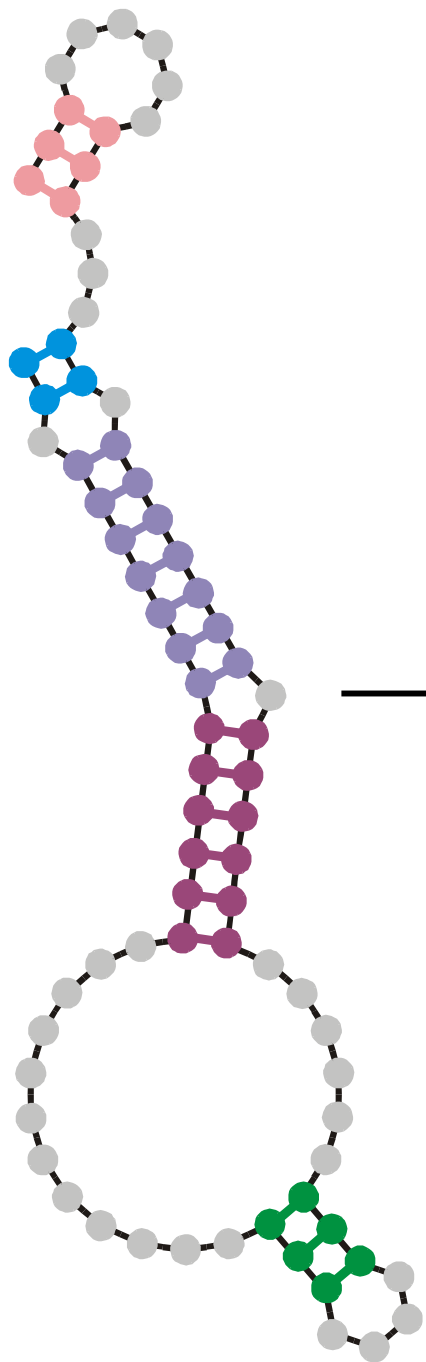
Evaluation of RNA secondary structures yields replication rate constants



Hamming distance $d_H(S_1, S_2) = 4$

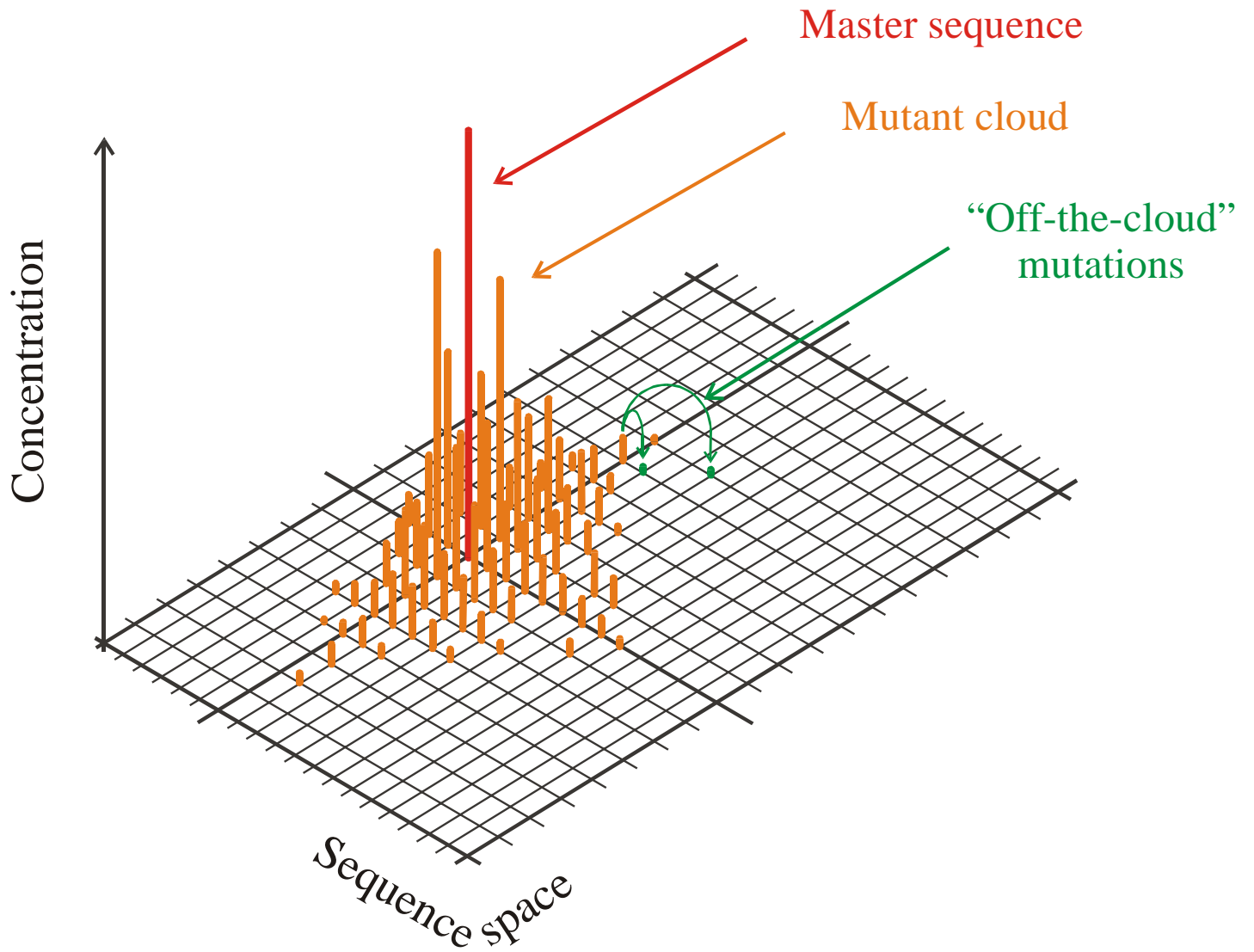
- (i) $d_H(S_1, S_1) = 0$
- (ii) $d_H(S_1, S_2) = d_H(S_2, S_1)$
- (iii) $d_H(S_1, S_3) \leq d_H(S_1, S_2) + d_H(S_2, S_3)$

The Hamming distance between structures in parentheses notation forms a metric in structure space

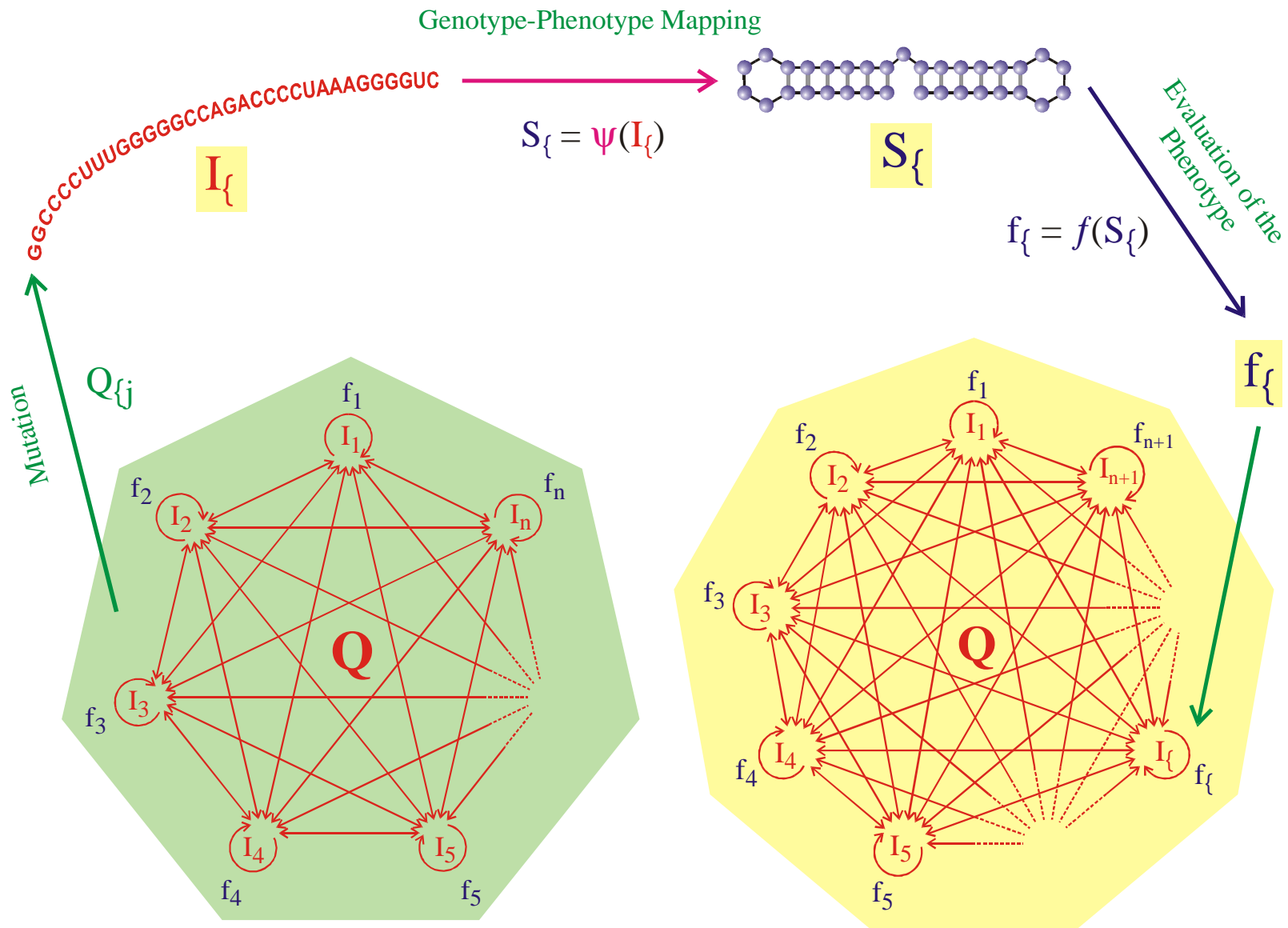


Randomly chosen
initial structure

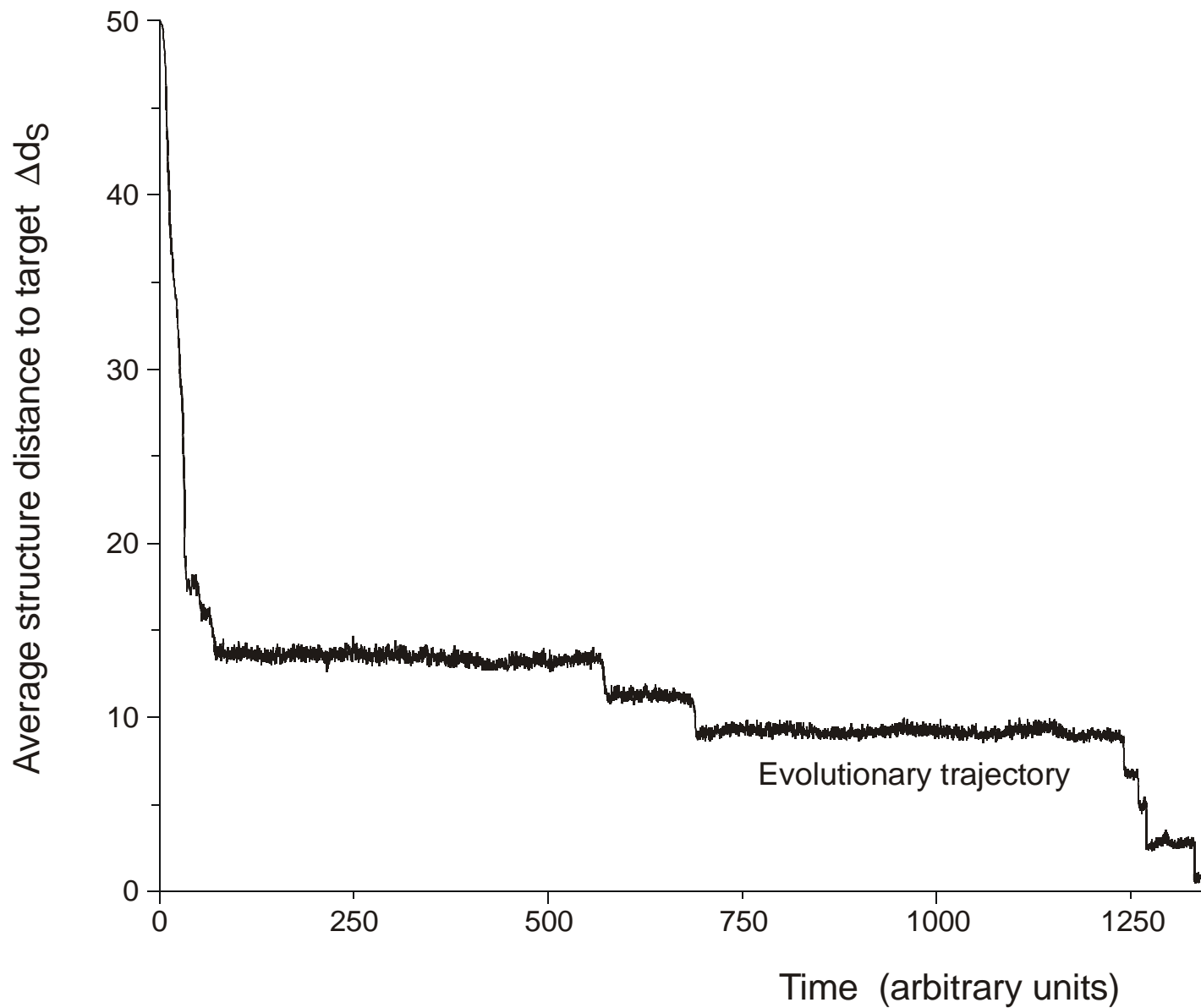
Phenylalanyl-tRNA as
target structure



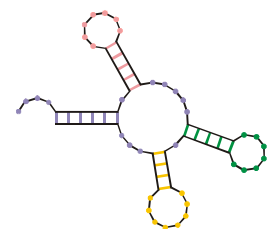
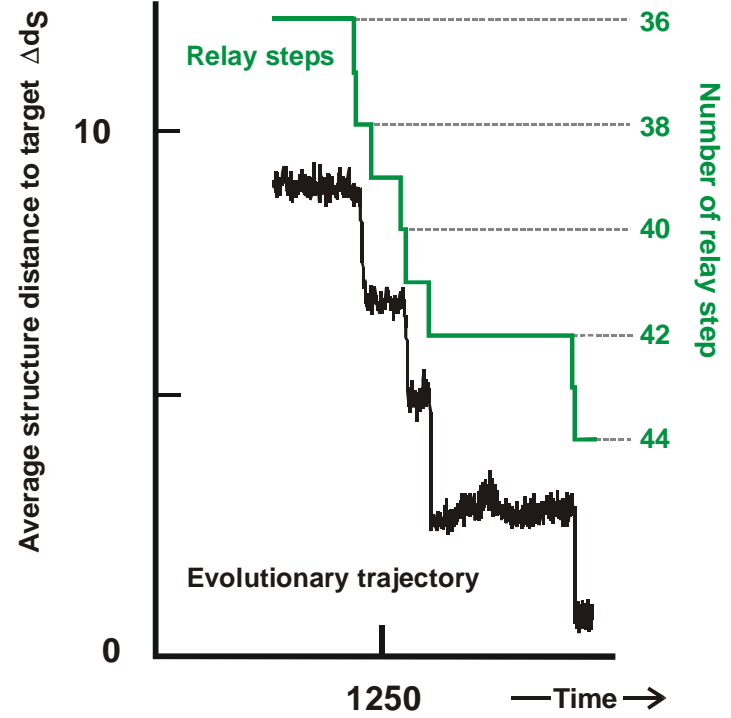
The molecular quasispecies
in sequence space



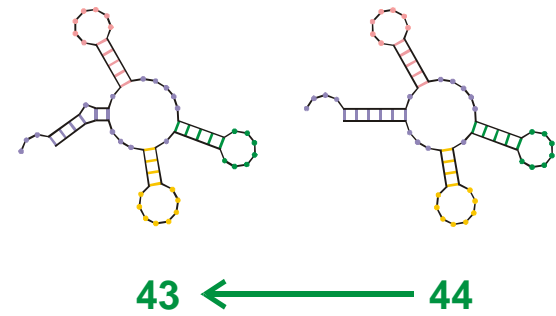
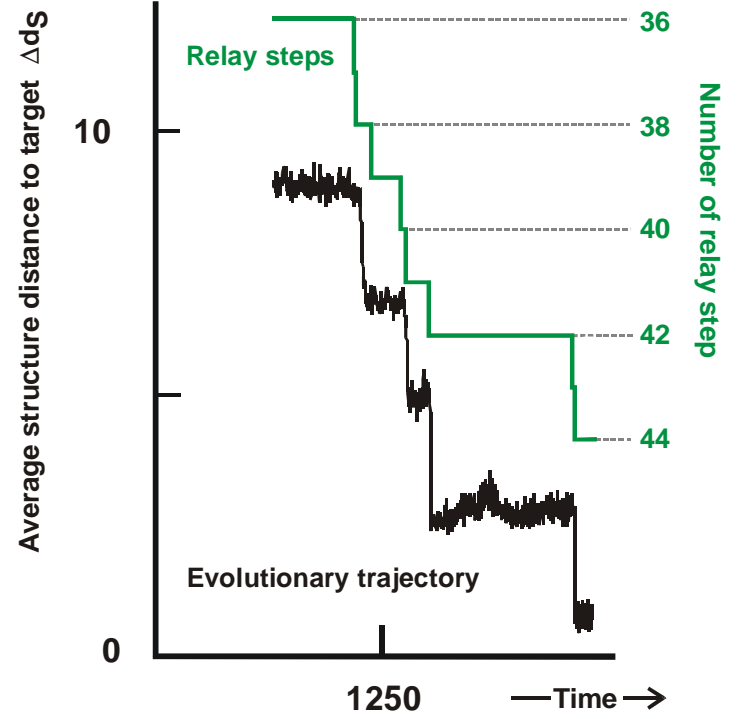
Evolutionary dynamics
including molecular phenotypes



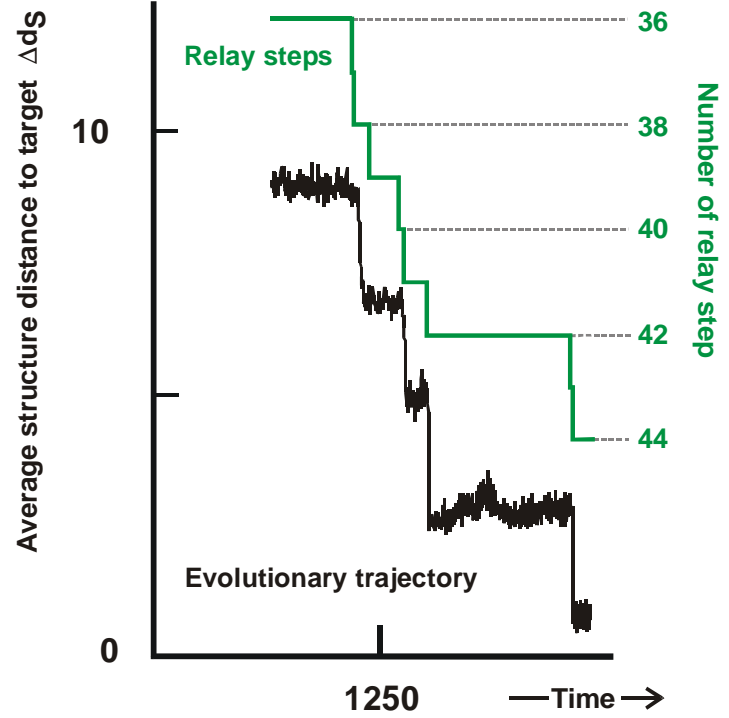
In silico optimization in the flow reactor: Evolutionary trajectory



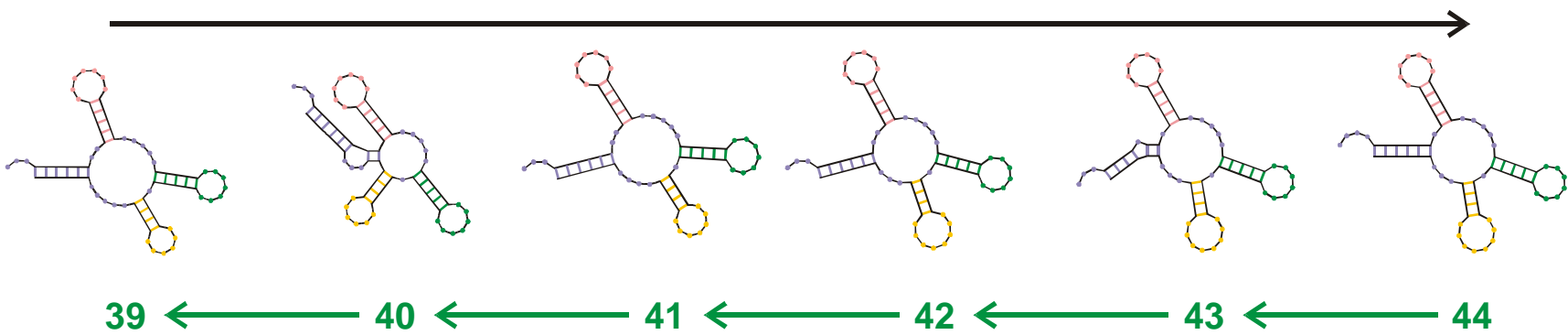
Final conformation of optimization



Reconstruction of the last step 43 \rightarrow 44



Evolutionary process



Reconstruction

Reconstruction of the relay series

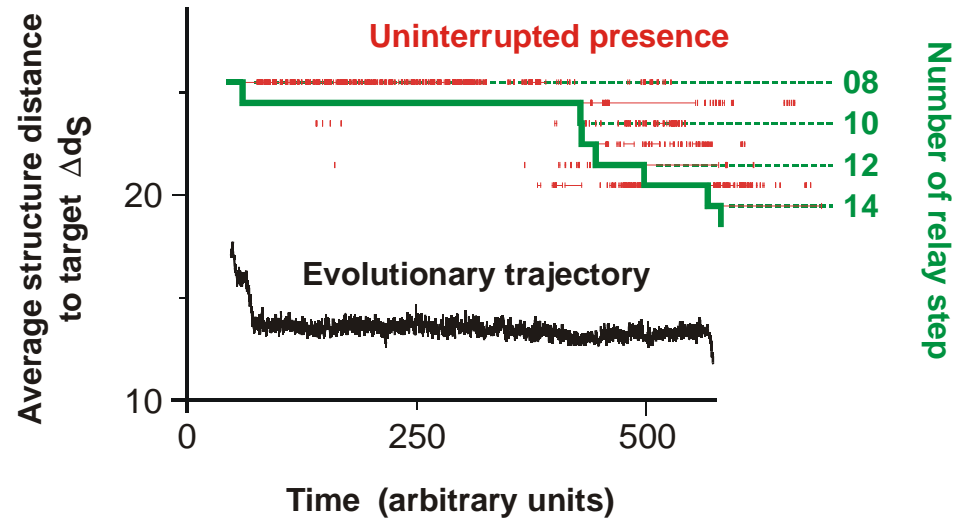
entry 39 GGGAUACAUGUGGCCCCUCAAGGCC**C**UAGCGAAACUGCUGCUGAAACCGUGUGAAUAAUCCGCACCCUGUCCCGA
 ((((((.....(((.....))))).(((.....))))).(((.....))))).(((.....))))).(((.....))))).
 exit GGGAUAUAC**G**AGGCCCGUCAAGGCC**G**UAGCGAA**C**CGACUGUUGAAACUGUG**C**GAAUAAUCCGCACCCUGUCCCG**G**
 entry 40 GGGAUAUAC**G**GGGCCCGUCAAGGCC**G**UAGCGAAACCGACUGUUGAAACUGUGCGAAUAAUCCGCACCCUGUCCCGG
 ((((((.....(((.....))))).(((.....))))).(((.....))))).(((.....))))).(((.....))))).
 exit GGGAUAUACGGG**G**CCCGUCAAGGCC**G**UAGCGAAACCGACUGUUGA**G**ACUGUGCGAAUAAUCCGCACCCUGUCCCGG
 entry 41 GGGAUAUACGGG**G**CCCGUCAAGGCC**G**UAGCGAAACCGACUGUUGAGACUGUGCGAAUAAUCCGCACCCUGUCCCGG
 ((((((.....(((.....))))).(((.....))))).(((.....))))).(((.....))))).(((.....))))).
 exit GGGAUAUACGGGCCCC**U**UCAAG**G**CC**A**UAGCGAAACCGACUGUUGA**A**ACUGUGCGAAUAAUCCGCACCCUGUCCCG**G**
 entry 42 GGGAUAUACGGGCCCC**U**UCAAG**C**CAUAGCGAAACCGACUGUUGAAACUGUGCGAAUAAUCCGCACCCUGUCCCG**G**
 ((((((.....(((.....))))).(((.....))))).(((.....))))).(((.....))))).(((.....))))).
 exit GGGAU**G**AUAGGG**C**GUGU**G**AUAGCCCAUAGCGAAAC**CC**CG**C**UGA**G**CUUGUGCGA**CG**UUUGUGCACCUGUCCCG**C**
 entry 43 GGG**A**GAUAGGG**C**GUGUGAUAGCCCAUAGCGAAAC**CC**CG**C**UGA**G**CUUGUGCGACGUUUGUGCACCUGUCCCG**C**
 ((((((.....(((.....))))).(((.....))))).(((.....))))).(((.....))))).(((.....))))).
 exit GGG**A**GAUAGGG**C**GUGUGAUAGCCCAUAGCGAAAC**CC**CG**C**UGA**G**CUUGUGCGACGUUUGUGCACCUGUCCCG**C**
 entry 44 GGG**C**AGAUAGGG**C**GUGUGAUAGCCCAUAGCGAAAC**CC**CG**C**UGA**G**CUUGUGCGACGUUUGUGCACCUGUCCCG**C**
 ((((((.....(((.....))))).(((.....))))).(((.....))))).(((.....))))).(((.....))))).

Transition inducing point mutations

Neutral point mutations

Change in RNA sequences during the final five relay steps 39 → 44

28 neutral point mutations during a long quasi-stationary epoch

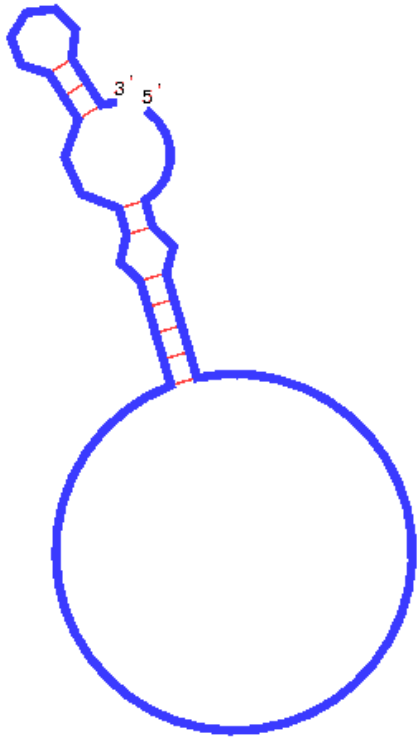


entry	GGUAUGGGCGUUGAAUAGUAGGGUUUAAACCAAUCGG	CAACGAUCUCGUGUGCGCAUUUCAUAUCCCGUACAGAA
8	.(((((((((((((. (((.))))))(((((.))))))))))	
exit	GGUAUGGGCGUUGAAUA	AJAGGGUUUAAACCAAUCGGCCAACGAUCUCGUGUGCGCAUUUCAUAU
entry	GGUAUGGGCGUUGAAUA	AUAGGGUUUAAACCAAUCGGCCAACGAUCUCGUGUGCGCAUUUCAUAU
9	.(((((((.(((((. (((.))))))(((((.))))))	
exit	UGGAUGGACGUUGAAUAACA	AGGU
entry	UGGAUGGACGUUGAAUAACA	AGGU
10	.(((((((.(((((. (((.))))))(((((.))))))	
exit	UGGAUGGACGUUGAAUAACA	AGGU

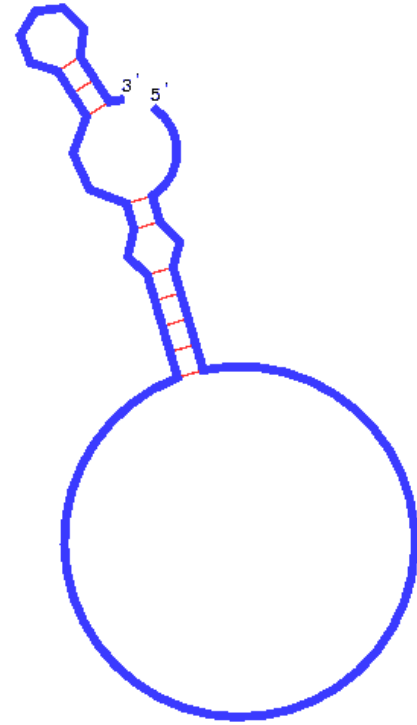
Transition inducing point mutations

Neutral point mutations

Neutral genotype evolution during phenotypic stasis



AUGC



GC

Movies of optimization trajectories over the **AUGC** and the **GC** alphabet





1. RNA and properties and function
2. RNA structures
3. Neutral networks and intersections
4. RNA evolution *in silico*
- 5. Intersection molecules and RNA switches**
6. Neutrality in evolution and design

- minus the background levels observed in the HSP in the control (Sar1-GDP-containing) incubation that prevents COPII vesicle formation. In the microsome control, the level of p115-SNARE associations was less than 0.1%.
46. C. M. Carr, E. Grote, M. Munson, F. M. Hughson, P. J. Novick, *J. Cell Biol.* **146**, 333 (1999).
 47. C. Ungermann, B. J. Nichols, H. R. Pelham, W. Wickner, *J. Cell Biol.* **140**, 61 (1998).
 48. E. Grote and P. J. Novick, *Mol. Biol. Cell* **10**, 4149 (1999).
 49. P. Uetz et al., *Nature* **403**, 623 (2000).
 50. GST-SNARE proteins were expressed in bacteria and purified on glutathione-Sepharose beads using standard methods. Immobilized GST-SNARE protein (0.5 μ M) was incubated with rat liver cytosol (20 mg) or purified recombinant p115 (0.5 μ M) in 1 ml of NS buffer containing 1% BSA for 2 hours at 4°C with rotation. Beads were briefly spun (3000 rpm for 10 s) and sequentially washed three times with NS buffer and three times with NS buffer supplemented with 150 mM NaCl. Bound proteins were eluted three times in 50 μ l of 50 mM tris-HCl (pH 8.5), 50 mM reduced glutathione, 150 mM NaCl, and 0.1% Triton X-100 for 15 min at 4°C with intermittent mixing, and elutes were pooled. Proteins were precipitated by MeOH/CH₂Cl₂ and separated by SDS-polyacrylamide gel electrophoresis (PAGE) followed by immunoblotting using p115 mAb 13F12.
 51. V. Rybin et al., *Nature* **383**, 266 (1996).
 52. K. G. Hardwick and H. R. Pelham, *J. Cell Biol.* **119**, 513 (1992).
 53. A. P. Newman, M. E. Groesch, S. Ferro-Novick, *EMBO J.* **11**, 3609 (1992).
 54. A. Spang and R. Schekman, *J. Cell Biol.* **143**, 589 (1998).
 55. M. F. Rexach, M. Latterich, R. W. Schekman, *J. Cell Biol.* **126**, 1133 (1994).
 56. A. Mayer and W. Wickner, *J. Cell Biol.* **136**, 307 (1997).
 57. M. D. Turner, H. Plutner, W. E. Balch, *J. Biol. Chem.* **272**, 13479 (1997).
 58. A. Price, D. Seals, W. Wickner, C. Ungermann, *J. Cell Biol.* **148**, 1231 (2000).
 59. X. Cao and C. Barlowe, *J. Cell Biol.* **149**, 55 (2000).
 60. G. G. Tall, H. Hama, D. B. DeWald, B. F. Horadzovsky, *Mol. Biol. Cell* **10**, 1873 (1999).
 61. C. G. Burd, M. Peterson, C. R. Cowles, S. D. Emr, *Mol. Biol. Cell* **8**, 1089 (1997).
 62. M. R. Peterson, C. G. Burd, S. D. Emr, *Curr. Biol.* **9**, 159 (1999).
 63. M. G. Waters, D. O. Clary, J. E. Rothman, *J. Cell Biol.* **118**, 1015 (1992).
 64. D. M. Walter, K. S. Paul, M. G. Waters, *J. Biol. Chem.* **273**, 29565 (1998).
 65. N. Hui et al., *Mol. Biol. Cell* **8**, 1777 (1997).
 66. T. E. Kreis, *EMBO J.* **5**, 931 (1986).
 67. H. Plutner, H. W. Davidson, J. Saraste, W. E. Balch, *J. Cell Biol.* **119**, 1097 (1992).
 68. D. S. Nelson et al., *J. Cell Biol.* **143**, 319 (1998).
 69. We thank G. Waters for p115 cDNA and p115 mAbs; G. Warren for p97 and p47 antibodies; R. Scheller for rbt1, membrin, and sec22 cDNAs; H. Plutner for excellent technical assistance; and P. Tan for help during the initial phase of this work. Supported by NIH grants GM 33301 and GM42336 and National Cancer Institute grant CA58689 (W.E.B.), a NIH National Research Service Award (B.D.M.), and a Wellcome Trust International Traveling Fellowship (B.B.A.).

20 March 2000; accepted 22 May 2000

One Sequence, Two Ribozymes: Implications for the Emergence of New Ribozyme Folds

Erik A. Schultes and David P. Bartel*

We describe a single RNA sequence that can assume either of two ribozyme folds and catalyze the two respective reactions. The two ribozyme folds share no evolutionary history and are completely different, with no base pairs (and probably no hydrogen bonds) in common. Minor variants of this sequence are highly active for one or the other reaction, and can be accessed from prototype ribozymes through a series of neutral mutations. Thus, in the course of evolution, new RNA folds could arise from preexisting folds, without the need to carry inactive intermediate sequences. This raises the possibility that biological RNAs having no structural or functional similarity might share a common ancestry. Furthermore, functional and structural divergence might, in some cases, precede rather than follow gene duplication.

Related protein or RNA sequences with the same folded conformation can often perform very different biochemical functions, indicating that new biochemical functions can arise from preexisting folds. But what evolutionary mechanisms give rise to sequences with new macromolecular folds? When considering the origin of new folds, it is useful to picture, among all sequence possibilities, the distribution of sequences with a particular fold and function. This distribution can range very far in sequence space (1). For example, only seven nucleotides are strictly conserved among the group I self-splicing introns, yet secondary (and presumably tertiary) structure within the core of the ribozyme is preserved (2). Because these dis-

parate isolates have the same fold and function, it is thought that they descended from a common ancestor through a series of mutational variants that were each functional. Hence, sequence heterogeneity among divergent isolates implies the existence of paths through sequence space that have allowed neutral drift from the ancestral sequence to each isolate. The set of all possible neutral paths composes a "neutral network," connecting in sequence space those widely dispersed sequences sharing a particular fold and activity, such that any sequence on the network can potentially access very distant sequences by neutral mutations (3-5).

Theoretical analyses using algorithms for predicting RNA secondary structure have suggested that different neutral networks are interwoven and can approach each other very closely (3, 5-8). Of particular interest is whether ribozyme neutral networks approach each other so closely that they intersect. If so, a single sequence would be capable of folding into two different conformations, would

have two different catalytic activities, and could access by neutral drift every sequence on both networks. With intersecting networks, RNAs with novel structures and activities could arise from previously existing ribozymes, without the need to carry non-functional sequences as evolutionary intermediates. Here, we explore the proximity of neutral networks experimentally, at the level of RNA function. We describe a close apposition of the neutral networks for the hepatitis delta virus (HDV) self-cleaving ribozyme and the class III self-ligating ribozyme.

In choosing the two ribozymes for this investigation, an important criterion was that they share no evolutionary history that might confound the evolutionary interpretations of our results. Choosing at least one artificial ribozyme ensured independent evolutionary histories. The class III ligase is a synthetic ribozyme isolated previously from a pool of random RNA sequences (9). It joins an oligonucleotide substrate to its 5' terminus. The prototype ligase sequence (Fig. 1A) is a shortened version of the most active class III variant isolated after 10 cycles of *in vitro* selection and evolution. This minimal construct retains the activity of the full-length isolate (10). The HDV ribozyme carries out the site-specific self-cleavage reactions needed during the life cycle of HDV, a satellite virus of hepatitis B with a circular, single-stranded RNA genome (11). The prototype HDV construct for our study (Fig. 1B) is a shortened version of the antigenomic HDV ribozyme (12), which undergoes self-cleavage at a rate similar to that reported for other antigenomic constructs (13, 14).

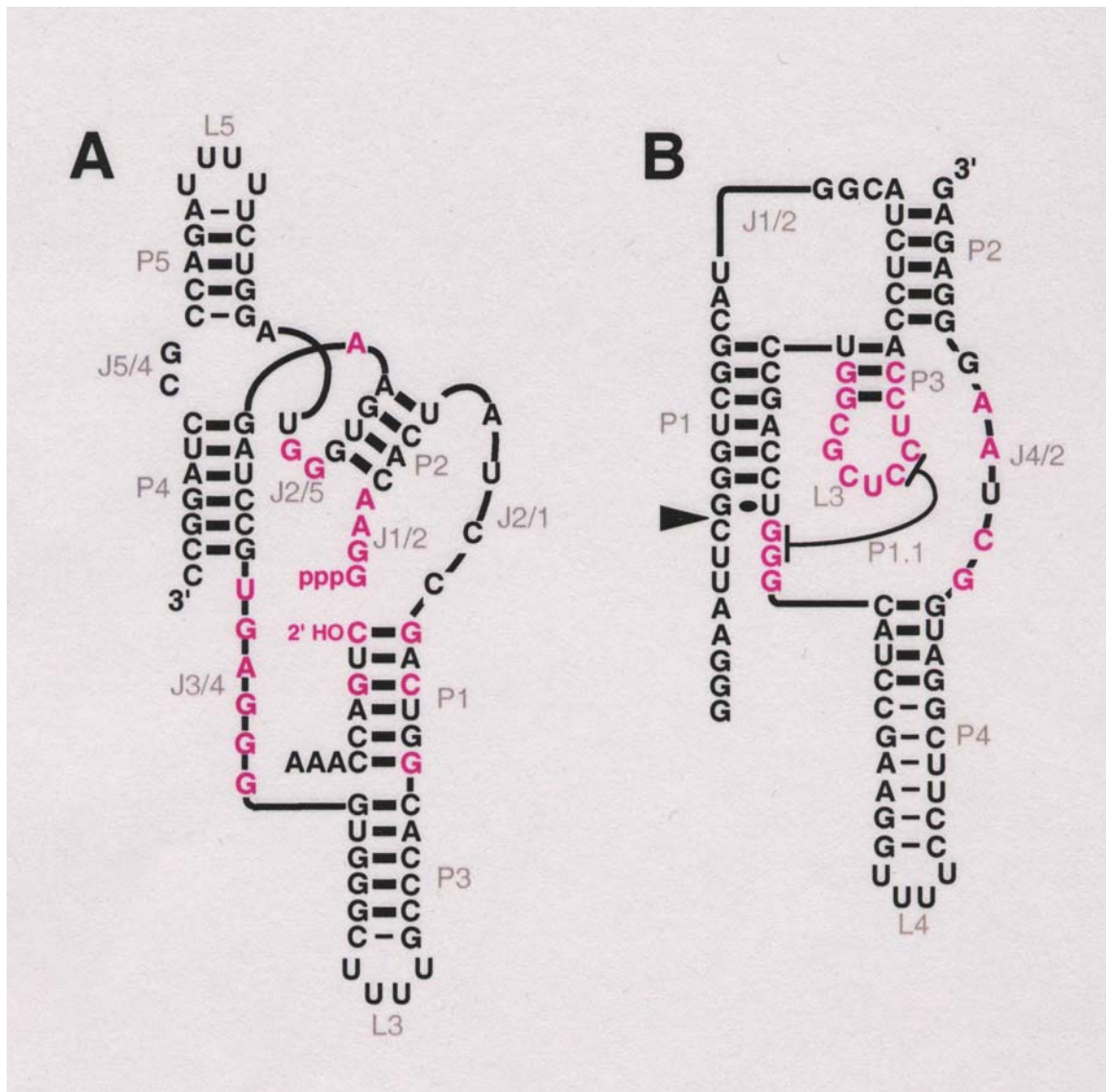
The prototype class III and HDV ribozymes have no more than the 25% sequence identity expected by chance and no fortuitous structural similarities that might favor an intersection of their two neutral networks. Nevertheless, sequences can be designed that simultaneously satisfy the base-pairing requirements

A ribozyme switch

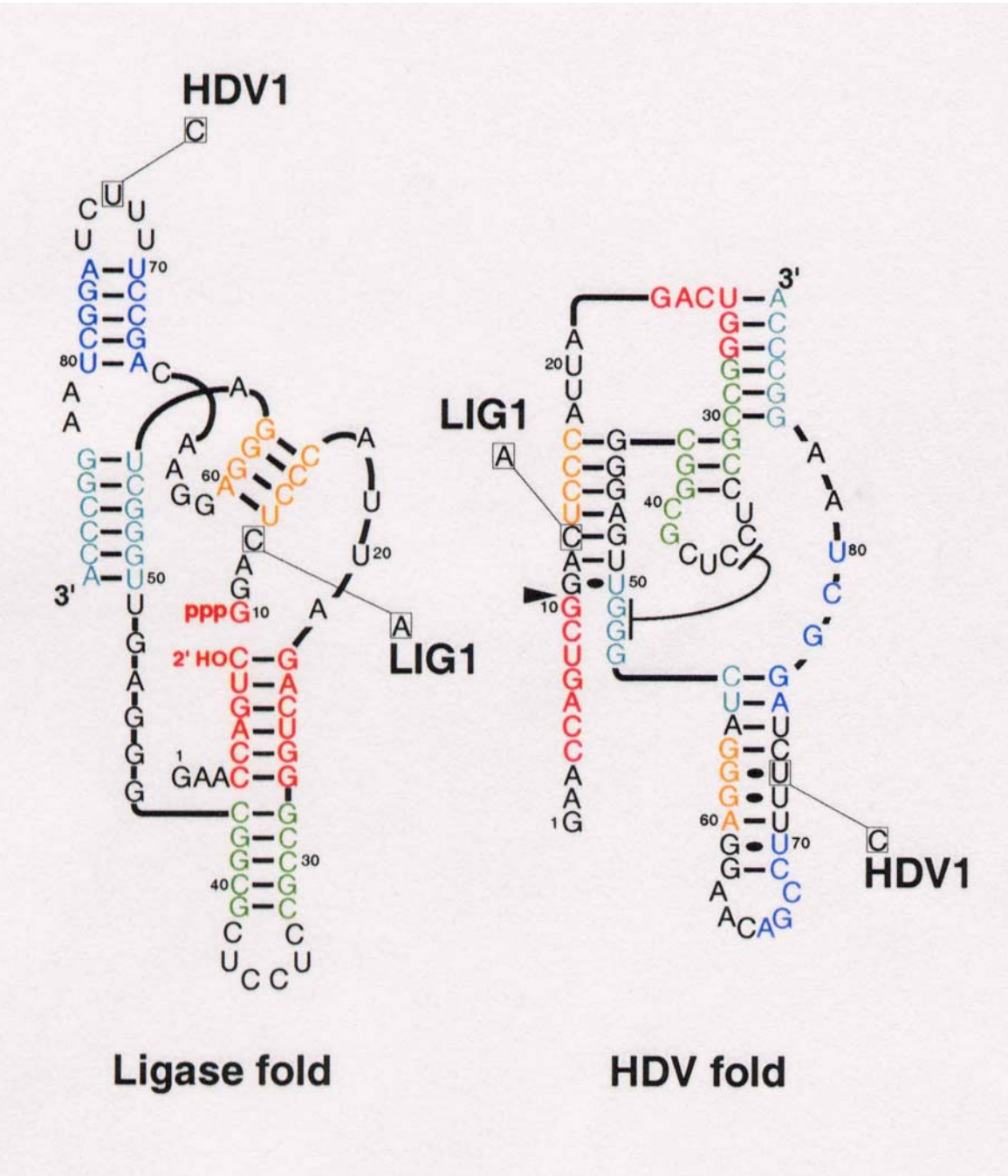
E.A.Schultes, D.B.Bartel, *Science*
289 (2000), 448-452

Whitehead Institute for Biomedical Research and Department of Biology, Massachusetts Institute of Technology, 9 Cambridge Center, Cambridge, MA 02142, USA.

*To whom correspondence should be addressed. E-mail: dbartel@wi.mit.edu

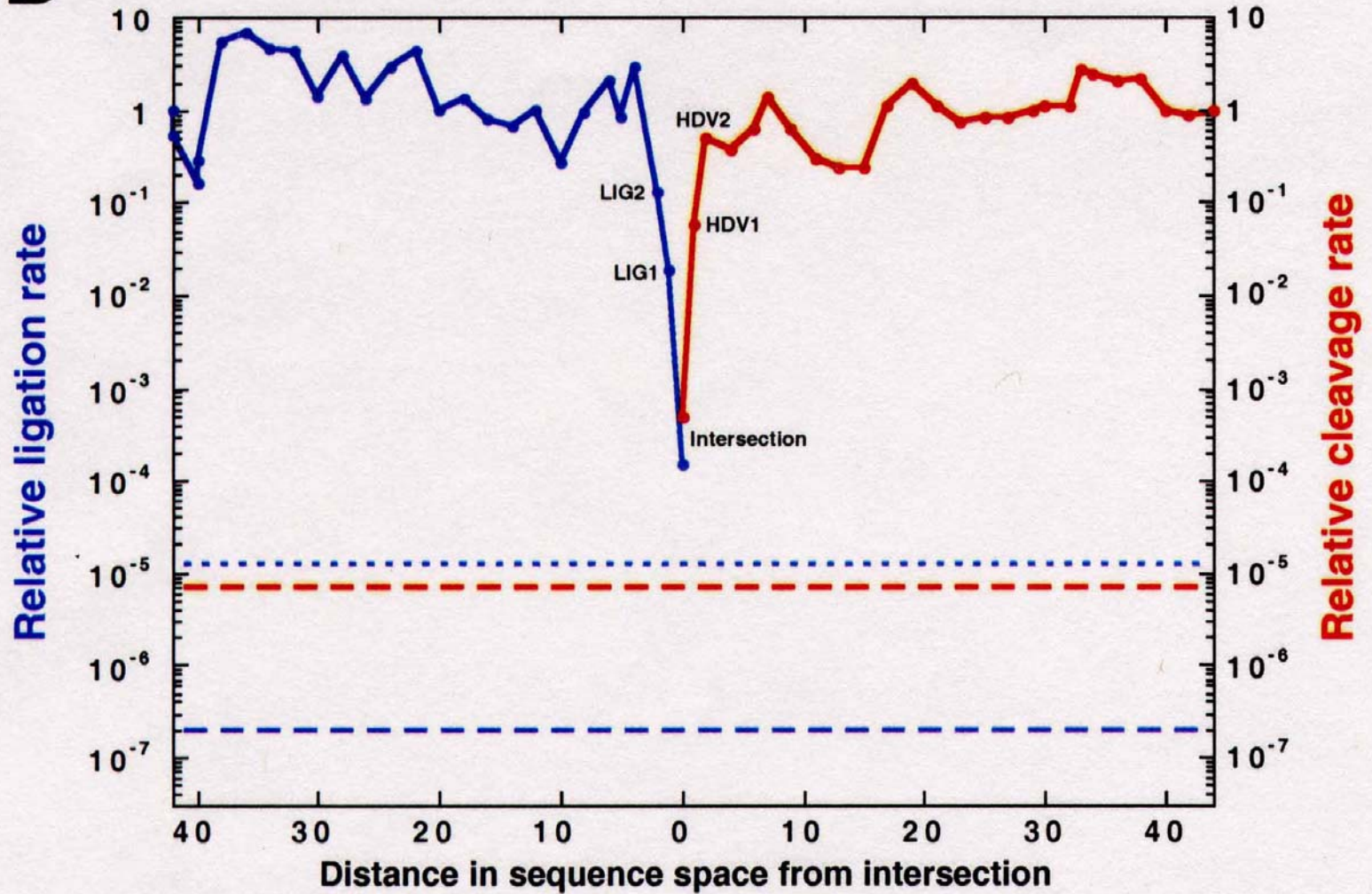


Two ribozymes of chain lengths $n = 88$ nucleotides: An artificial ligase (**A**) and a natural cleavage ribozyme of hepatitis- δ -virus (**B**)

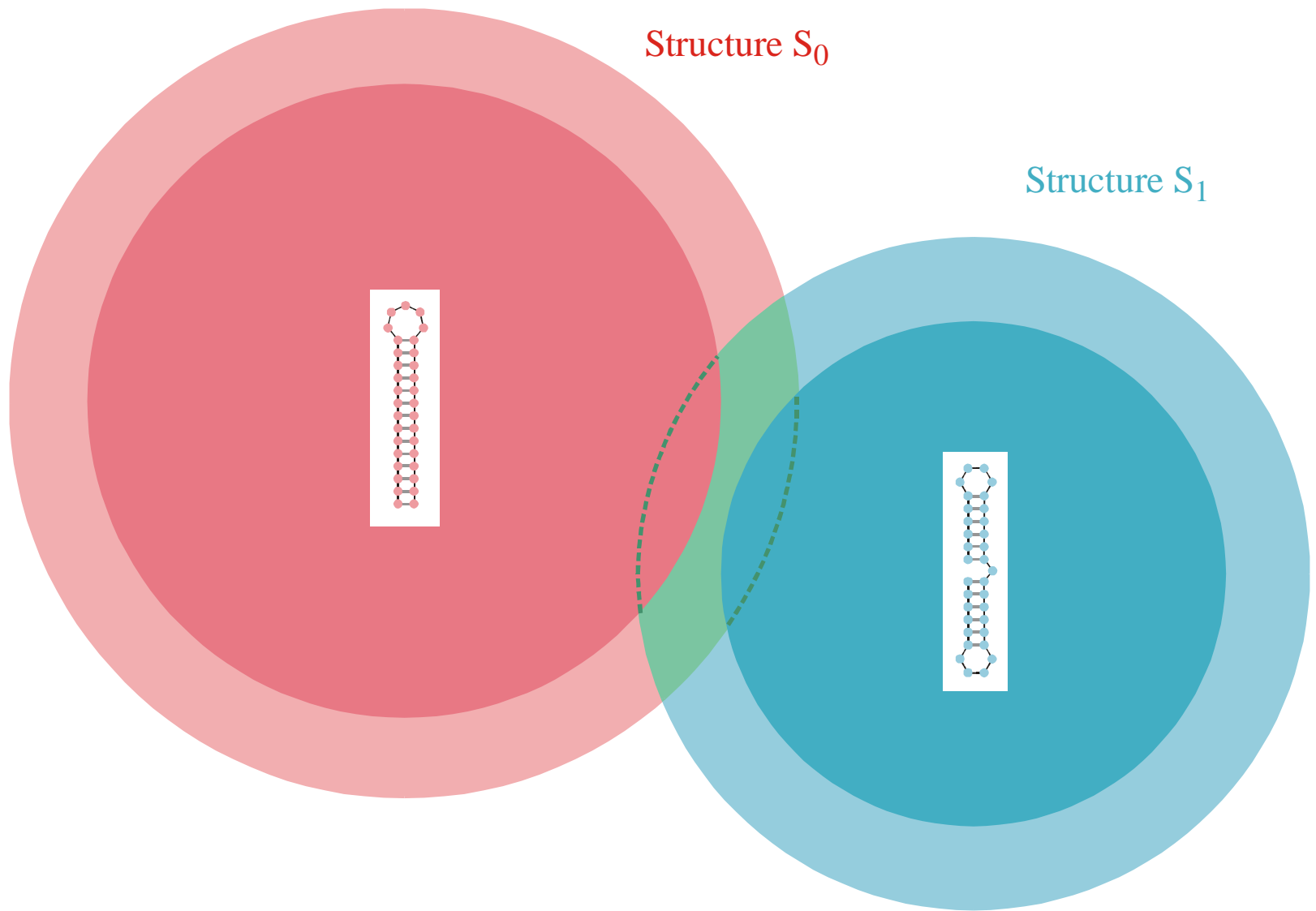


The sequence at the *intersection*:

An RNA molecules which is 88 nucleotides long and can form both structures

B

Two neutral walks through sequence space with conservation of structure and catalytic activity



Intersection of two compatible sets: $C_0 \cap C_1$

The intersection of two compatible sets is always non empty: $C_0 \cap C_1 \neq \emptyset$

J. H. A. Nagel, C. Flamm, I. L. Hofacker, K. Franke, M. H. de Smit, P. Schuster, and C. W. A. Pleij. *Structural parameters affecting the kinetic competition of RNA hairpin formation*, in press 2004.

J. H. A. Nagel, J. Møller-Jensen, C. Flamm, K. J. Öistämö, J. Besnard, I. L. Hofacker, A. P. Gulyaev, M. H. de Smit, P. Schuster, K. Gerdes and C. W. A. Pleij. *The refolding mechanism of the metastable structure in the 5'-end of the hok mRNA of plasmid R1*, submitted 2004.

1. RNA and properties and function
2. RNA structures
3. Neutral networks and intersections
4. RNA evolution *in silico*
5. Intersection molecules and RNA switches
- 6. Neutrality in evolution and design**



*„... Variations neither useful not injurious would not be affected by natural selection, and would be left either a fluctuating element, as perhaps we see in certain polymorphic species, or would ultimately become fixed, owing to the nature of the organism and the nature of the conditions.
...“*

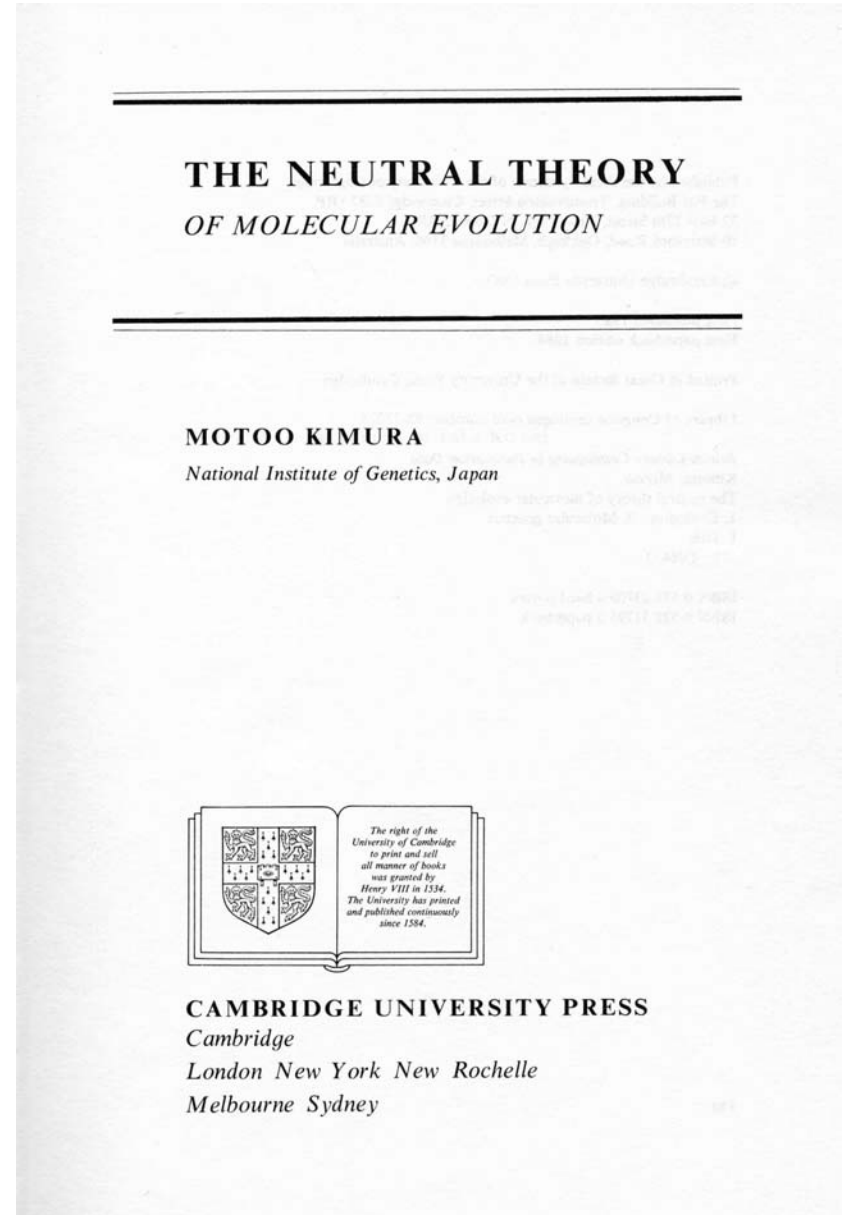
Charles Darwin, Origin of species (1859)



Motoo Kimura's Populationsgenetik der Neutral Evolution.

Evolutionary rate at the molecular level.
Nature **217**: 624-626, 1955.

The Neutral Theory of Molecular Evolution.
Cambridge University Press. Cambridge,
UK, 1983.



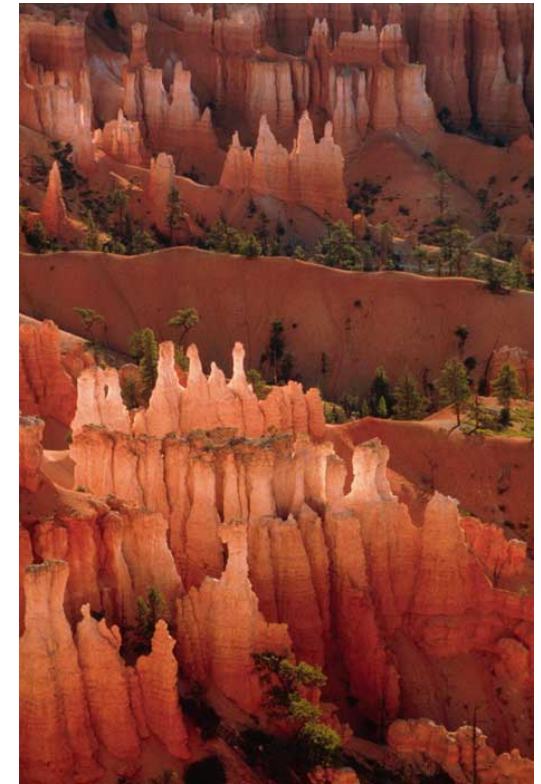


Mount Fuji

Example of a smooth landscape on Earth



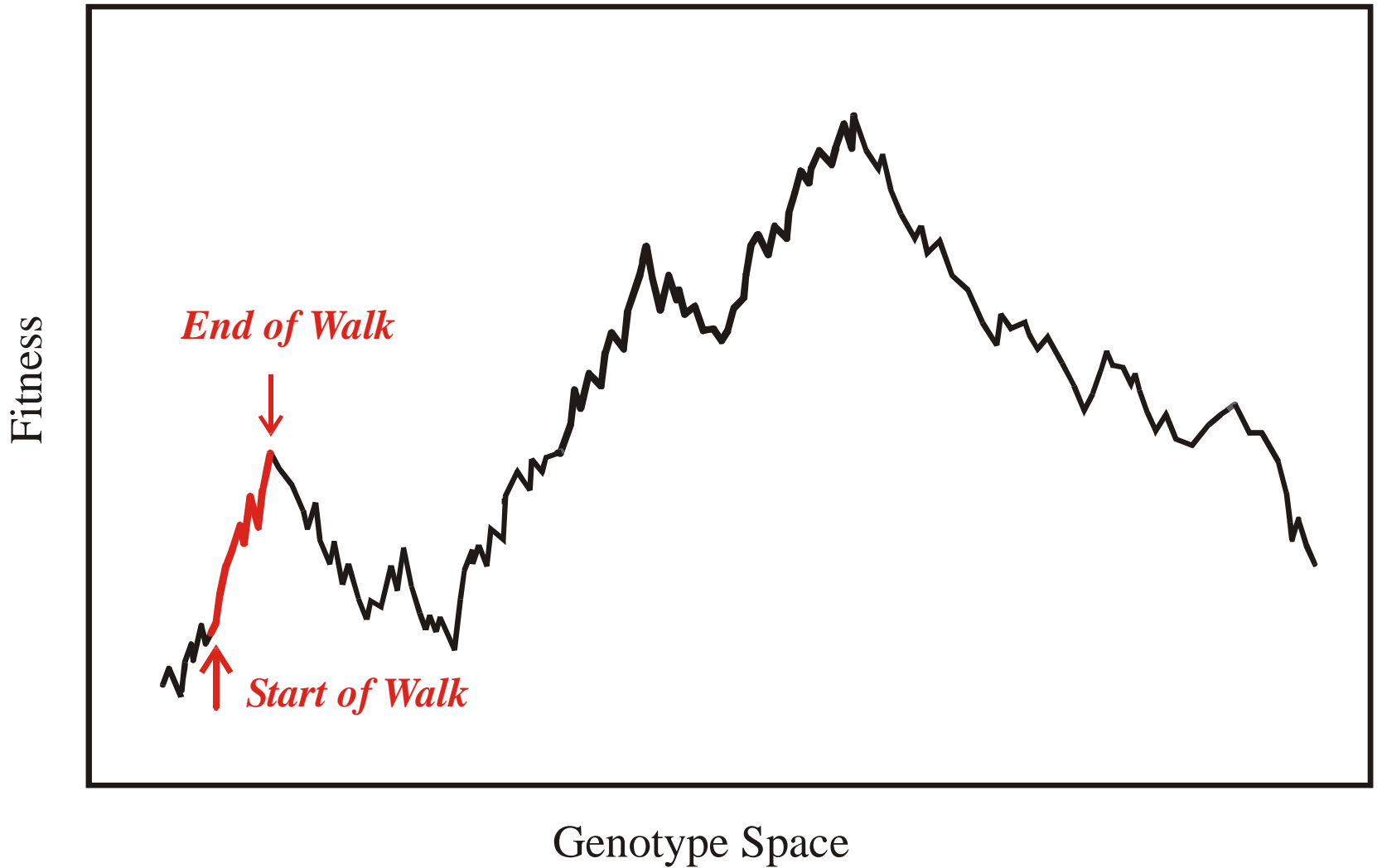
Dolomites



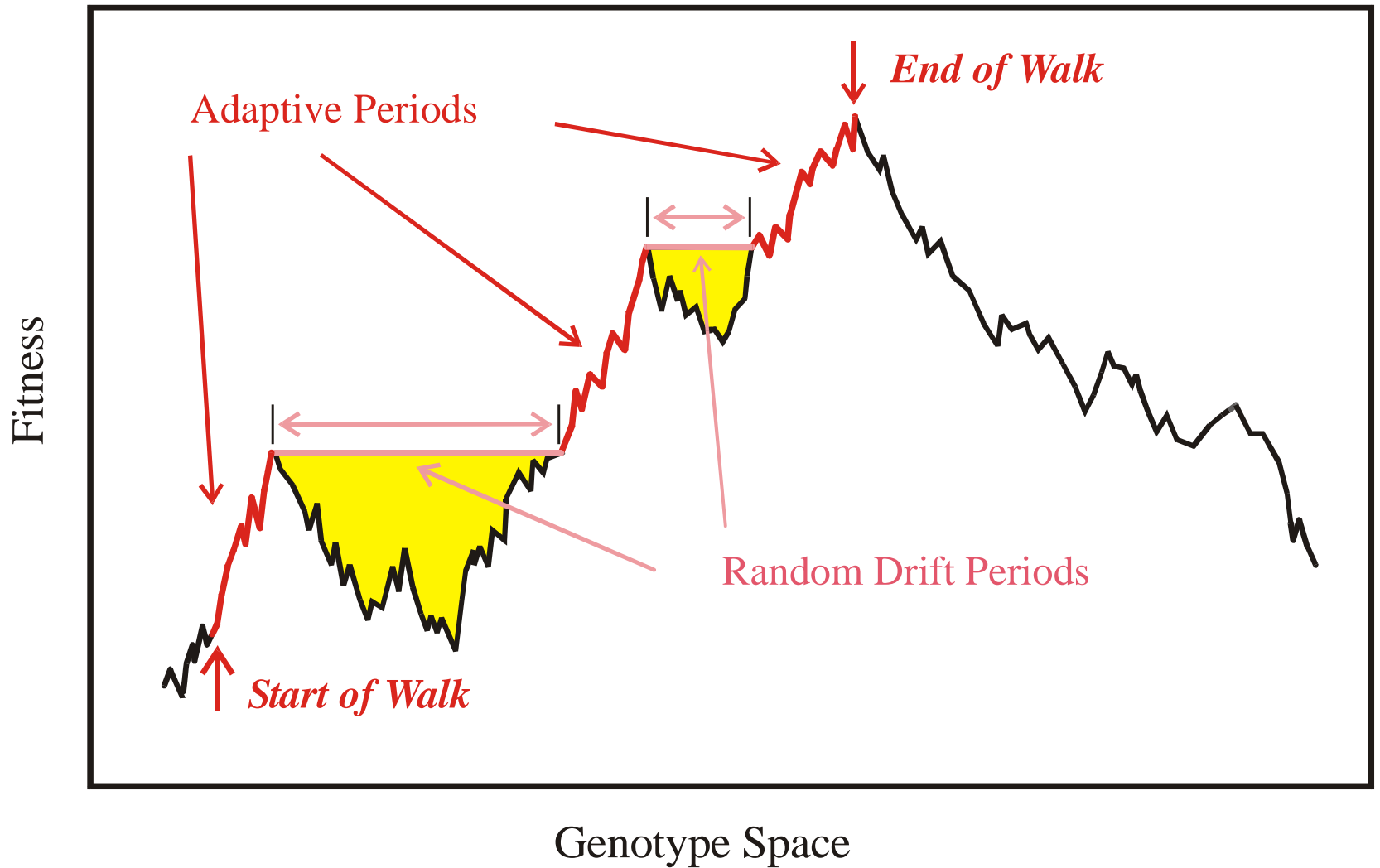
Bryce Canyon



Examples of rugged landscapes on Earth



Evolutionary optimization in absence of neutral paths in sequence space



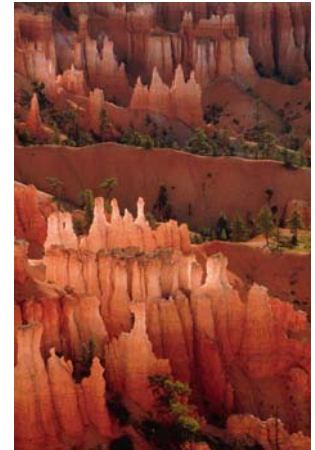
Evolutionary optimization including neutral paths in sequence space



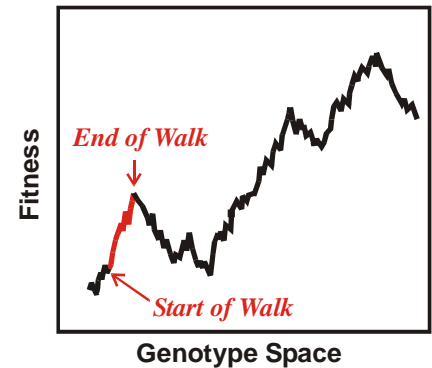
Grand Canyon

Example of a landscape on Earth with ‘neutral’
ridges and plateaus

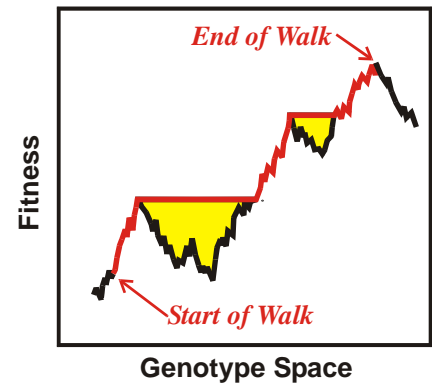
- Conformational and mutational landscapes of biomolecules as well as fitness landscapes of evolutionary biology are **rugged**.

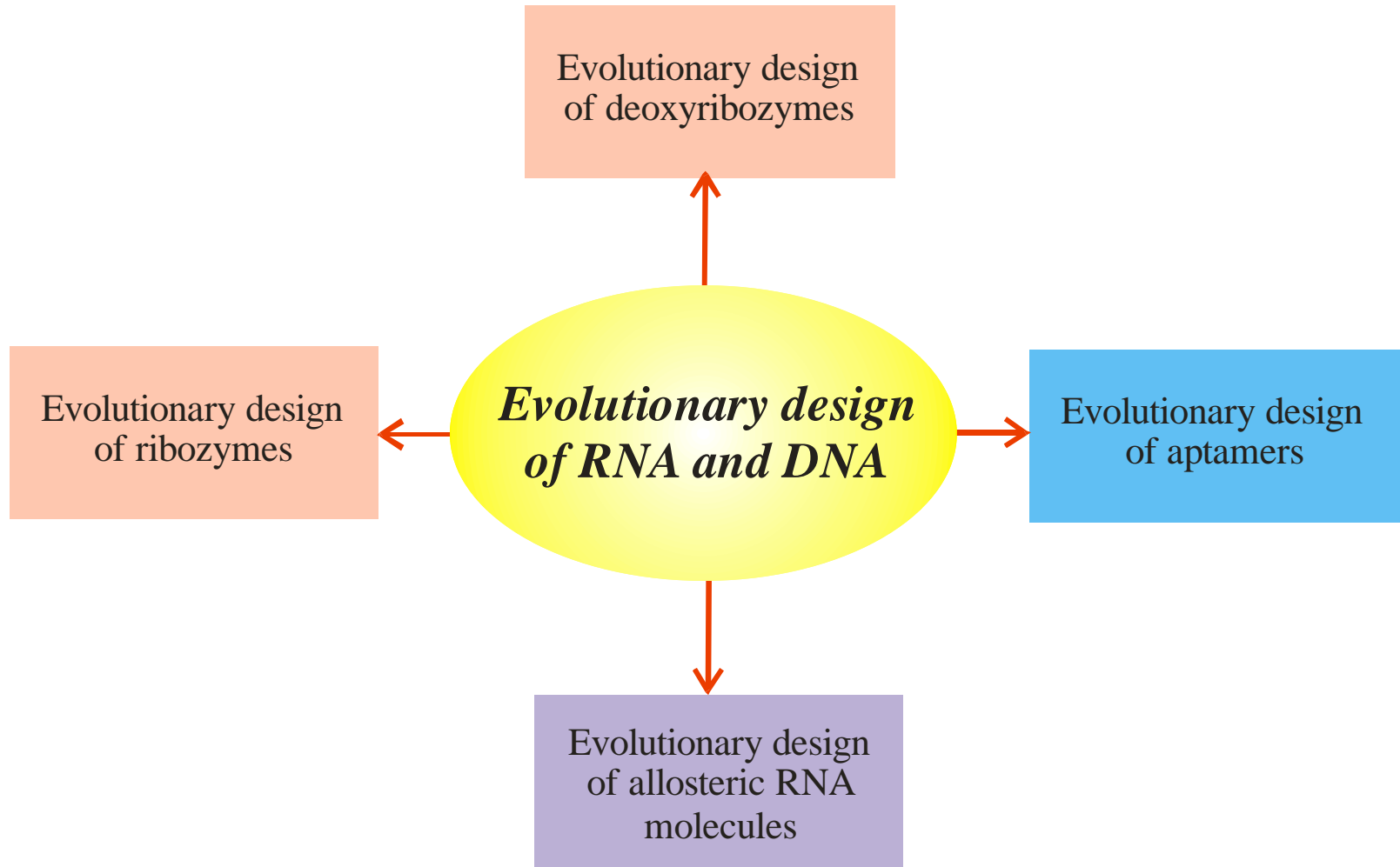


- **Adaptive** or **non-descending walks** on rugged landscapes end commonly at one of the low lying local maxima.

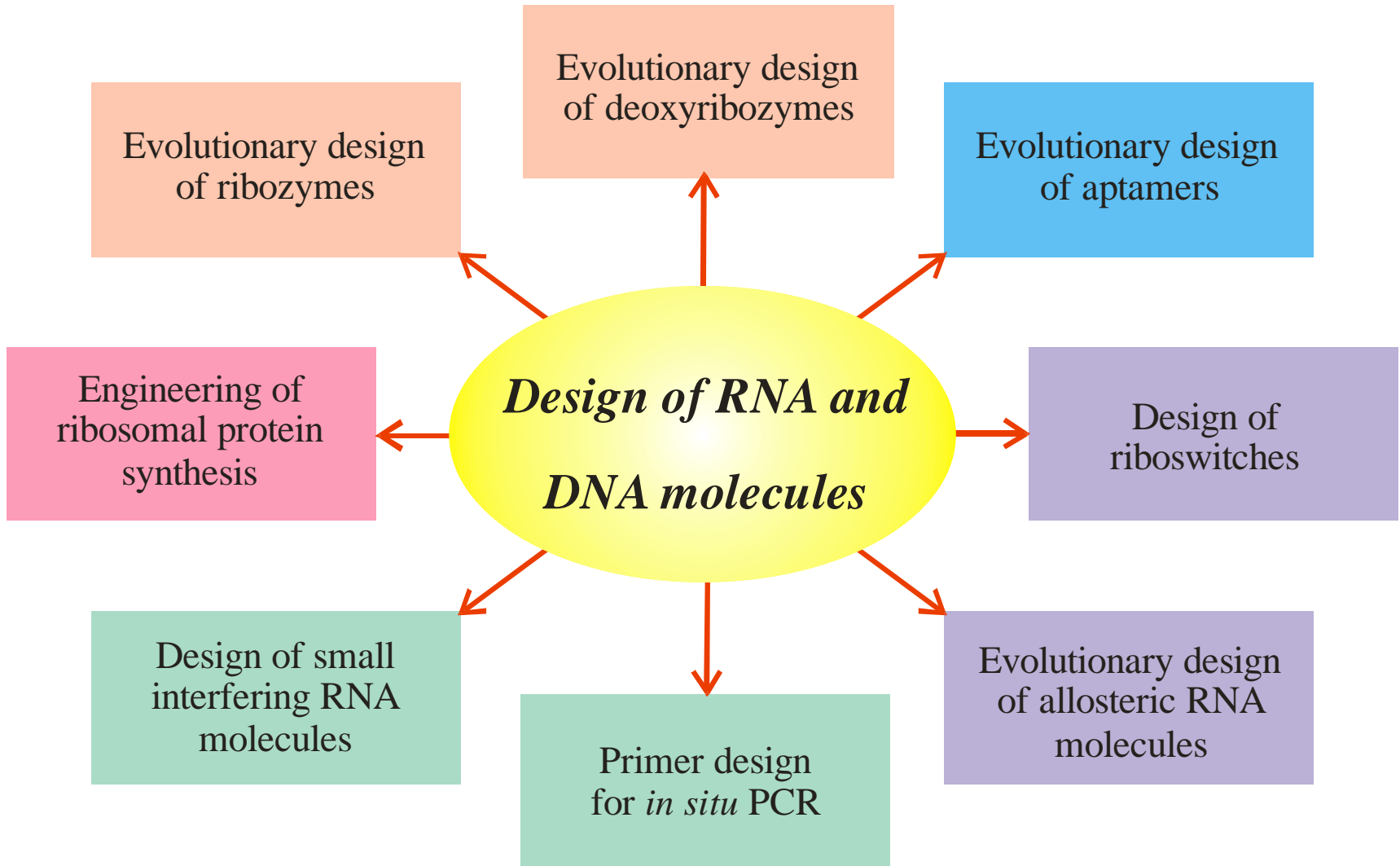


- Selective neutrality in the form of **neutral networks** plays an active role in evolutionary optimization and enables populations to reach high local maxima or even the global optimum.





Examples of evolutionary design of RNA or DNA molecules



Examples of evolutionary and rational design of RNA and DNA molecules

Acknowledgement of support

Fonds zur Förderung der wissenschaftlichen Forschung (FWF)

Projects No. 09942, 10578, 11065, 13093
13887, and 14898

Jubiläumsfonds der Österreichischen Nationalbank

Project No. Nat-7813

European Commission: Project No. EU-980189

Austrian Genome Research Program – GEN-AU

Siemens AG, Austria

Universität Wien and the Santa Fe Institute



Universität Wien

Web-Page for further information:

<http://www.tbi.univie.ac.at/~pks>

