Darwinsche Evolution aus molekularer Sicht

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- 1. Darwinsche Evolution
- 2. Evolutionsexperimente mit Molekülen
- 3. Replikation, Mutation und Fitnesslandschaften
- 4. Evolution *in silico*
- 5. Neutrale Evolution
- 6. Multistabilität und RNA-Schalter

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	Generation time	Selection and adaptation 10 000 generations	Genetic drift in small populations 10 ⁶ generations	Genetic drift in large populations 10 ⁷ generations
RNA molecules	10 sec	27.8 h = 1.16 d	115.7 d	3.17 a
	1 min	6.94 d	1.90 a	19.01 a
Bacteria	20 min	138.9 d	38.03 a	380 a
	10 h	11.40 a	1 140 a	11 408 a
Multicelluar organisms	10 d	274 a	27 380 a	273 800 a
	20 a	20 000 a	2×10^7 a	2×10^8 a

Time scales of evolutionary change



Three necessary conditions for Darwinian evolution are:

- 1. Multiplication,
- 2. Variation, and
- 3. Selection.

Variation through mutation and recombination operates on the genotype whereas the phenotype is the target of selection.

One important property of the Darwinian scenario is that variations in the form of mutations or recombination events occur uncorrelated with their effects on the selection process.

All conditions can be fulfilled not only by cellular organisms but also by nucleic acid molecules in suitable cell-free experimental assays.

Bacterial Evolution

S. F. Elena, V. S. Cooper, R. E. Lenski. *Punctuated evolution caused by selection of rare beneficial mutants*. Science **272** (1996), 1802-1804

D. Papadopoulos, D. Schneider, J. Meier-Eiss, W. Arber, R. E. Lenski, M. Blot. *Genomic evolution during a 10,000-generation experiment with bacteria*. Proc.Natl.Acad.Sci.USA **96** (1999), 3807-3812



1 year » 2400 generations

Serial transfer of Escherichia coli cultures in Petri dishes





Fig. 1. Change in average cell size (1 fl = 10^{-15} L) in a population of *E. coli* during 3000 generations of experimental evolution. Each point is the mean of 10 replicate assays (*22*). Error bars indicate 95% confidence intervals. The solid line shows the best fit of a step-function model to these data (Table 1).



Fig. 2. Correlation between average cell size and mean fitness, each measured at 100-generation intervals for 2000 generations. Fitness is expressed relative to the ancestral genotype and was obtained from competition experiments between derived and ancestral cells (6, 7). The open symbols indicate the only two samples assigned to different steps by the cell size and fitness data.

Epochal evolution of bacteria in serial transfer experiments under constant conditions

S. F. Elena, V. S. Cooper, R. E. Lenski. *Punctuated evolution caused by selection of rare beneficial mutants*. Science **272** (1996), 1802-1804



Variation of genotypes in a bacterial serial transfer experiment

D. Papadopoulos, D. Schneider, J. Meier-Eiss, W. Arber, R. E. Lenski, M. Blot. *Genomic evolution during a 10,000-generation experiment with bacteria*. Proc.Natl.Acad.Sci.USA **96** (1999), 3807-3812



В

D. Papadopoulos et al. Genomic evolution during a 10000-generation experiment with bacteria. *Proc.Natl.Acad.Sci.USA* **96**:3807-3812, 1999

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Evolution of RNA molecules based on $Q\beta$ phage

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S.Spiegelman, *An approach to the experimental analysis of precellular evolution*. Quart.Rev.Biophys. **4** (1971), 213-253

C.K.Biebricher, *Darwinian selection of self-replicating RNA molecules*. Evolutionary Biology **16** (1983), 1-52

G.Bauer, H.Otten, J.S.McCaskill, *Travelling waves of* in vitro evolving RNA. *Proc.Natl.Acad.Sci.USA* **86** (1989), 7937-7941

C.K.Biebricher, W.C.Gardiner, *Molecular evolution of RNA* in vitro. Biophysical Chemistry **66** (1997), 179-192

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F.Öhlenschlager, M.Eigen, 30 years later – A new approach to Sol Spiegelman's and Leslie Orgel's in vitro evolutionary studies. Orig.Life Evol.Biosph. 27 (1997), 437-457

RNA sample



Stock solution: Qβ RNA-replicase, ATP, CTP, GTP and UTP, buffer

Anwendung der seriellen Überimpfungstechnik auf RNA-Evolution in Reagenzglas



The increase in RNA production rate during a serial transfer experiment



Stock solution:

activated monomers, **ATP, CTP, GTP, UTP (TTP);** a replicase, an enzyme that performs complemantary replication;

buffer solution

The flowreactor is a device for **studies** of evolution *in vitro* and *in silico*.

Evolutionary design of RNA molecules

D.B.Bartel, J.W.Szostak, **In vitro** *selection of RNA molecules that bind specific ligands*. Nature **346** (1990), 818-822

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Y. Wang, R.R.Rando, *Specific binding of aminoglycoside antibiotics to RNA*. Chemistry & Biology **2** (1995), 281-290

Jiang, A. K. Suri, R. Fiala, D. J. Patel, *Saccharide-RNA recognition in an aminoglycoside antibiotic-RNA aptamer complex*. Chemistry & Biology **4** (1997), 35-50



An example of 'artificial selection' with RNA molecules or 'breeding' of biomolecules



The SELEX technique for the evolutionary preparation of aptamers



tobramycin

5'-GGCACGAGGUUUAGCUACACUCGUGCC-3'



Formation of secondary structure of the tobramycin binding RNA aptamer with $K_D = 9 nM$

L. Jiang, A. K. Suri, R. Fiala, D. J. Patel, *Saccharide-RNA recognition in an aminoglycoside antibiotic-RNA aptamer complex.* Chemistry & Biology **4**:35-50 (1997)



The three-dimensional structure of the tobramycin aptamer complex

L. Jiang, A. K. Suri, R. Fiala, D. J. Patel, Chemistry & Biology **4**:35-50 (1997)

WILEY-VCH

Directed Molecular Evolution of Proteins

or How to Improve Enzymes for Biocatalysis

Edited by Susanne Brakmann and Kai Johnsson





Application of molecular evolution to problems in biotechnology

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,Replication fork' in DNA replication

The mechanism of DNA replication is ,semi-conservative'



Complementary replication is the simplest copying mechanism of RNA.

Complementarity is determined by Watson-Crick base pairs:

G≡C and A=U



Variation of genotypes through mutation

DIE NATURWISSENSCHAFTEN

58. Jahrgang, 1971

Heft to Oktobe

which even in its simplest forms always appears to be

associated with complex macroscopic (i.e. multimolec-ular systems, such as the living cell. As a consequence of the exciting discoveries of "molecular biology", a common version of the subce-question is: Which case first, the previous of the subce-coil? – a modern variant of the old "chicker-and-the-egg" problem. The term "first" is usually meant to define a causal rather than a temporal relationship, assoassociated with complex macroscopic fi.e. multimolec-

define a causal rather than a temporal relationship, sho the words "protein" and "suckie acid" may be sub-stituted by "function" and "information". The question in this form, when applied to the interplay of nucleic acids and proteins as presently encountered in the living cull, leads ad abaurdum, because "function"

Selforganization of Matter and the Evolution of Biological Macromolecules

MANERED EDGEN* Max-Planck-Institut für Biophysikalische Chemie

Karl-Friedrich-Bonhoeffer-Institut, Göttingen-Nikolausberg

J. Introduction	V. Selforganization via Cyclic Catalysis: Proteins 498
1.1. Cause and Effect	V.1. Recognition and Catalysis by Enzymes 498
 Prerequisitos of Selforganization	V.2. Selforganizing Enzyme Cycles (Theory) 499
L2.1. Evolution Must Start from Random Events 467	V.2.1. Catalytic Networks
1.2.2. Instruction Requires Information 467	V.2.2. The Selfreproducing Loop and Its Variants 499
I.2.3. Information Originates or Gains Value by	V.2.3. Competition between Different Cycles:
Selection	Selection
L2.4. Selection Occurs with Special Substances	V.J. Can Proteins Reproduce Themselves 7
under Special Conditions 470	VI. Sollowbering by Founded Catalogic Function
11. Phenoinmological Theory of Selection	VI a We Development of Concention between Norbic
II 4 The Concert "Information" 423	 Vi.1 Line Rodulirement of Cooperation between Nucleic Acids and Destains
II.2 Phonemetrological Equations	VI.1 A Selferenducing Haner Cavle
II.3. Selection Strains	V1.2.1. The Model 503
II.4. Selection Equilibrium	VI.2.2. Theoretical Treatment
II.4. Quality Factor and Error Distribution	VI.1. On the Origin of the Code
IL6. Kinetics of Selection	
	VII. Evolution Experiments
III. Stochastic Approach to Selection	VIL1. The Off-Replicase System
III.4. Limitations of a Deterministic Theory of Selection 484	VII.2. Darwinian Evolution in the Test Tube 512
III.2. Fluctuations around Equilibrium States 484	VII.3. Quantitative Selection Studies
III.3. Fluctuations in the Steady State	VIL4. "Minus One" Experiments
111.4. Stochastic Models as Markov Chains	WHI Annahology and
III.5. Quantitative Discussion of Three Prototypes of	FJJ7. Conclusion
Selection	VIII.1. Limits of Theory
10 Sollowanization Road on Combinantary Records	villi.2. The Concept - value
tion: Narlaic Arida	VIII.3. "Dissipation" and the "Origin of Dirochation." 316
The Way O'F-Hardenships"	VIII.4. The Principles of Selection and Accounter 517
IV.9. Complementary Instruction and Selection	VIII.5. Indeterminant, our internation of Life he Exclained by Our
(Theory) 402	Present Concerns of Physics ?
IV.1. Complementary Base Recognition (Experimental	i talin chicipi di tajina i i i i i i i i i i jao
Duda)	IX. Deutsche Zurannentainung
IV.1.t. Single Pair Formation 404	
IV.1.2. Cooperative Interactions in Oligo- and	Acknowledgements
Polymncheotides	
IV.1.1. Conclusions about Recognition 496	Literature

I. Introduction

I.I. "Cause and Effect"

The question about the origin of life often appears as a In equasion about the edge of microtent appears as a question about "cause and effect". Physical theories of macroscopic processes annuly involve answers to such questions, even if a statistical interpretation is given to the relation between "cause" and "effect". It is mainly due to the nature of this question that many scientists believe that our present physics does and offer any obvious explanation for the existence of life.

 Partity presented as the "Robbins Lectures" at Pomona College, California, in spring 1970. 234 Naturvissessehaften 1971

Die Naturwissenschaften 64. Jahrgang High 11 November 1977

The Hypercycle

A Principle of Natural Self-Organization

Part A: Emergence of the Hypercycle

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Peter Schuster

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This paper is the first part of a trilogy, which comprises a detailed study of a special type of functional expaniantion and demonstratus its relevance with respect to the origin and avolation of life. Self-replicative macromolecules, such as RNA or DNA in a suit-Self-replaced or materiableoutes, staft as KNA or DNA in a sun-able extrements exhibit a behavior, which we ray call Derivitian and which can be formully represented by the concept of the quasi-points. A quasi-species is defined as u given distribution of macro-moleculus species with closely interrelated sequences, dominated by one or several (degenerate) master copies. External constraints enforce the selection of the best adapted distribution, commonly referred to as the wild-type. Most important for Darwanian behavfor one the oriteria for internal stability of the quasi-species. If for one the extern for internal statisticy of the quasi-species. It these externa as violated, the information stored in the nucleotide sequence of the master copy will desintegrate renversibly leading to an error extintrophy. As a consequence, identic, and evolution of RNA or DNA molecules is limited with respect to the amount of RNA or DNA monutes a minor with respect to the amount of information that can be stored in a single replicative unit. An analysis of experimental data regarding RNA and DNA replication at various leach of organization reveals, that a sufficient amount of information for the build up of a translation patchney can of information for the build up of a transition ratchinery can be painted only via integration of several different replacative multi-lor reproductive cycleto through (severiceal) Takages. A stable func-tional integrations than will make the system to a new level of originization and Davidly enlarge to information capacity considerably. The hypercycle appears to be such a form of organization.

Preview on Part B: The Abstract Humercycle

The mathematical analysis of dynamical systems using methods of differential topology, yields the result that there is only one type of mediatelenas which fulfills the following requirements: Ope of manhadram when rutum the colouring requirements: The informations showd in each single replacitive any(or response-tive cycls) must be maintained, i.e., the respective master copies must competitive theorem of the state of distributions. Despite their competitive behavior there units must results a cooperation which includes all functionally integrated species. On the other which includes all functionally infigurated species. On the other hand, the cryst as a whole stud construct to compute acrosply with aty other single entity or linked anountible which does not countribut as its insugraved function. These tragutements are cratical for a selection of the best adopted interactions theorem on the selection of the best adopted interactions. Only

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hypercyclic organizations are able to fulfil these requirements. Non system integers among the avicences reproduction cycles, such as chains or branched, true-like networks are devoid of such prop-The mathematical methods used for proving these assertious are

the recommendation methods used for proving these analysis in higher-dimen-fished-point. Lyapernov- and trajectorial analysis in higher-dimen-tional phase spaces, spenned by the concentration coordinates of the cooperating portners. The self-organizing properties of hypersy-cles are elucidated, using analytical as well as numerical techniques

Proving on Part C: The Realized Report of

A realistic model of a hypercycle relevant with respect to the origin of the genetic code and the translation machinery is presented. It includes the following features referring to natural systems: 1) The hypersystems a sufficiently emple surseture to adult an origination, with finite probability ander purblotic conditions. 3 It permits a continuous emergence from closely interrelated

(), RNA-like) procursors, originally bring members of a stable RNA quari-species and having been amplified to a level of higher aban

3) The expansion structure and the properties of single (ano-tions) units of this logarcycle are still reflected in the present gaments code in the translation apparatus of the proharyotic cell, as well as in certain bacturial vipous.

J. The Paradigm of Unity and Diversity in Evolution

Why do millions of species, plants and animals, exist, while there is only one basic molecular machinery of the cell: one universal genetic code and unique chiralities of the macromolecules?

The geneticists of our day would not hesitate to give an immediate answere to the first part of this question. Diversity of species is the outcome of the tremendous branching process of evolution with its myriads of single sters of reproduction and mutation. It in-

M. Eigen P. Schuster The Hypercycle

A Principle of Natural Self-Organization



Chemical kinetics of molecular evolution



$$\frac{dx_i}{dt} = \sum_{i=1}^n f_i Q_{ij} x_i - x_j \Phi \quad \text{with} \quad \Phi = \sum_{i=1}^n f_i x_i$$

and
$$\sum_{i=1}^n x_i = 1$$

$$Q_{ij} = (1-p)^{n-d_H(X_i,X_j)} p^{d_H(X_i,X_j)}; \quad p \dots \text{ error rate per digit}$$

 $d_H(X_i, X_j)$... Hamming distance between X_i and X_j

$$\sum_{j=1}^{n} Q_{ij} = 1$$

The replication-mutation equation

Mutation-selection equation: $[I_i] = x_i \ge 0, f_i > 0, Q_{ii} \ge 0$

$$\frac{dx_i}{dt} = \sum_{j=1}^n f_j Q_{ji} x_j - x_i \phi, \quad i = 1, 2, \dots, n; \quad \sum_{i=1}^n x_i = 1; \quad \phi = \sum_{j=1}^n f_j x_j = \overline{f}$$

Solutions are obtained after integrating factor transformation by means of an eigenvalue problem

$$x_{i}(t) = \frac{\sum_{k=0}^{n-1} \ell_{ik} \cdot c_{k}(0) \cdot \exp(\lambda_{k}t)}{\sum_{j=1}^{n} \sum_{k=0}^{n-1} \ell_{jk} \cdot c_{k}(0) \cdot \exp(\lambda_{k}t)}; \quad i = 1, 2, \dots, n; \quad c_{k}(0) = \sum_{i=1}^{n} h_{ki} x_{i}(0)$$

$$W \div \{f_i Q_{ij}; i, j=1,2,\cdots,n\}; \ L = \{\ell_{ij}; i, j=1,2,\cdots,n\}; \ L^{-1} = H = \{h_{ij}; i, j=1,2,\cdots,n\}$$

$$L^{-1} \cdot W \cdot L = \Lambda = \{\lambda_k; k=0, 1, \cdots, n-1\}$$










SELF-REPLICATION WITH ERRORS A MODEL FOR POLYNUCLEOTIDE REPLICATION ** Jörg SWETINA and Peter SCHUSTER * Janina für Thorenische Chonic and Stehlenchenie der Universität, Währingeräralle 17, A-1090 Wire, Austria Received 4th June 1982

Revised manuscript received 23rd August 1982 Accepted 30th August 1982

Biophysical Chemistry 16 (1982) 329-345 Elsevier Biomedical Press

Key words: Polynucleotide replication; Quasi-species; Point mutation; Mutant class; Stochastic replication

A model for polynucleosite replication is presented and analyzed by means of perturbation theory. Two busic assumptions allow handling of expensions up to action length of r = 80 explicitly, point mutations are retrictive to a it would perturbate and analyzed by the second perturbation theory is in excellent agreement with the exact results for long encough asymptetic (s > 30).

1. Introduction

Eigen [8] proposed a formal kinetic equation (eq. 1) which describes self-replication under the constraint of constant total population size:

 $\frac{dx_i}{dt} = \dot{x}_i = \sum_j w_{ij} x_j - \frac{x_i}{c} \phi; i = 1, ..., n^{\frac{1}{2}}$ (1)

By x_i we denote the population number or concentration of the self-replicating element 1_i , i.e., $x_i = [1,]$. The total population size or total concentration $c = \Sigma_i x_i$ is kept constant by proper adjustment of the constraint $\phi_i = \phi_i \sum_i w_i x_i$. Characteristically, this constraint has been called 'comstant organization'. The relative values of diagonal

 Dedicated to the late Professor B.L. Jones who was among the first to do rigorous mathematical analysis on the problems described here.

•• This paper is considered as part II of Model Studies on RNA replication. Part I is by Gassner and Schuster [14]. All summations throughout this paper run from 1 to *x* unless specified differently: $\Sigma_i = \sum_{i=1}^{n}$ and $\Sigma_{i,i=x_i} = \sum_{i=1}^{n-1} + \sum_{i=x_i=1}^{n}$.

0301-4622/82/0000-0000/\$02.75 © 1982 Elsevier Biomedical Press

 (w_{ii}) and off-diagonal $(w_{ij}, i \neq j)$ rates, as we shall see in detail in section 2, are related to the accuracy of the replication process. The specific properties of eq. 1 are essentially based on the fact that it leads to exponential growth in the absence of constraints (q = 0) and competitors (n = 1).

The non-linear differential equation, eq. 1 – the non-linearity is introduced by the definition of ϕ at constant organization – shows a remarkable feature: it leads to selection of a defined ensemble of self-replicating elements above a certain accuracy threshold. This ensemble of a master and its most frequent mutants is a so-called 'quasi-species' [9]. Below this threshold, however, no selection takes place and the frequencies of the individual elements are determined exclusively by their statistical weights.

Rigorous mathematical analysis has been performed on e.g. 17,15,24,26. In particular, it was shown that the non-linearity of eq. 1 can be removed by an appropriate transformation. The eigenvalue problem of the linear differential equation obtained thereby may be solved approximately by the conventional perturbation technique



Quasispecies as a function of the error rate p

Chain length and error threshold

$$Q \cdot \sigma = (1-p)^n \cdot \sigma \ge 1 \implies n \cdot \ln(1-p) \ge -\ln\sigma$$

$$n \dots \text{ constant} : p_{\text{max}} \approx \frac{\ln \sigma}{n}$$

$$p \dots \text{ constant} : n_{\text{max}} \approx \frac{\ln \sigma}{p}$$

 $Q = (1-p)^{n} \dots \text{ replication accuracy}$ $p \dots \text{ error rate}$ $n \dots \text{ chain length}$ $\sigma = \frac{f_{m}}{\sum_{j \neq m} f_{j}} \dots \text{ superiority of master sequence}$



Chain length: $n = 100 \implies m = 1.6 \times 10^{60}$



The error threshold in replication



Fitness landscapes showing error thresholds

Hamming distance $d_{H}(I_k, I_0)$

24

Mutant class

0

1

2

3

4

5

Binary sequences can be encoded by their decimal equivalents:

C = 0 and G = 1, for example,

"0" = 00000 =**CCCCC**,

 $"14" \equiv 01110 = CGGGC,$

 $"29" \equiv 11101 = GGGCG$, etc.

Every point in sequence space is equivalent

Sequence space of binary sequences with chain length n = 5





Error threshold: Error classes and individual sequences

n = 10 and $\sigma = 2$





Error threshold: Individual sequences $n = 10, \sigma = 2$ and d = 0, 1.0, 1.85



Fitness landscapes **not** showing error thresholds

Hamming distance $d_{H}(I_k,I_0)$





Error thresholds and gradual transitions

n = 20 and $\sigma = 10$

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5' - end

N₁

random individuals. The primer pair used for genomic DNA amplification is 5'-TCTCCCTGGATTCT-CATTTA-3' (forward) and 5'-TCTTTGTCTTCTGT TCCACC-3' (reverse). Reactions were performed in 25 µl using 1 unit of Tag DNA polymerase with each primer at 0.4 µM; 200 µM each dATP, dTTP, dGTP, and dCTP; and PCR buffer [10 mM tris-HCI (pH 8.3) 50 mM KCl₂,1.5 mM MgCl₂] in a cycle condition of 94°C for 1 min and then 35 cycles of 94°C for 30 s. 55°C for 30 s, and 72°C for 30 s followed by 72°C for 6 min. PCR products were purified (Qiagen), digested with Xmn L and senarated in a 2% agarose gel.

- 32. A nonsense mutation may affect mRNA stability and result in degradation of the transcript [L. Maguat, Am. J. Hum. Genet. 59, 279 (1996)]
- 33. Data not shown: a dot blot with poly (A)+ RNA from 50 human tissues (The Human BNA Master Blot. 7770-1, Clontech Laboratories) was hybridized with a probe from exons 29 to 47 of MYO15 using the same condition as Northern blot analysis (13).
- 34. Smith-Magenis syndrome (SMS) is due to deletions of 17p11.2 of various sizes, the smallest of which includes MYO15 and perhaps 20 other genes ((6): K-S Chen, L. Potocki, J. R. Lupski, MRDD Res. Rev. 2 122 (1996)] MYO15 expression is easily detected in the pituitary gland (data not shown). Haploinsufficiency for MYO15 may explain a portion of the SMS

Continuity in Evolution: On the Nature of Transitions

Walter Fontana and Peter Schuster

To distinguish continuous from discontinuous evolutionary change, a relation of nearness between phenotypes is needed. Such a relation is based on the probability of one phenotype being accessible from another through changes in the genotype. This nearness relation is exemplified by calculating the shape neighborhood of a transfer RNA secondary structure and provides a characterization of discontinuous shape transformations in RNA. The simulation of replicating and mutating RNA populations under selection shows that sudden adaptive progress coincides mostly, but not always, with discontinuous shape transformations. The nature of these transformations illuminates the key role of neutral genetic drift in their realization.

A much-debated issue in evolutionary biology concerns the extent to which the history of life has proceeded gradually or has been punctuated by discontinuous transitions at the level of phenotypes (1). Our goal is to make the notion of a discontinuous transition more precise and to understand how it arises in a model of evolutionary adaptation.

We focus on the narrow domain of RNA secondary structure, which is currently the simplest computationally tractable, yet realistic phenotype (2). This choice enables the definition and exploration of concepts that may prove useful in a wider context. RNA secondary structures represent a coarse level of analysis compared with the three-dimensional structure at atomic resolution. Yet, secondary structures are empir-

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ically well defined and obtain their biophysical and biochemical importance from being a scaffold for the tertiary structure. For the sake of brevity, we shall refer to secondary structures as "shapes." RNA combines in a single molecule both genotype (replicatable sequence) and phenotype (selectable shape), making it ideally suited for in vitro evolution experiments (3, 4).

phenotype such as short stature. Moreover, a few

SMS natients have sensorineural hearing loss, pos-

sibly because of a point mutation in MYO15 in trans

X-7 Liu et al ihid 17 268 (1997): E Gibson et al

vrinths) obtained from human fetuses at 18 to 22

weeks of development in accordance with guidelines

established by the Human Research Committee at

the Brigham and Women's Hospital. Only samples

without evidence of degradation were pooled for

poly (A)* selection over oligo(dT) columns. First-

strand cDNA was prepared using an Advantage RT-

for-PCR kit (Clontech Laboratories). A portion of the

first-strand cDNA (4%) was amplified by PCR with

Advantage cDNA polymerase mix (Clontech Labora-

tories) using human MYO15-specific oligonucleotide

primers (forward, 5'-GCATGACCTGCCGGCTAAT

GGG-3': reverse, 5'-CTCACGGCTTCTGCATGGT-

GCTCGGCTGGC-3'). Cycling conditions were 40 s

at 94°C; 40 s at 66°C (3 cycles), 60°C (5 cycles), and

55°C (29 cycles); and 45 s at 68°C. PCB products

were visualized by ethidium bromide staining after

fractionation in a 1% agarose gel. A 688-bp PCR

Nature 374, 62 (1995): D. Weil et al. ibid. p. 60.

37. RNA was extracted from cochlea (membranous lab

36. K. B. Avraham et al., Nature Genet. 11, 369 (1995);

to the SMS 17n11.2 deletion.

35. R. A. Fridell, data not shown

To generate evolutionary histories, we used a stochastic continuous time model of an RNA population replicating and mutating in a capacity-constrained flow reactor under selection (5, 6). In the laboratory, a goal might be to find an RNA aptamer binding specifically to a molecule (4). Although in the experiment the evolutionary end product was unknown, we thought of its shape as being specified implicitly by the imposed selection criterion. Because our intent is to study evolutionary histories rather than end products, we defined a target shape in advance and assumed the replication rate of a sequence to be a function of because, in contrast to sequences, there are

product is expected from amplification of the human MYO15 cDNA. Amplification of human genomic DNA with this primer pair would result in a 2903-bp fragment

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the similarity between its shape and the target. An actual situation may involve more than one best shape, but this does not affect our conclusions.

An instance representing in its qualitative features all the simulations we performed is shown in Fig. 1A. Starting with identical sequences folding into a random shape, the simulation was stopped when the population became dominated by the target, here a canonical tRNA shape. The black curve traces the average distance to the target (inversely related to fitness) in the population against time. Aside from a short initial phase, the entire history is dominated by steps, that is, flat periods of no apparent adaptive progress, interrupted by sudden approaches toward the target structure (7). However, the dominant shapes in the population not only change at these marked events but undergo several fitness-neutral transformations during the periods of no apparent progress. Although discontinuities in the fitness trace are evident, it is entirely unclear when and on the basis of what the series of successive phenotypes itself can be called continuous or discontinuous.

A set of entities is organized into a (topological) space by assigning to each entity a system of neighborhoods. In the present case, there are two kinds of entities: sequences and shapes, which are related by a thermodynamic folding procedure. The set of possible sequences (of fixed length) is naturally organized into a space because point mutations induce a canonical neighborhood. The neighborhood of a sequence consists of all its one-error mutants. The problem is how to organize the set of possible shapes into a space. The issue arises

Evolution *in silico*

W. Fontana, P. Schuster, Science 280 (1998), 1451-1455



Replication rate constant:

$$f_{k} = \gamma / [\alpha + \Delta d_{S}^{(k)}]$$
$$\Delta d_{S}^{(k)} = d_{H}(S_{k}, S_{\tau})$$

Selection constraint:

Population size, N = # RNA molecules, is controlled by the flow

$$N(t) \approx \overline{N} \pm \sqrt{\overline{N}}$$

Mutation rate:

 $p = 0.001 / site \times replication$

The flowreactor as a device for **studies** of evolution *in vitro* and *in silico*







Phenylalanyl-tRNA as target structure



In silico optimization in the flow reactor: Evolutionary Trajectory



28 neutral point mutations during a long quasi-stationary epoch

GGUAUGGGCGUUGAAUAGUAGGGUUUAAACCAAUCGGCCAACGAUCUCGUGUGCGCAUUUCAUAUCCCGUACAGAA entry 8 GGUAUGGGCGUUGAAUAAUAGGGUUUAAAACCAAUCGGCCAACGAUCUCGUGUGCGCAUUUCAUAUGCCAUACAGAA exit GGUAUGGGCGUUGAAUAAUAGGGUUUAAACCAAUCGGCCAACGAUCUCGUGUGCGCAUUUCAUAUACCAUACAGAA entry 9 exit entrv 10exit

Transition inducing point mutations change the molecular structure

Neutral point mutations leave the molecular structure unchanged

Neutral genotype evolution during phenotypic stasis

From sequences to shapes and back: a case study in RNA secondary structures

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SUMMARY

RNA folding is viewed here as a map assigning secondary structures to sequences. At fixed chain length the number of sequences far exceeds the number of structures. Frequencies of structures are highly nonuniform and follow a generalized form of Zipf's law: we find relatively few common and many rare ones. By using an algorithm for inverse folding, we show that sequences sharing the same structure are distributed randomly over sequence space. All common structures can be accessed from an arbitrary sequence by a number of mutations much smaller than the chain length. The sequence space is percolated by extensive neutral networks connecting nearest neighbours folding into identical structures. Implications for evolutionary adaptation and for applied molecular evolution are evident: finding a particular structure by mutation and selection is much simpler than expected and, even if catalytic activity should turn out to be sparse in the space of RNA structures, ica n hardly be missed by evolutionary processes.

1. INTRODUCTION

Folding sequences into structures is a central problem in biopolymer research. Both robustness and accessibility of structures, as functions of mutational change in the underlying sequence, are crucial to both natural and applied molecular evolution. Test-tube evolution experiments are based on properties of RNA molecules: as sequences they are genotypes, and as spatial structures they are phenotypes (Spiegelman 1971; Biebricher 1983). Our concern is the mapping from RNA sequences into structures being the simplest, and the only tractable, example of a genotype-phenotype mapping.

An RNA sequence is a point in the space of all 4^n sequences with fixed length n. This space has a natural metric induced by point mutations interconverting sequences known as the Hamming distance (Hamming 1950, 1986). The folding process considered here maps an RNA sequence into a secondary structure (figure 1a) minimizing free energy. A secondary structure is tantamount to a list of Watson-Crick type and GU base pairs, and can be represented as a tree graph (figure 1b). This emphasizes the combinatorial nature of secondary structures and allows for a canonical distance measure between structures (Tai 1979). Assuming elementary edit operations with pre-defined costs, such as deletion, insertion and relabelling of nodes, the distance between two trees is given by the smallest sum of the edit costs along any path that converts one tree into the other (Sankoff & Kruskal 1983).

An approximate upper bound on the number of minimum free-energy structures (of fixed chain length n) can be obtained along the lines devised by Stein & Waterman (1978). Counting only those planar secondary structures that contain hairpin loops of size three or more (steric constraint), and that contain no isolated base pairs (stacks of two or more pairs are essentially the only stabilizing elements), one finds:

$S_n = 1.4848 \times n^{-\frac{3}{2}} (1.8488)^n$

which is consistently smaller than the number of sequences.

Folding can thus be viewed as a map between two metric spaces of combinatorial complexity, a sequence space and a shape space. (The notion of shape space was originally used in theoretical immunology in a similar context by Perelson & Oster (1979).) 'Shape' refers to a discretized (and hence coarse-grained) structure representation, such as the secondary structures or the tree graphs used here. The notion of secondary structure is but one among a spectrum of possible levels of resolution that can be used to define shape. It discards atomic coordinates, as well as the relative spatial orientation of the structural elements, taking into account only their number, size and relative connectedness. Nevertheless, secondary structure is a major component of whatever turns out to be an adequate shape definition for RNA: it covers the dominant part of the three-dimensional folding energies, very often it can be used successfully in the interpretation of function and reactivity, and it is frequently conserved in evolution (Sankoff et al. 1978;



Figure 4. Neutral paths. A neutral path is defined by a series of nearest neighbour sequences that fold into identical structures. Two classes of nearest neighbours are admitted: neighbours of Hamming distance 1, which are obtained by single base exchanges in unpaired stretches of the structure, and neighbours of Hamming distance 2, resulting from base pair exchanges in stacks. Two probability densities of Hamming distances are shown that were obtained by searching for neutral paths in sequence space: (i) an upper bound for the closest approach of trial and target sequences (open circles) obtained as endpoints of neutral paths approaching the target from a random trial sequence (185 targets and 100 trials for each were used); (ii) a lower bound for the closest approach of trial and target sequences (open diamonds) derived from secondary structure statistics (Fontana et al. 1993a; see this paper, §4); and (iii) longest distances between the reference and the endpoints of monotonously diverging neutral paths (filled circles) (500 reference sequences were used).

279

- 1. Darwinsche Evolution
- 2. Evolutionsexperimente mit Molekülen
- 3. Replikation, Mutation und Fitnesslandschaften
- 4. Evolution *in silico*
- 5. Neutrale Evolution
- 6. Multistabilität und RNA-Schalter



Evolutionary trajectory

Spreading of the population on neutral networks

Drift of the population center in sequence space

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_	





























A sketch of optimization on neutral networks
- 1. Darwinsche Evolution
- 2. Evolutionsexperimente mit Molekülen
- 3. Replikation, Mutation und Fitnesslandschaften
- 4. Evolution *in silico*
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The compatible set C_k of a structure S_k consists of all sequences which form S_k as its minimum free energy structure (the neutral network G_k) or one of its suboptimal structures.



The intersection of two compatible sets is always non empty: $\mathbf{C}_0 \cap \mathbf{C}_1 \notin \emptyset$



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GENERIC PROPERTIES OF COMBINATORY MAPS: NEUTRAL NETWORKS OF RNA SECONDARY STRUCTURES¹

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Random graph theory is used to model and analyse the relationships between sequences and secondary structures of RNA molecules, which are understood as mappings from sequence space into shape space. These maps are non-invertible since there are always many orders of magnitude more sequences than structures. Sequences folding into identical structures form neutral networks. A neutral network is embedded in the set of sequences that are compatible with the given structure. Networks are modeled as graphs and constructed by random choice of vertices from the space of compatible sequences. The theory characterizes neutral networks by the mean fraction of neutral neighbors (λ). The networks are connected and percolate sequence space if the fraction of neutral nearest neighbors exceeds a threshold value $(\lambda > \lambda^*)$. Below threshold $(\lambda < \lambda^*)$, the networks are partitioned into a largest "giant" component and several smaller components. Structures are classified as "common" or "rare" according to the sizes of their pre-images, i.e. according to the fractions of sequences folding into them. The neutral networks of any pair of two different common structures almost touch each other, and, as expressed by the conjecture of shape space covering sequences folding into almost all common structures, can be found in a small ball of an arbitrary location in sequence space. The results from random graph theory are compared to data obtained by folding large samples of RNA sequences. Differences are explained in terms of specific features of RNA molecular structures. © 1997 Society for Mathematical Biology

THEOREM 5. INTERSECTION-THEOREM. Let s and s' be arbitrary secondary structures and C[s], C[s'] their corresponding compatible sequences. Then,

$C[s] \cap C[s'] \neq \emptyset.$

Proof. Suppose that the alphabet admits only the complementary base pair [XY] and we ask for a sequence x compatible to both s and s'. Then $j(s, s') \cong D_m$ operates on the set of all positions $\{x_1, \ldots, x_n\}$. Since we have the operation of a dihedral group, the orbits are either cycles or chains and the cycles have even order. A constraint for the sequence compatible to both structures appears only in the cycles where the choice of bases is not independent. It remains to be shown that there is a valid choice of bases for each cycle, which is obvious since these have even order. Therefore, it suffices to choose an alternating sequence of the pairing partners X and Y. Thus, there are at least two different choices for the first base in the orbit.

Remark. A generalization of the statement of theorem 5 to three different structures is false.

> Reference for the definition of the intersection and the proof of the **intersection theorem**



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An RNA switch



J1LH barrier tree

A ribozyme switch

E.A.Schultes, D.B.Bartel, Science **289** (2000), 448-452

minus the background levels observed in the HSP in the control (Sar1-GDP-containing) incubation that prevents COPII vesicle formation. In the microsome control, the level of p115-SNARE associations was less than 0.1%.

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REPORTS

X-100 for 15 min at 4°C with intermittent mixing, and elutes were pooled. Proteins were precipitated by MeOH/CH₃Cl and separated by SDS-polyacrylamide gel electrophoresis (PAGE) followed by immunoblotting using p115 mAb 13F12.

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One Sequence, Two Ribozymes: Implications for the Emergence of New Ribozyme Folds

Erik A. Schultes and David P. Bartel*

We describe a single RNA sequence that can assume either of two ribozyme folds and catalyze the two respective reactions. The two ribozyme folds share no evolutionary history and are completely different, with no base pairs (and probably no hydrogen bonds) in common. Minor variants of this sequence are highly active for one or the other reaction, and can be accessed from prototype ribozymes through a series of neutral mutations. Thus, in the course of evolution, new RNA folds could arise from preexisting folds, without the need to carry inactive intermediate sequences. This raises the possibility that biological RNAs having no structural or functional similarity might share a common ancestry. Furthermore, functional and structural divergence might, in some cases, precede rather than follow gene duplication.

Related protein or RNA sequences with the same folded conformation can often perform very different biochemical functions, indicating that new biochemical functions can arise from preexisting folds. But what evolutionary mechanisms give rise to sequences with new macromolecular folds? When considering the origin of new folds, it is useful to picture, among all sequence possibilities, the distribution of sequences with a particular fold and function. This distribution can range very far in sequence space (1). For example, only seven nucleotides are strictly conserved among the group I selfsplicing introns, yet secondary (and presumably tertiary) structure within the core of the ribozyme is preserved (2). Because these disparate isolates have the same fold and function, it is thought that they descended from a common ancestor through a series of mutational variants that were each functional. Hence, sequence heterogeneity among divergent isolates implies the existence of paths through sequence space that have allowed neutral drift from the ancestral sequence to each isolate. The set of all possible neutral paths composes a "neutral network," connecting in sequence space those widely dispersed sequences sharing a particular fold and activity, such that any sequence on the network can potentially access very distant sequences by neutral mutations (3–5).

Theoretical analyses using algorithms for predicting RNA secondary structure have suggested that different neutral networks are interwoven and can approach each other very closely (3, 5–8). Of particular interest is whether ribozyme neutral networks approach each other so closely that they intersect. If so, a single sequence would be capable of folding into two different conformations, would M. R. Peterson, C. G. Burd, S. D. Emr, Curr. Biol. 9, 159 (1999).

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have two different catalytic activities, and could access by neutral drift every sequence on both networks. With intersecting networks, RNAs with novel structures and activities could arise from previously existing ribozymes, without the need to carry nonfunctional sequences as evolutionary intermediates. Here, we explore the proximity of neutral networks experimentally, at the level of RNA function. We describe a close apposition of the neutral networks for the hepatitis delta virus (HDV) self-cleaving ribozyme and the class III self-ligating ribozyme.

In choosing the two ribozymes for this investigation, an important criterion was that they share no evolutionary history that might confound the evolutionary interpretations of our results. Choosing at least one artificial ribozyme ensured independent evolutionary histories. The class III ligase is a synthetic ribozyme isolated previously from a pool of random RNA sequences (9). It joins an oligonucleotide substrate to its 5' terminus. The prototype ligase sequence (Fig. 1A) is a shortened version of the most active class III variant isolated after 10 cycles of in vitro selection and evolution. This minimal construct retains the activity of the full-length isolate (10). The HDV ribozyme carries out the site-specific self-cleavage reactions needed during the life cycle of HDV, a satellite virus of hepatitis B with a circular, single-stranded RNA genome (11). The prototype HDV construct for our study (Fig. 1B) is a shortened version of the antigenomic HDV ribozvme (12), which undergoes self-cleavage at a rate similar to that reported for other antigenomic constructs (13, 14).

The prototype class III and HDV ribozymes have no more than the 25% sequence identity expected by chance and no fortuitous structural similarities that might favor an intersection of their two neutral networks. Nevertheless, sequences can be designed that simultaneously satisfy the base-pairing requirements

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Two ribozymes of chain lengths n = 88 nucleotides: An artificial ligase (A) and a natural cleavage ribozyme of hepatitis- δ -virus (B)



The sequence at the *intersection*:

An RNA molecules which is 88 nucleotides long and can form both structures



Two neutral walks through sequence space with conservation of structure and catalytic activity

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