

Refining Knowledge Based Potentials of Proteins

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WHY?

- Finding errors in empirically obtained 3-d structures
- Predicting effects of aa mutation on structure
- Inverse folding: structure \Rightarrow sequence
- Ultimately: sequence \Rightarrow structure

“Physical” potential field Amber

$$\begin{aligned}
 E_{\text{total}} = & \sum_{\text{bonds}} K_r (r - r_{eq})^2 + \\
 & + \sum_{\text{angles}} K_\theta (\theta - \theta_{eq})^2 + \\
 & + \sum_{\text{dihedrals}} \frac{V_n}{2} [1 + \cos(n\phi - \gamma)] + \\
 & + \sum_{i < j} \left[\frac{A_{ij}}{R_{ij}^{12}} - \frac{B_{ij}}{R_{ij}^6} + \frac{q_i q_j}{\epsilon R_{ij}} \right] + \\
 & + \sum_{\text{H-bonds}} \left[\frac{C_{ij}}{R_{ij}^{12}} - \frac{D_{ij}}{R_{ij}^{10}} \right]
 \end{aligned}$$

Knowledge based Potentials

Using Boltzmann's Principle:

Frequently observed states correspond to low energy states

Sippl

$$E_{\text{total}} = \sum_{a < b, s} -kT \ln \left[\frac{f_{(r)}^{abs}}{f_{(r)}^s} \right]$$

Tropsha

$$E_{\text{total}} = \sum_{\text{quadruples}} q_{ijkl}$$

Possible Problems

'Physical' Potential Field

- Vast energy landscape
- Rugged energy landscape

Knowledge based potential

- Size of Database
- Reliability of Database

Sippl's Approach

Pair interactions depending on:

- type of amino acids a, b
- type of atom c, d
- distance in sequence between a, b : k
- spatial separation of a, b : r

r is a continuous variable \longrightarrow intervalls

$$\Rightarrow f_r^{abcdk}$$

redundant information \longrightarrow reference state:

$$f_r^{cdk}$$

$$\begin{aligned}\Delta E_r^{abcdk} &= E_r^{abcdk} - E_r^{cdk} = \\ &= -kT \ln \left(\frac{f_r^{abcdk}}{f_r^{cdk}} \right)\end{aligned}$$

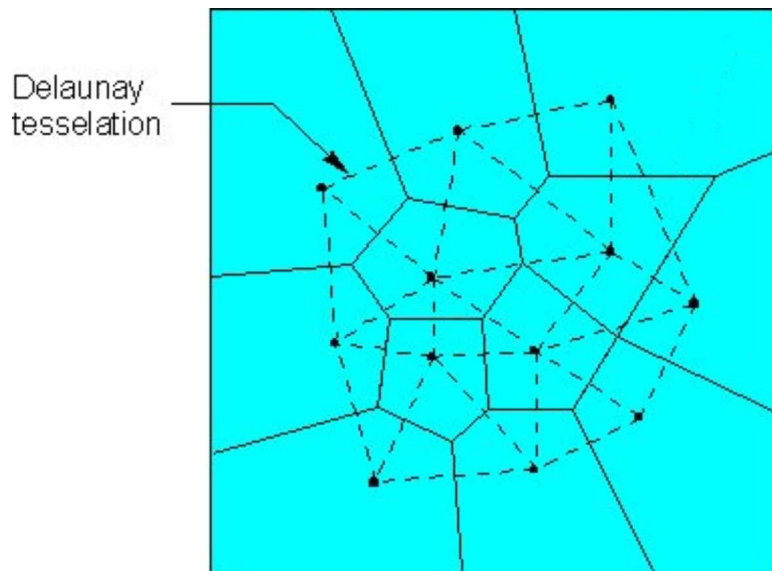
Tropsha's Approach

Filling protein space with tetrahedra

$$E_{\text{total}} = \sum_{\text{tetrahedra}} \log \left(\frac{f_{ijkl}}{p_{ijkl}} \right)$$

$$p_{ijkl} = C a_i a_j a_k a_l$$

Delaunay Triangulation



2 Dimensions: Triangles vertices i, j, k

3 Dimensions: Tetrahedra vertices i, j, k, l

C_α as vertices

Expanding Tropsha's Potential

$$\begin{aligned}
 \sum_{\text{tetrahedras}} q_{ijkl} &= \sum_{aa} q_{aa} + \\
 &+ \sum_{\text{pairs}} q_{pairs} | (q_{aa1}, q_{aa2}) + \\
 &+ \sum_{\text{triangles}} q_{trian} | (q_{pair1}, q_{pair2}, q_{pair3}) + \\
 &+ \sum_{\text{4-tupel}} q_{tetra} | (q_{triangle1}, q_{tr2}, q_{tr3}, q_{tr4})
 \end{aligned}$$

$$\begin{aligned}
 q_{pair_{ab}} | (q_a, q_b) &= \frac{f_{pair_{ab}}}{p_{pair_{ab}} | (p_a, p_b)} \\
 p_{pair_{ab}} | p_a, p_b &= a p_a p_b
 \end{aligned}$$

$$\begin{aligned}
 q_{abc} | (q_{ab}, q_{ac}, q_{bc}) &= \frac{f_{triangle_{abc}}}{p_{triangle_{abc}} | (p_{ab}, p_{ac}, p_{bc})} \\
 p_{triangle_{abc}} | (p_{ab}, p_{ac}, p_{bc}) &= a p_{ab} p_{ac} p_{bc} p_{triangle} \\
 p_{triangle} &= N_{triangles} / N_{triples}
 \end{aligned}$$

Tesselated Protein with Water Shell

