

# Modeling RNA-RNA Interaction Kinetics

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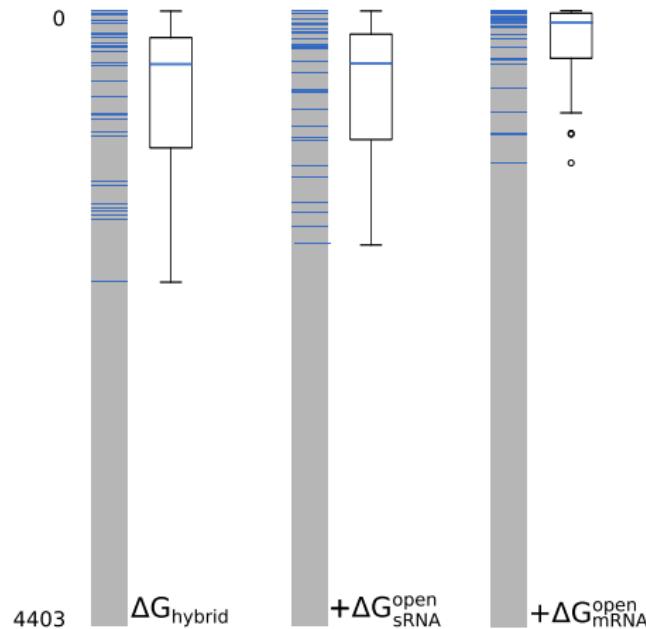
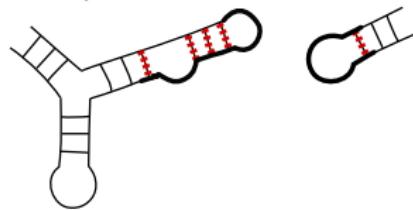
Bled, February 12th, 2020

# RNA-RNA interaction prediction - thermodynamic

►  $\Delta G_{\text{hybrid}}$



►  $\Delta G_{\text{open}}$



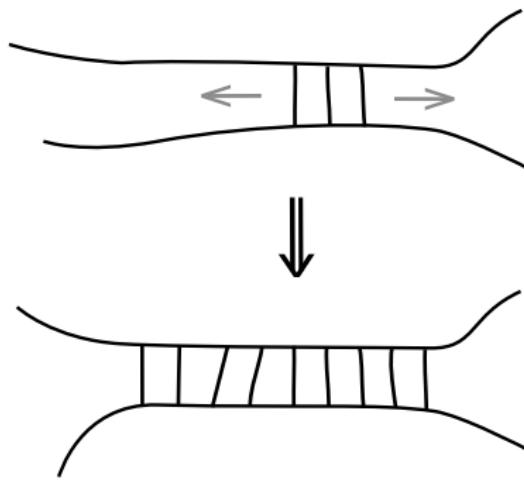
4403

$\Delta G_{\text{hybrid}}$

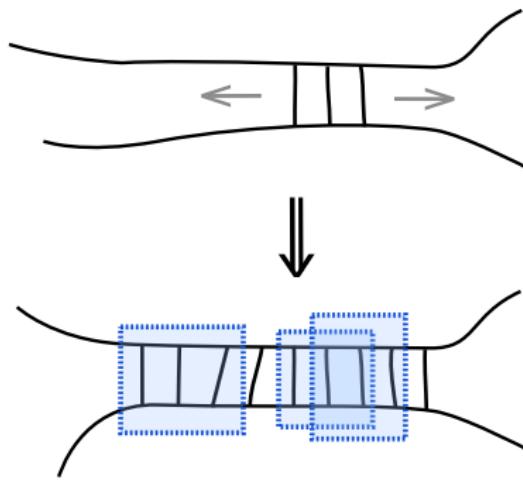
$+\Delta G_{\text{sRNA}}^{\text{open}}$

$+\Delta G_{\text{mRNA}}^{\text{open}}$

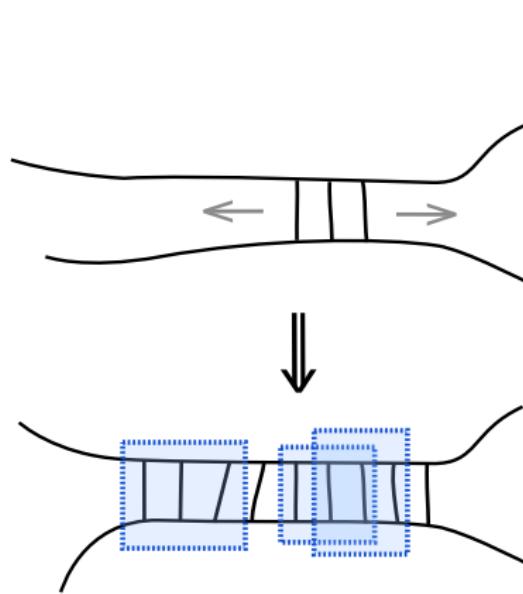
# Interaction formation process



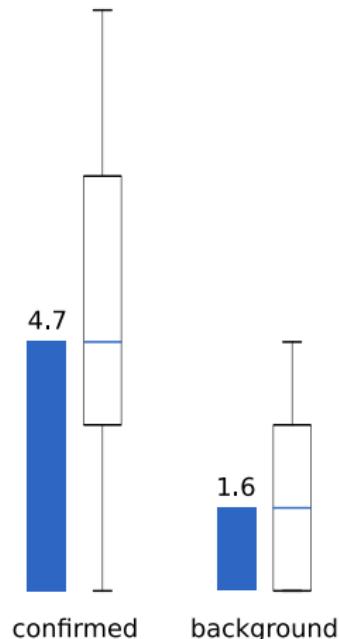
# Interaction formation process



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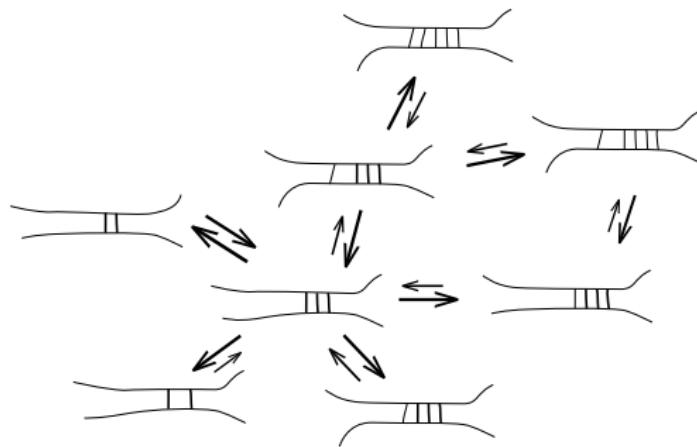
# seeds of length 7



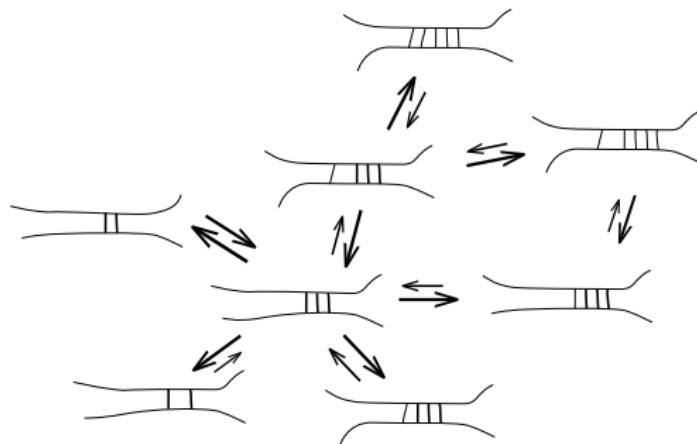
41 experimentally confirmed interactions in *E. coli*

20 randomized background interactions per confirmed interaction (same  $E_{\text{therm}}$ )

# Interaction kinetics



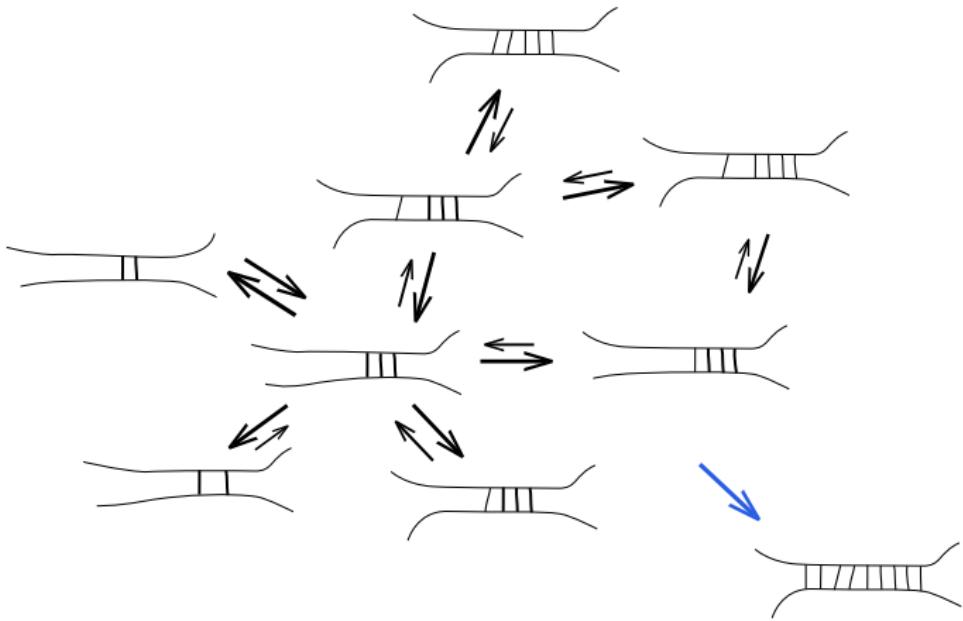
# Interaction kinetics



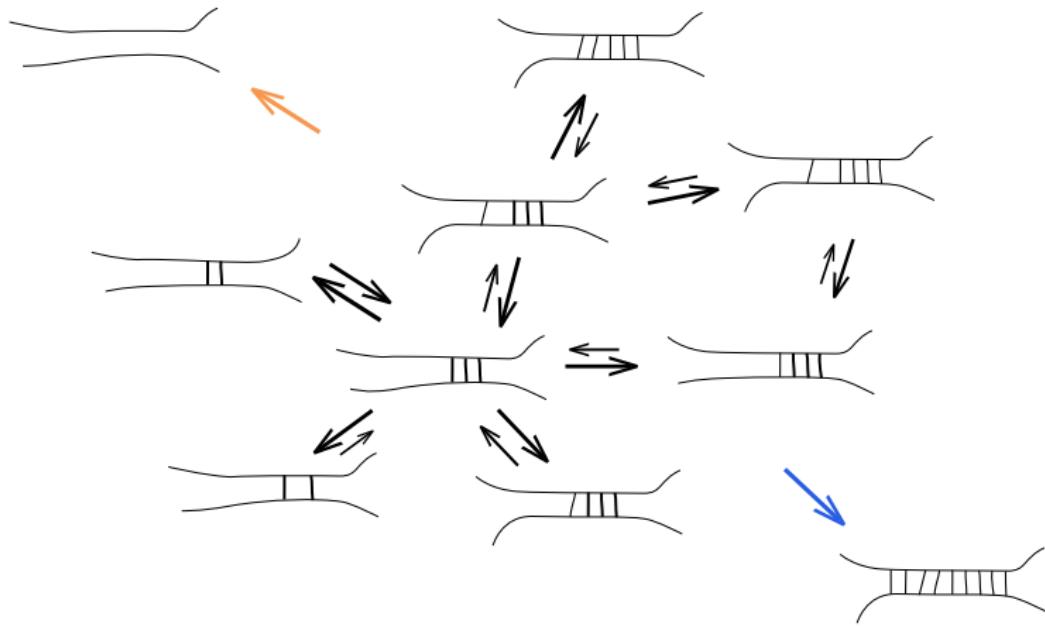
- set of structures/states  $\Omega$
- move set  $M$
- energy function  $E$
- $\Rightarrow$  folding rate  $k_{ij}$

$$k_{ij} = \begin{cases} k_0 & \text{if } \Delta G^\ddagger \leq 0, \\ k_0 e^{-\frac{\Delta G^\ddagger}{RT}} & \text{otherwise} \end{cases}$$

$$\frac{P_i(t)}{dt} = \sum_{i \neq j} (P_j(t)k_{ji} - P_i(t)k_{ij})$$

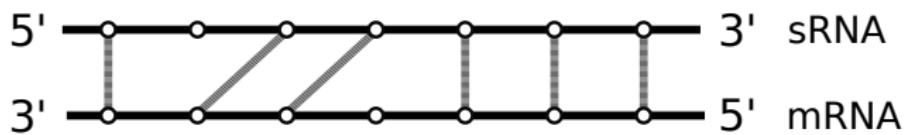


How fast does the full duplex form?  
Dissociation before full duplex?



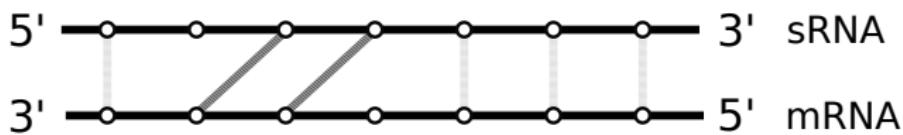
How fast does the full duplex form?  
Dissociation before full duplex?

## Direct folding paths



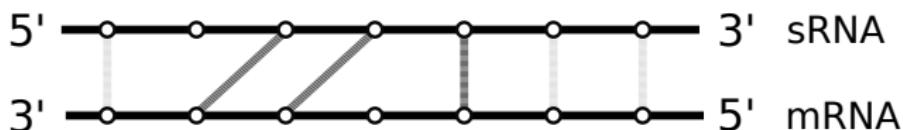
$$B_s(k, l) = \min \begin{cases} \max \begin{cases} E(k, l) \\ B_s(k+1, l) \end{cases} & \text{if } k < s \\ \max \begin{cases} E(k, l) \\ B_s(k, l-1) \end{cases} & \text{if } l > s \\ E(s, s) & \text{if } s = k = l \end{cases}$$

## Direct folding paths



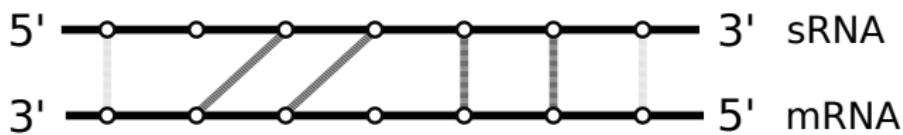
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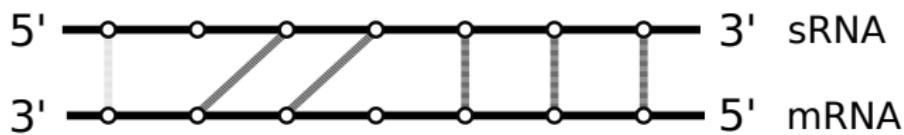
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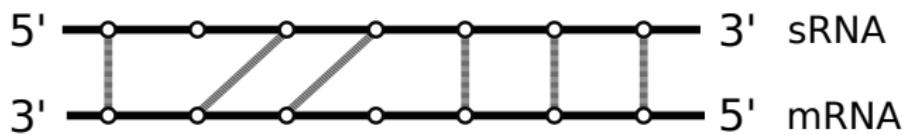
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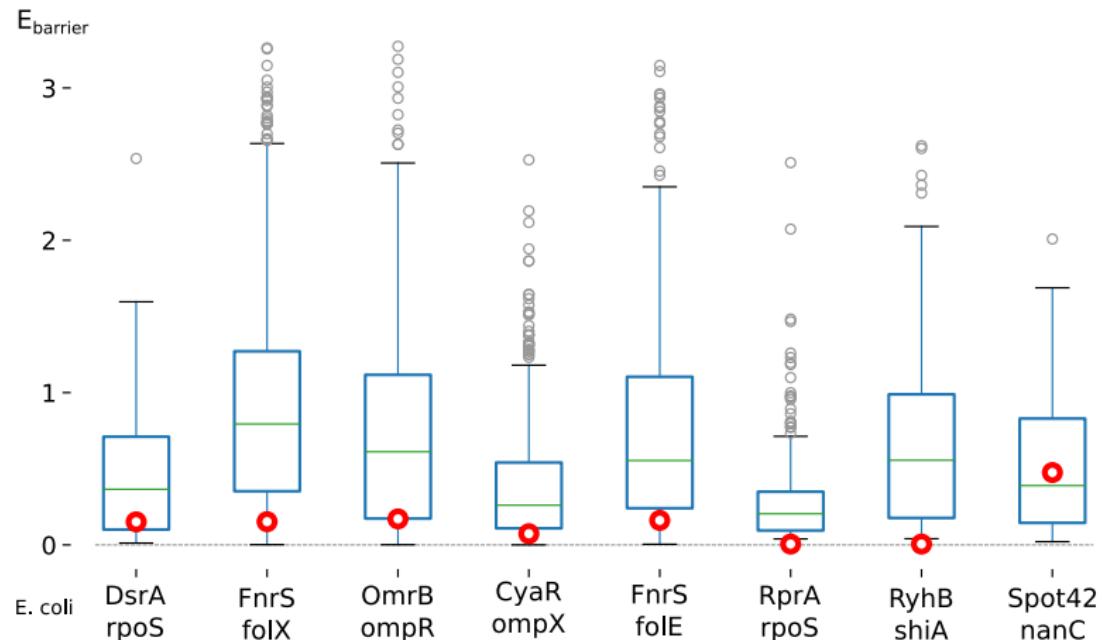
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## Direct folding paths



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# Energy barrier: confirmed interactions vs. randomized background



# Exact kinetics on reduced state space

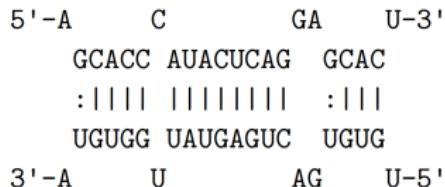
mRNA: ptsG

5'-A        C            GA        U-3'  
GCACC AUACUCAG GCAC  
:||||| |||||||| :|||  
UGUGG UAUGAGUC UGUG  
3'-A        U            AG        U-5'

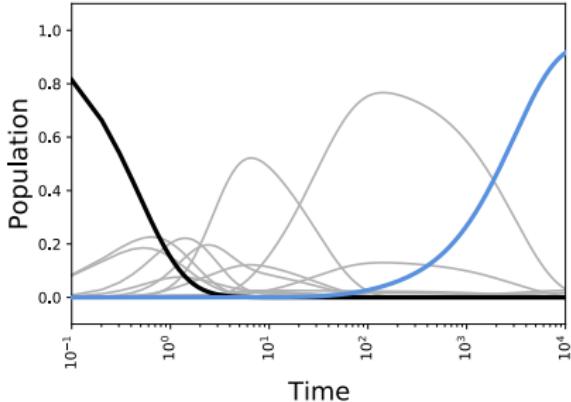
sRNA: SgrS

# Exact kinetics on reduced state space

mRNA: ptsG

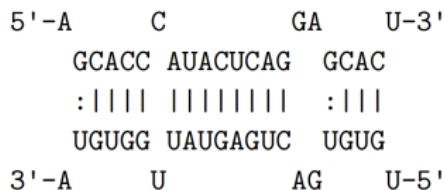


sRNA: SgrS

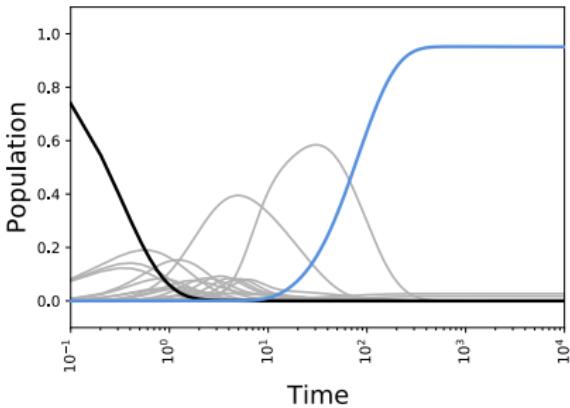
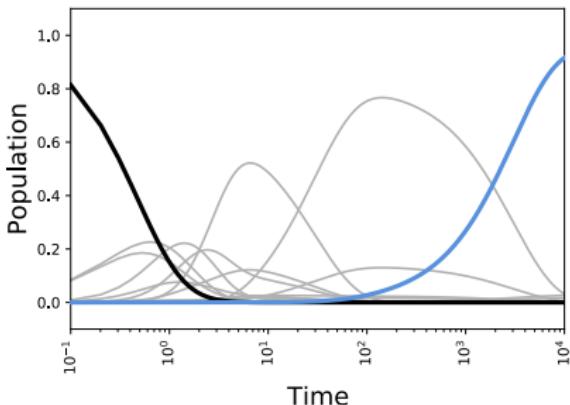


# Exact kinetics on reduced state space

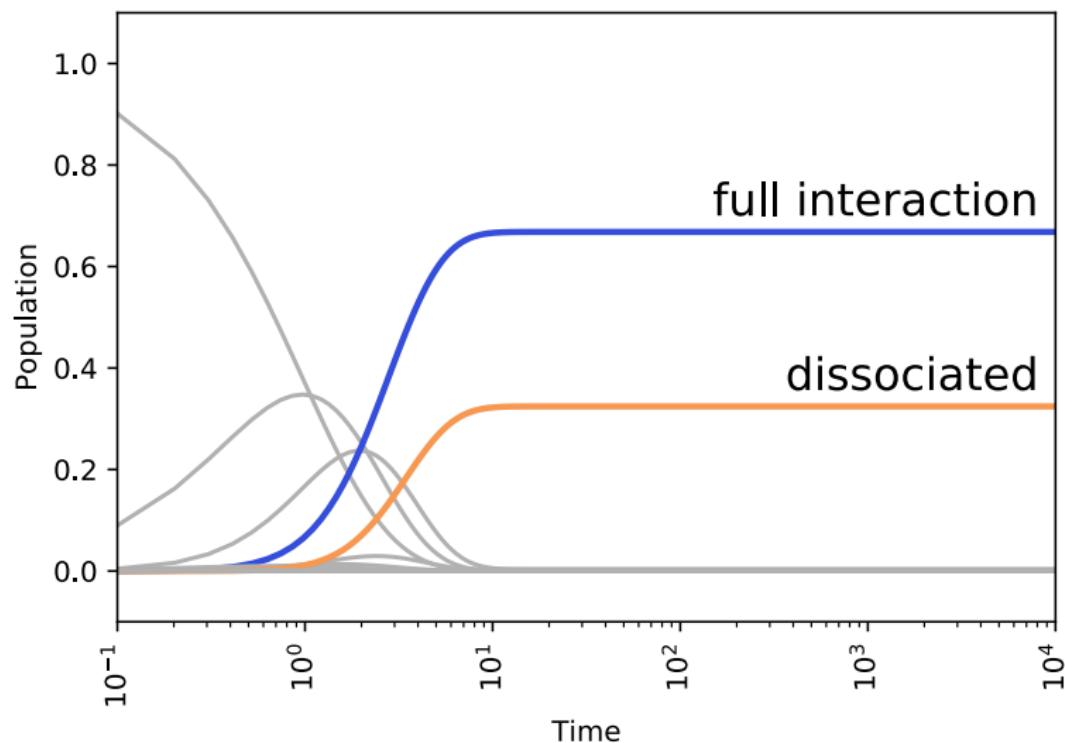
mRNA: ptsG



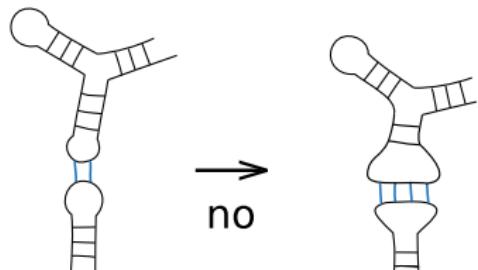
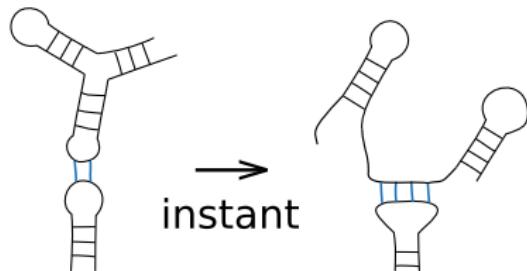
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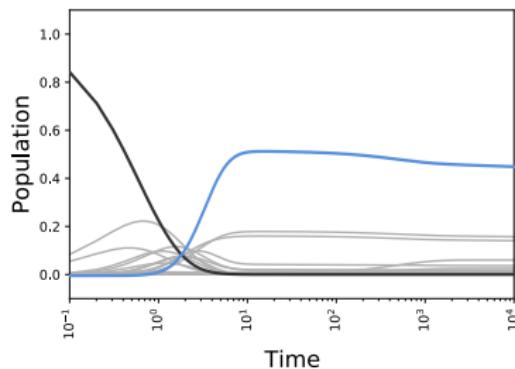
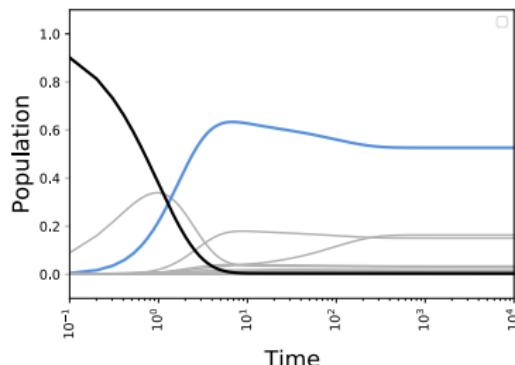
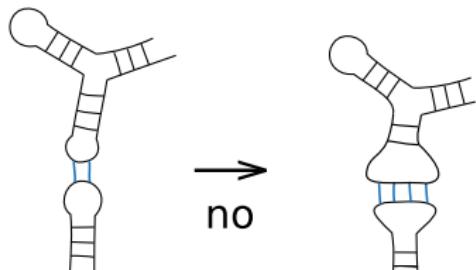
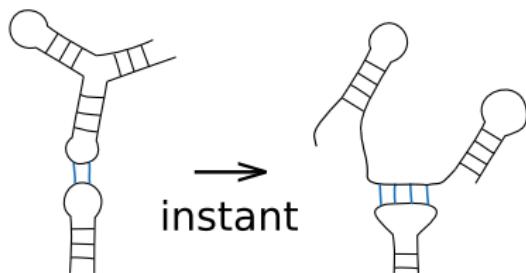
# Probability of dissociation before full interaction is formed



# Energy model - intramolecular refolding



# Energy model - intramolecular refolding



ArcZ, rpoS, seed 1

## RNA-RNA interaction formation process

- ▶ mechanistic hypotheses
- ▶ identify kinetic features
- ▶ benchmark data set and background models
- ▶ efficient computation methods for kinetic features
- ▶ extend and improve interaction prediction method

## THANKS TO ...

- ▶ Irene, Sebastian, Ivo
- ▶ TBI team
- ▶ Martin Raden, Rolf Backofen
- ▶ You!

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universität  
wien



# Direct Paths Recursion

$$B_s(k, l) = \min \begin{cases} \max \begin{cases} E(k, l) \\ B_s(k + 1, l) \end{cases} & \text{if } k < s \\ \max \begin{cases} E(k, l) \\ B_s(k, l - 1) \end{cases} & \text{if } l > s \\ E(s, s) & \text{if } s = k = l \end{cases}$$

$$E(k, l) = E^{\text{hybrid}}(k, l) + E^{\text{unpaired}}(k, l)$$

$$E^{\text{hybrid}}(k, l) = \min \begin{cases} E^{\text{hybrid}}(k + 1, l) + L(k, k + 1) & \text{if } k < l \\ E_{\text{init}} & \text{if } k = l \end{cases}$$