Modeling Evolution of Molecules New Variations of an Old Theme

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Minisymposium on Evolutionary Dynamics

Utrecht, 05.03.2008

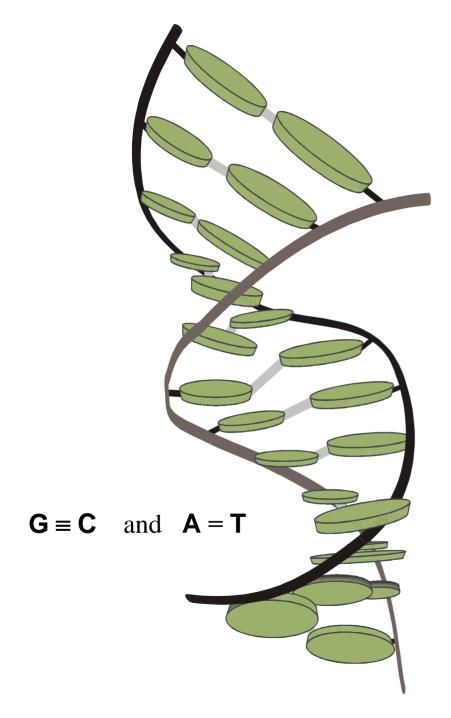
Web-Page for further information:

http://www.tbi.univie.ac.at/~pks

- 1. Replication and mutation
- 2. Quasispecies and error thresholds
- 3. Fitness landscapes and randomization
- 4. Lethal mutations
- 5. Ruggedness of natural landscapes
- 6. Simulation of stochastic phenomena

1. Replication and mutation

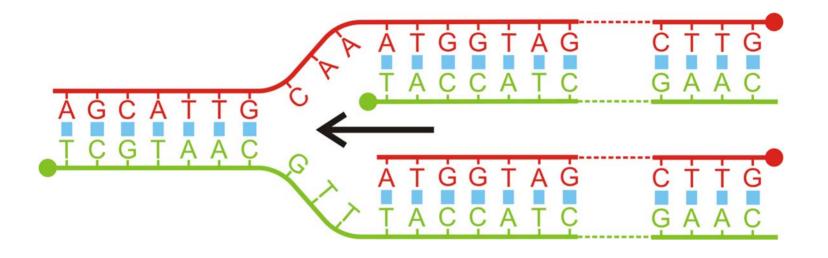
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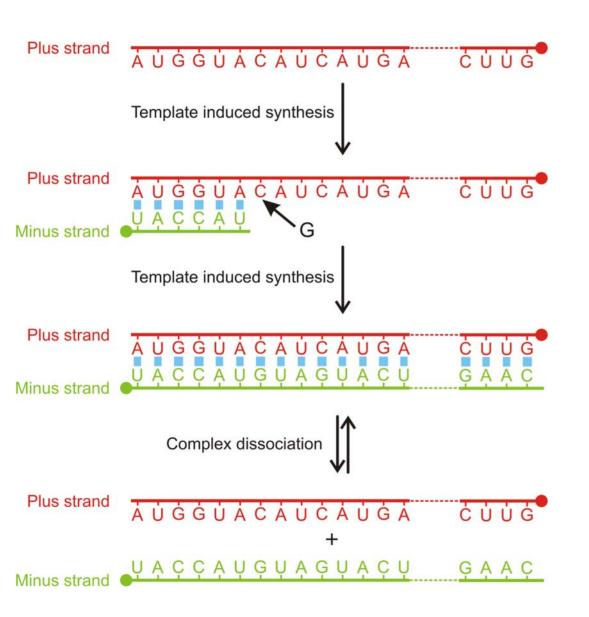
James D. Watson, 1928-, and Francis Crick, 1916-2004, Nobel Prize 1962

The three-dimensional structure of a short double helical stack of B-DNA



,Replication fork' in DNA replication

The mechanism of DNA replication is ,semi-conservative'



Complementary replication is the simplest copying mechanism of RNA.

Complementarity is determined by Watson-Crick base pairs:

G≡C and A=U

DIE NATURWISSENSCHAFTEN

Selforganization of Matter and the Evolution of Biological Macromolecules

MANERED EDIEM*

Max-Planck-Institut für Biophysikalische Chemie Karl-Friedrich-Bonhoeffer-Institut, Göttingen-Nikolausberg

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I. Introduction

I.I. "Cause and Effect"

The question about the origin of life often appears as a In equestion about the origin of life orient appears are question about "cause and effect". Physical theories of macroscopic processes usually involve answers to such usustions, even if a statistical interpretation is given to the relation between "cause" and "effect". In similarly due to the nature of this question that many scientists believe that our present physics does not often any obvious explanation for the existence of life.

* Partily presented as the "Robbins Lectures" at Pomona College, California, in spring 1970.

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which even in its simplest forms always appears to be associated with complex macroscopic fi.e. multimolec-

associated with complex macroscopic (i.e. multimolec-ular) systems, such as the living cell.

As a consequence of the exciting discoveries of "molecular biology": a common version of the above question is: Which casee first, the pressive or the susclein self — a modern variant of the old "chickees-and-the-egg" problem. The term "first is usually meant to define a causal rather than a temporal relabsociation, and define a causal rather than a temporar relationship, and the words "protein" and "suckeic acid" may be sub-stituted by "inction" and "information". The question in this form, when applied to the interplay of nucleic acids and proteins as presently esconsistered in the living cell, leads ad absurdum, because "function"

Die Naturwissenschaften

64. Jahrgang Heft 11 November 1977

The Hypercycle

A Principle of Natural Self-Organization

Part A: Emergence of the Hypercycle

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This paper is the first part of a trilogy, which comprises a detailed study of a special type of functional regardation and demensionals in relevance with respect to the origin and evolution of life. Self-replicative macromolecules, such as RNA or DNA in a suitable environment exhibit a behavior, which we gay cell Darwinian and which can be formally represented by the concept of the quasi-species. A quasi-species is defined as a given distribution of macromolecular species with closely interrelated sequences, dominated by one or several degenerate) master copies. External constraints enforce the selection of the best adapted distribution, commonly referred to as the wild-type. Most important for Darwanius behavfor are the criteria for internal stability of the quasi-species. If hit are the extern for internal stability of the quasi-species. It these critical nat violated, the information stored in the sucjectific sequence of the master copy will dientegrate irreversibly loading to an error estioatrophy. As a consequence, selection and evolution of RNA or DNA molecules is limited with respect to the amount of RNA of DNA improves a timined with reciper to the amount of information that can be stored in a single replicative unit. An analysis of experimental data regarding RNA and DNA replication at various levels of organization reveals, that a sufficient amount of information for the build up of a translation reachinery can of information for the bath up of a translation machinery can be platted only via inforgration of several different replicative units for reproductive cycleo through (secricus) Bakages. A stable fun-tional insignation then will mean the system to a new level of organization and Tarretty enlarge its information capacity considerably. The hypercycle appears to be such a form of organization.

The mathematical analysis of dynamical systems using methods of differential topology, yields the result that there is only one type of medianisms which fulfills the following requirements: Ope or maximum when return to be concess prequentions. The information showd in each single applicative with (or regoods-tive cycle) must be maintained, i.e., the respective master copies must compare favorably with their error distributions. Despite their competitive behavior there units must establish a cooperation which includes all functionally integrated species. On the other which includes all functionally integrated speeces. On the other hand, the cycle as a whole send continue to compute strongly with any other single emitty or includ ensemble which does no contribute us in unique off tention of the best shaped of the contribute of the best shaped of the best shaped incurringly little december of the best shaped of the best shaped of the best shaped of the best shaped incurrency little december of the best shaped of the best s

Naturwissenschaften 64, 541-565 (1977) D by Springer-Verlag 197.

hypercyclic organizations are able to fulfil these requirements. Non syche linkages among the autonomous reproduction cycles, such as chains or branched, troe-like networks are devoid of such prop-

the mothermical methods used for proving time assertions are fined-point. Lyapunov- and trajectorial analysis in higher-dimen-sional phase space, spanned by the concentration coordinates of the consensing partners. The self-organizing properties of hypercy-cles are clusicated, using snallytical as well as numerical techniques

Province on Part C: The Bucker's Honorcycle

of the grantic code and the translation machinery is recognized. it includes the following features referring to natural systems:

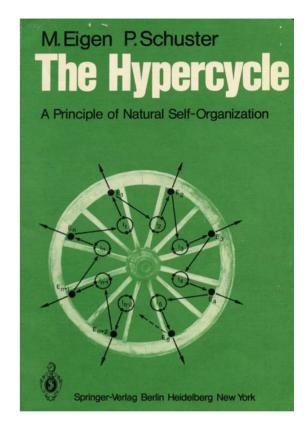
1) The hypercycle has a sufficiently emple structure to admit an origination, with finite probability under problems conditions. 3) It permits a continuous emergence from closely intermisted (t. RNA-like) procursors, originally being members of a stable RNA quasi-species and having been amplified to a level of higher abuse

3) The organizational structure and the properties of single (laporities) units of this laypercycle are still reflected in the present genetic code in the translation apparatus of the prolaryotic cell, as well as in outrain bacterial visious.

J. The Paradigm of Unity and Diversity in Evolution

Why do millions of species, plants and animals, exist, while there is only one basic molecular machinery of the cell: one universal genetic code and unique chiralities of the macromolecules?

The geneticists of our day would not hesitate to give an immediate answere to the first part of this question. Diversity of species is the outcome of the tremendous branching process of evolution with its myriads of single sters of reproduction and mutation. It in-



Chemical kinetics of molecular evolution

Stock solution:

activated monomers, ATP, CTP, GTP, UTP (TTP);

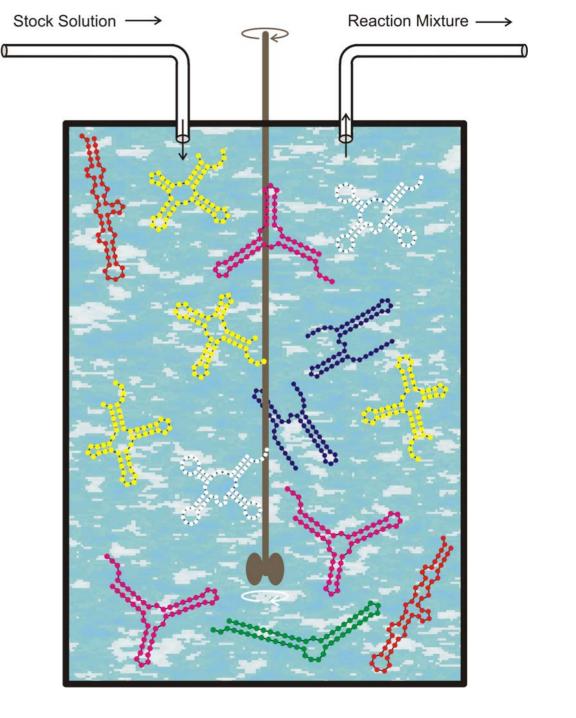
a replicase, an enzyme that performs complementary replication; buffer solution

Flow rate:
$$r = \tau_R^{-1}$$

The population size N, the number of polynucleotide molecules, is controlled by the flow \emph{r}

$$N(t) \approx \overline{N} \pm \sqrt{\overline{N}}$$

The flowreactor is a device for **studies** of evolution *in vitro* and *in silico*.



$$(A) + I_1 \longrightarrow I_2 + I_1$$

$$dx_1 / dt = f_2 x_2 - x_1 \Phi dx_2 / dt = f_1 x_1 - x_2 \Phi$$

$$(A) + I_2 \longrightarrow I_1 + I_2$$

$$\Phi = \Sigma_i \mathbf{f}_i \mathbf{x}_i$$
; $\Sigma_i \mathbf{x}_i = 1$; $i = 1,2$

Complementary replication as the simplest molecular mechanism of reproduction

Equation for complementary replication: $[I_i] = x_i \ge 0$, $f_i > 0$; i=1,2

$$\frac{dx_1}{dt} = f_2 x_2 - x_1 \phi, \quad \frac{dx_2}{dt} = f_1 x_1 - x_2 \phi, \quad \phi = f_1 x_1 + f_2 x_2 = \overline{f}$$

Solutions are obtained by integrating factor transformation

$$x_{1,2}(t) = \frac{\sqrt{f_{2,1}}(\gamma_1(0) \cdot \exp(ft) + \gamma_2(0) \cdot \exp(-ft))}{(\sqrt{f_1} + \sqrt{f_2}) \gamma_1(0) \cdot \exp(ft) - (\sqrt{f_1} - \sqrt{f_2}) \gamma_1(0) \cdot \exp(-ft)}$$

$$\gamma_1(0) = \sqrt{f_1} x_1(0) + \sqrt{f_2} x_2(0), \gamma_2(0) = \sqrt{f_1} x_1(0) - \sqrt{f_2} x_2(0), f = \sqrt{f_1 f_2}$$

$$x_1(t) \to \frac{\sqrt{f_2}}{\sqrt{f_1} + \sqrt{f_2}} \text{ and } x_2(t) \to \frac{\sqrt{f_1}}{\sqrt{f_1} + \sqrt{f_2}} \text{ as } \exp(-ft) \to 0$$

Reproduction of organisms or replication of molecules as the basis of selection

Selection equation: $[I_i] = x_i \ge 0$, $f_i > 0$

$$\frac{dx_i}{dt} = x_i \left(f_i - \phi \right), \quad i = 1, 2, \dots, n; \quad \sum_{i=1}^n x_i = 1; \quad \phi = \sum_{j=1}^n f_j x_j = \overline{f}$$

Mean fitness or dilution flux, $\phi(t)$, is a non-decreasing function of time,

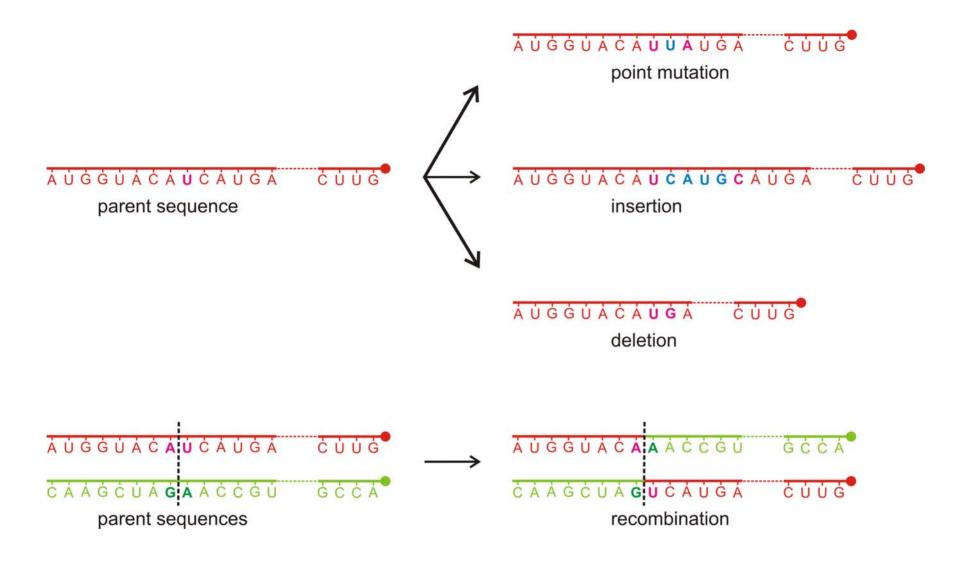
$$\frac{d\phi}{dt} = \sum_{i=1}^{n} f_i \frac{dx_i}{dt} = \overline{f^2} - (\overline{f})^2 = \operatorname{var}\{f\} \ge 0$$

Solutions are obtained by integrating factor transformation

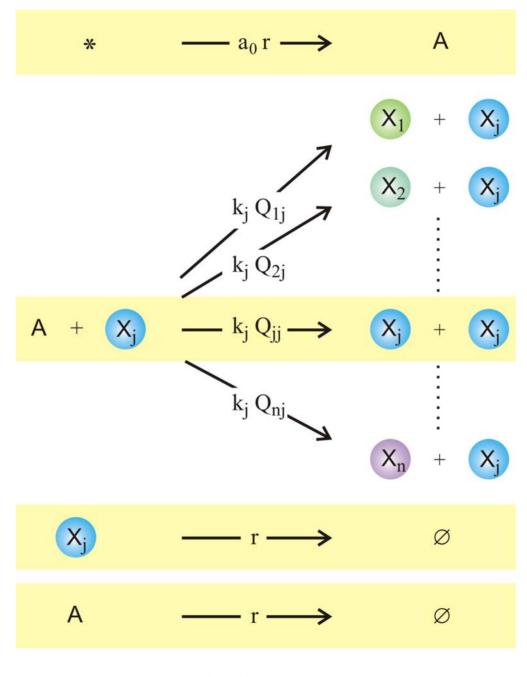
$$x_{i}(t) = \frac{x_{i}(0) \cdot \exp(f_{i}t)}{\sum_{j=1}^{n} x_{j}(0) \cdot \exp(f_{j}t)}; \quad i = 1, 2, \dots, n$$



Selection between three species with $f_1 = 1, f_2 = 2$, and $f_3 = 3$



Variation of genotypes through mutation and recombination



$$j = 1,2, ..., n$$

$$* \xrightarrow{a_0 \cdot r} \mathbf{A}$$
 : influx

$$\mathbf{A} + \mathbf{X}_i \xrightarrow{k_i Q_{ii}} 2 \mathbf{X}_i \; ; \quad i = 1, \dots, n$$
 : replication

$$\mathbf{A} + \mathbf{X}_i \xrightarrow{k_i Q_{ji}} \mathbf{X}_i + \mathbf{X}_j \quad i, j = 1, \dots, n; i \neq j$$
: mutation

$$A \xrightarrow{r} \emptyset$$
 : outflux

$$\mathbf{X}_i \xrightarrow{r} \emptyset \; ; \; j = 1, \dots, n$$
 : outflux

$$\frac{da}{dt} = -a \sum_{i=1}^{n} \sum_{j=1}^{n} k_i Q_{ji} x_i + r (a_0 - a) = -a \sum_{i=1}^{n} k_i x_i + r (a_0 - a)$$

$$\frac{dx_j}{dt} = a \sum_{i=1}^n k_i Q_{ji} x_i - r x_j$$

Origin of the replication-mutation equation from the flowreactor

Stationary solutions of the flow reactor:

$$\frac{da}{dt} = 0 = -\tilde{a} \left(\sum_{i=1}^{n} k_i \, \tilde{x}_i + r \right) + r \, \tilde{a}$$

$$\frac{dx_j}{dt} = 0 = \tilde{a} \sum_{i=1}^{n} k_i Q_{ji} \tilde{x}_i - r \, \tilde{x}_j; \ c = \sum_{i=1}^{n} x_i; \ \bar{k} = \frac{\sum_{i=1}^{n} k_i \, x_i}{c}$$

$$\frac{dc}{dt} = 0 = \tilde{c} \left(\bar{k} \, \tilde{a} - r \right)$$

Stationary solutions: 1. active state

Stationary solutions: 2. extinction

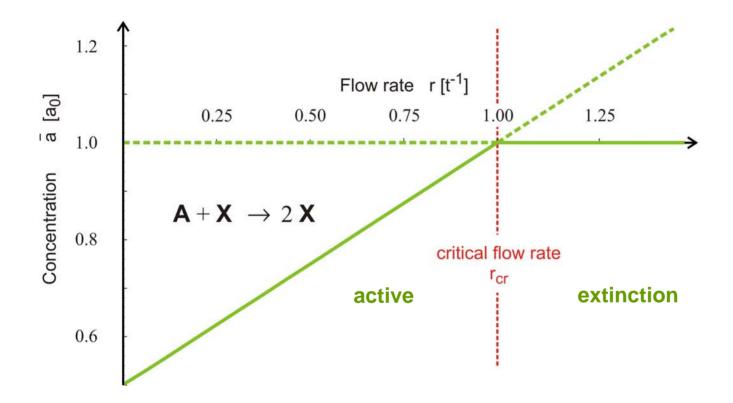
$$r < \bar{k} a_0$$

$$\tilde{a} = \frac{r}{\bar{k}}$$

$$\tilde{a} = a_0$$

$$\tilde{c} = \frac{\bar{k} a_0 - r}{\bar{k}}$$

$$\tilde{x}_j = 0; j = 1, 2, \dots, n$$



Find r(t) such that $a(t) = \bar{a} = const.$

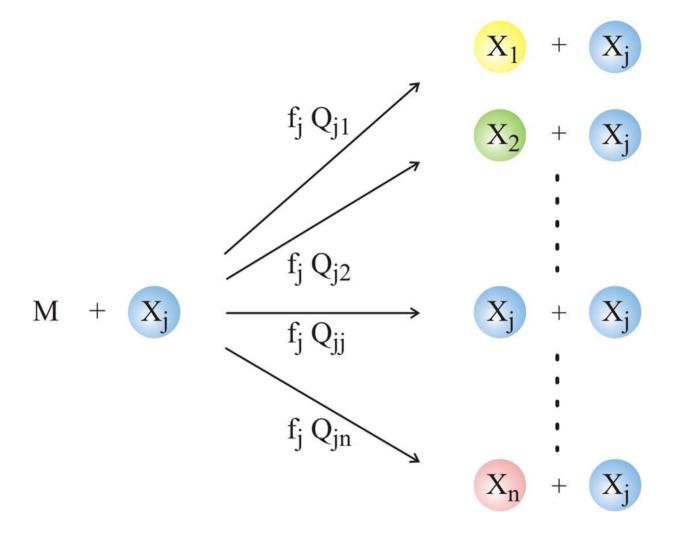
$$\frac{da}{dt} = 0 = -\bar{a} \sum_{i=1}^{n} \sum_{j=1}^{n} k_i Q_{ji} x_i + r(t) (a_0 - \bar{a})$$

$$r(t) = \frac{\bar{a}}{a_0 - \bar{a}} \sum_{i=1}^{n} k_i x_i; f_i = k_i \bar{a}$$

$$\frac{dx_j}{dt} = \sum_{i=1}^n f_i Q_{ji} x_i - x_j \frac{\sum_{i=1}^n f_i x_i}{\sum_{i=1}^n x_i} = \sum_{i=1}^n f_i Q_{ji} x_i - x_j \bar{f}$$

Origin of the replication-mutation equation from the flowreactor

- 1. Replication and mutation
- 2. Quasispecies and error thresholds
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Chemical kinetics of replication and mutation as parallel reactions

$$\frac{dx_{j}}{dt} = \sum_{i=1}^{n} f_{i} Q_{ij} x_{i} - x_{j} \Phi \quad \text{with} \quad \Phi = \sum_{i=1}^{n} f_{i} x_{i}$$
and
$$\sum_{i=1}^{n} x_{i} = 1$$

$$Q_{ij} = (1-p)^{n-d_H(X_i,X_j)} p^{d_H(X_i,X_j)}; \quad p... \text{ error rate per digit}$$

 $d_H(X_i, X_j)$... Hamming distance between X_i and X_j

$$\sum_{j=1}^n Q_{ij} = 1$$

The replication-mutation equation

Mutation-selection equation: $[I_i] = x_i \ge 0, f_i > 0, Q_{ij} \ge 0$

$$\frac{dx_i}{dt} = \sum_{j=1}^n f_j Q_{ji} x_j - x_i \phi, \quad i = 1, 2, \dots, n; \quad \sum_{i=1}^n x_i = 1; \quad \phi = \sum_{j=1}^n f_j x_j = \overline{f}$$

Solutions are obtained after integrating factor transformation by means of an eigenvalue problem

$$x_{i}(t) = \frac{\sum_{k=0}^{n-1} \ell_{ik} \cdot c_{k}(0) \cdot \exp(\lambda_{k}t)}{\sum_{j=1}^{n} \sum_{k=0}^{n-1} \ell_{jk} \cdot c_{k}(0) \cdot \exp(\lambda_{k}t)}; \quad i = 1, 2, \dots, n; \quad c_{k}(0) = \sum_{i=1}^{n} h_{ki} x_{i}(0)$$

$$W \div \{f_i Q_{ij}; i, j=1,2,\cdots,n\}; L = \{\ell_{ij}; i, j=1,2,\cdots,n\}; L^{-1} = H = \{h_{ij}; i, j=1,2,\cdots,n\}$$

$$L^{-1} \cdot W \cdot L = \Lambda = \{\lambda_k; k=0,1,\dots,n-1\}$$

Matrix W and Frobenius theorem:

$$W = \begin{pmatrix} w_{11} & w_{12} & \dots & w_{1n} \\ w_{21} & w_{22} & \dots & w_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ w_{n1} & w_{n2} & \dots & w_{nn} \end{pmatrix}$$

Primitive matrix W:

A nonnegative square matrix $W = \{w_{ij}\}$ is said to be a primitive matrix if there exists k such that $W^k \gg 0$, i.e., if there exists k such that for all i, j, the (i, j) entry of W^k is positive.

Perron-Frobenius theorem applied to the value matrix W

W is primitive: (i) λ_0 is real and strictly positive

(ii)
$$\lambda_0 > |\lambda_k|$$
 for all $k \neq 0$

- (iii) λ_0 is associated with strictly positive eigenvectors
- (iv) λ_0 is a simple root of the characteristic equation of W (v-vi) etc.

W is irreducible: (i), (iii), (iv), etc. as above

(ii)
$$\lambda_0 \ge |\lambda_k|$$
 for all $k \ne 0$

Decomposition of matrix W

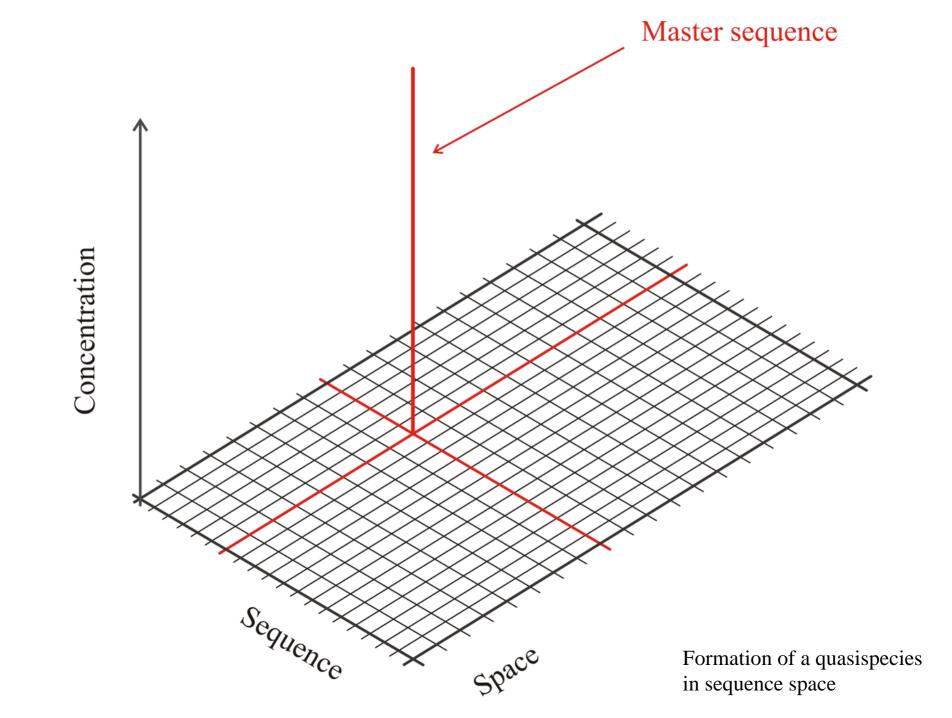
$$W = \begin{pmatrix} w_{11} & w_{12} & \dots & w_{1n} \\ w_{21} & w_{22} & \dots & w_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ w_{n1} & w_{n2} & \dots & w_{nn} \end{pmatrix} = Q \cdot F \text{ with}$$

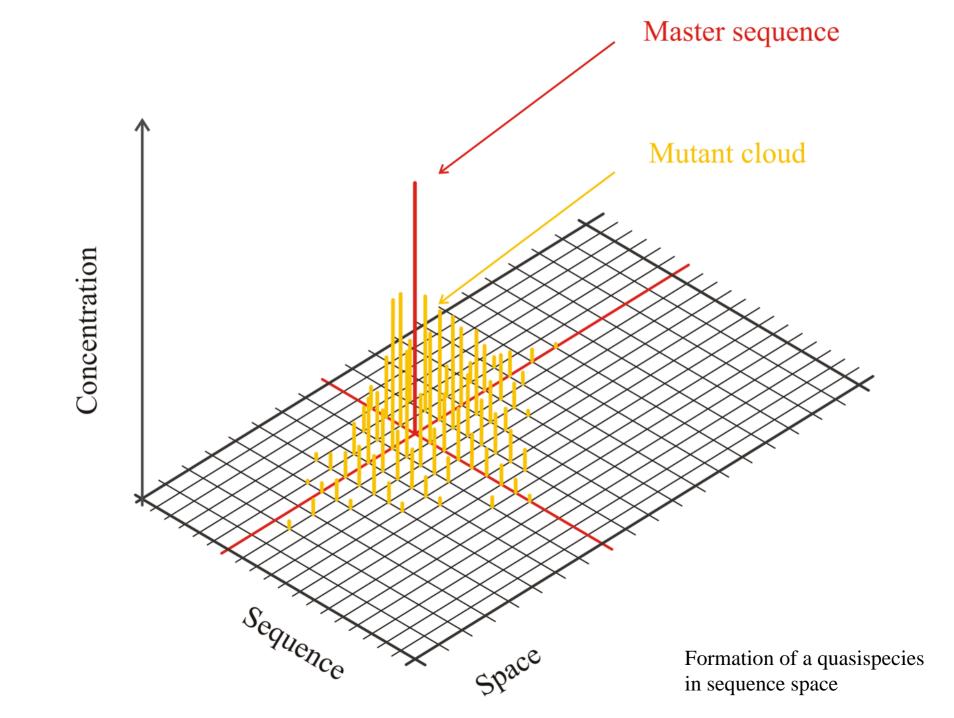
$$Q = \begin{pmatrix} Q_{11} & Q_{12} & \dots & Q_{1n} \\ Q_{21} & Q_{22} & \dots & Q_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ Q_{n1} & Q_{n2} & \dots & Q_{nn} \end{pmatrix} \text{ and } F = \begin{pmatrix} f_1 & 0 & \dots & 0 \\ 0 & f_2 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & f_n \end{pmatrix}$$

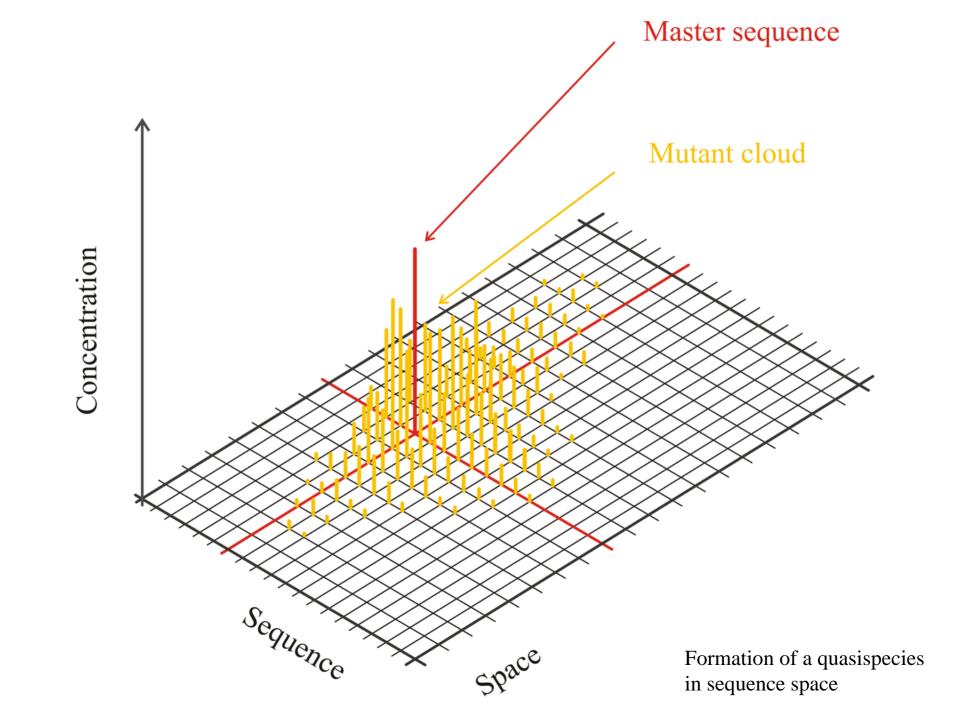
Uniform error rate model:

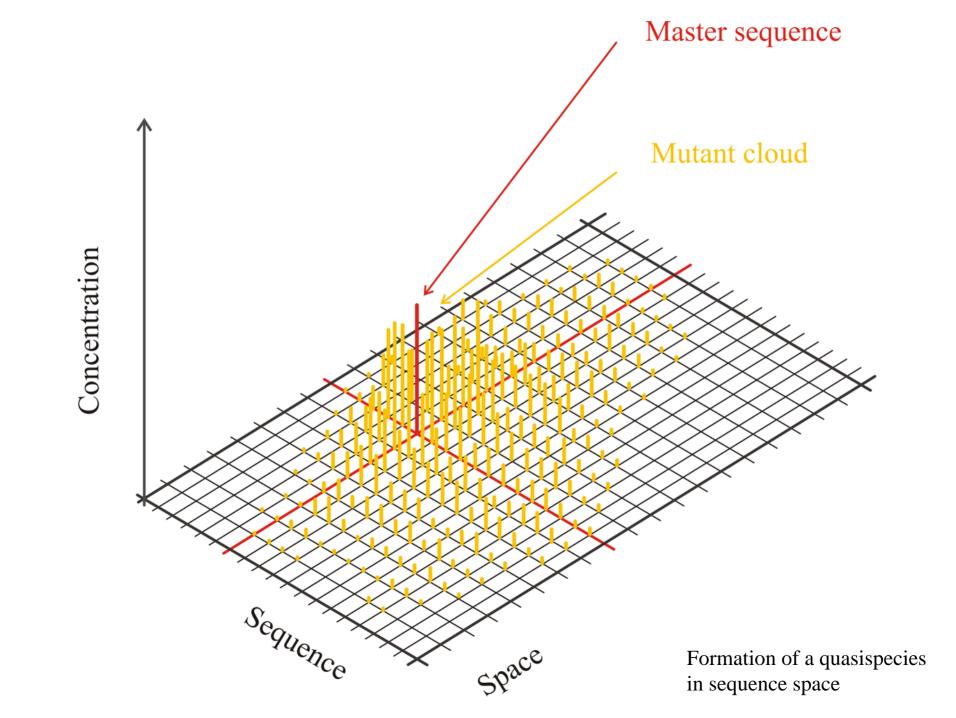
$$Q_{ij} = p^{d_H(\mathbf{X}_i, \mathbf{X}_j)} (1 - p)^{(n - d_H(\mathbf{X}_i, \mathbf{X}_j))}$$

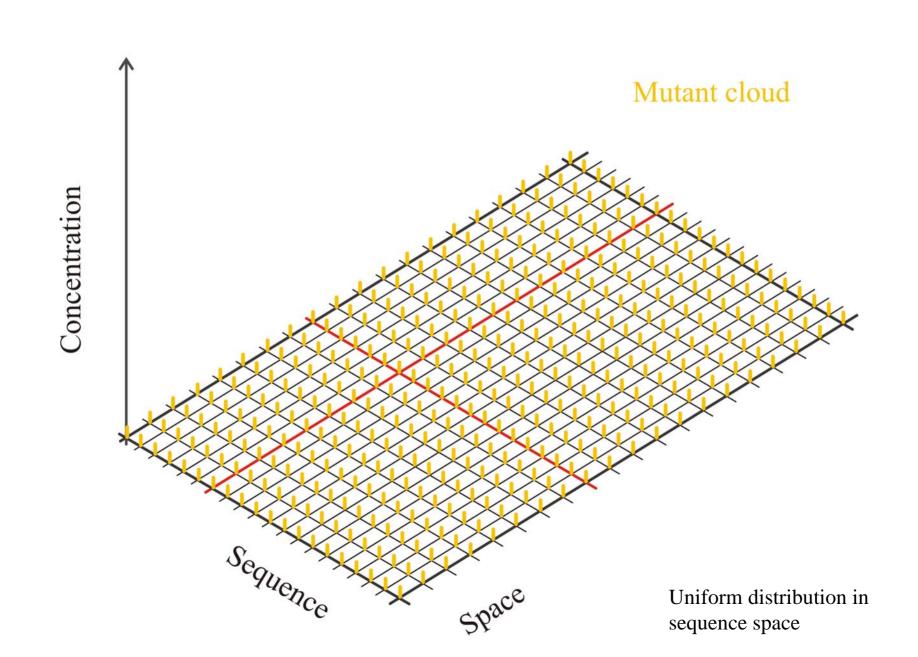
 $d_H(\mathbf{X}_i, \mathbf{X}_j)$... Hamming distance











Biophysical Chemistry 16 (1982) 329–345.

Elsevier Biomedical Press

SELF-REPLICATION WITH ERRORS

A MODEL FOR POLYNUCLEOTIDE REPLICATION **

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Received 4th June 1982 Revised manuscript received 23rd August 198

Key words: Polynucleotide replication; Quasi-species; Point mutation; Mutant class; Stochastic replication

A model for polymacloside replication is presented and analyzed by means of perturbation theory. Two basic assumptions allow handling of dependence up to a chain length of # = 90 to explicitly point mutations are restricted to a two-digit model and individual sequences are subsumed into mutant classes. Perturbation theory is in excellent agreement with the exact results for long enough sequences (* > 20).

1. Introduction

Eigen [8] proposed a formal kinetic equation (eq. 1) which describes self-replication under the constraint of constant total population size:

$$\frac{dx_i}{dt} = \dot{x}_i = \sum_i w_{ij} x_j - \frac{x_i}{c} \phi; i = 1,...,n$$
(1)

By x_i we denote the population number or concentration of the self-replicating element 1_i , i.e., $x_i = [1_i]$. The total population size or total concentration $c = \Sigma_i x_i$ is kept constant by proper adjustment of the constraint $c_i \in \Sigma_i \Sigma_i w_i x_i$. Characteristically, this constraint has been called 'constant organization'. The relative values of diagonal

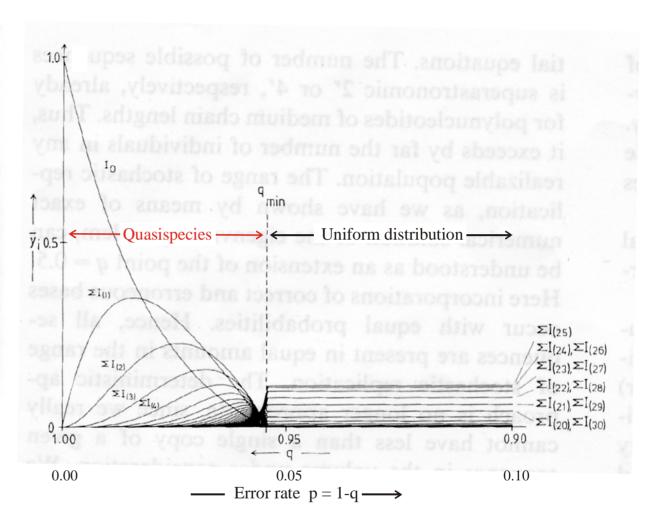
- Dedicated to the late Professor B.L. Jones who was among the first to do rigorous mathematical analysis on the problems described here.
- •• This paper is considered as part II of Model Studies on RNA replication. Part I is by Gassner and Schuster [14].
 All summations throughout this paper run from I to α unless specified differently: Σ_i = Σⁿ_{i-1} and Σ_{i,i-1} = Σⁿ_{i-1} + Σⁿ_{i-1,i-1}.

 (w_{ii}) and off-diagonal $(w_{ji}, i \neq j)$ rates, as we shall see in detail in section 2, are related to the accuracy of the replication process. The specific properties of eq. 1 are essentially based on the fact that it leads to exponential growth in the absence of constraints $(\phi = 0)$ and competitors (n = 1).

The non-linear differential equation, eq. 1 — to non-linearity is introduced by the definition of 6 at constant organization — shows a remarkable feature: it leads to selection of a defined ensemble of self-replicating elements above a certain accuracy threshold. This ensemble of a master and its most frequent mutants is a so-called 'quasi-species' [9]. Below this threshold, however, no selection takes place and the frequencies of the individual elements are determined exclusively by their statistical weights.

Rigorous mathematical analysis has been performed on eq. 1 [7,15,24,6]. In particular, it was shown that the non-linearity of eq. 1 can be removed by an appropriate transformation. The eigenvalue problem of the linear differential equation obtained thereby may be solved approximately by the conventional perturbation technique

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Chain length and error threshold

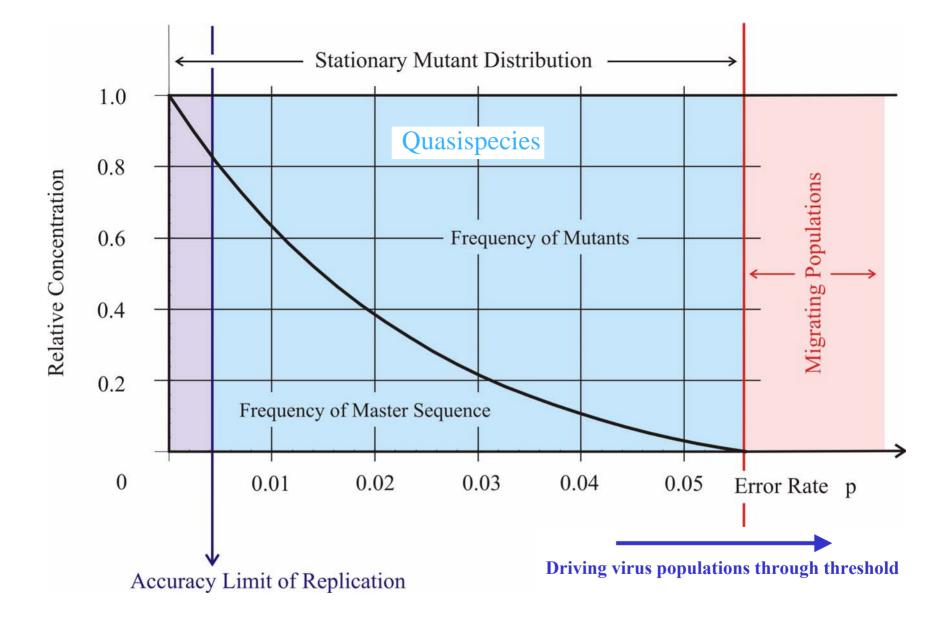
$$Q \cdot \sigma = (1-p)^n \cdot \sigma \ge 1 \implies n \cdot \ln(1-p) \ge -\ln \sigma$$

$$n \dots \text{constant} : p_{\text{max}} \approx \frac{\ln \sigma}{n}$$

$$p \dots \text{constant} : n_{\text{max}} \approx \frac{\ln \sigma}{p}$$

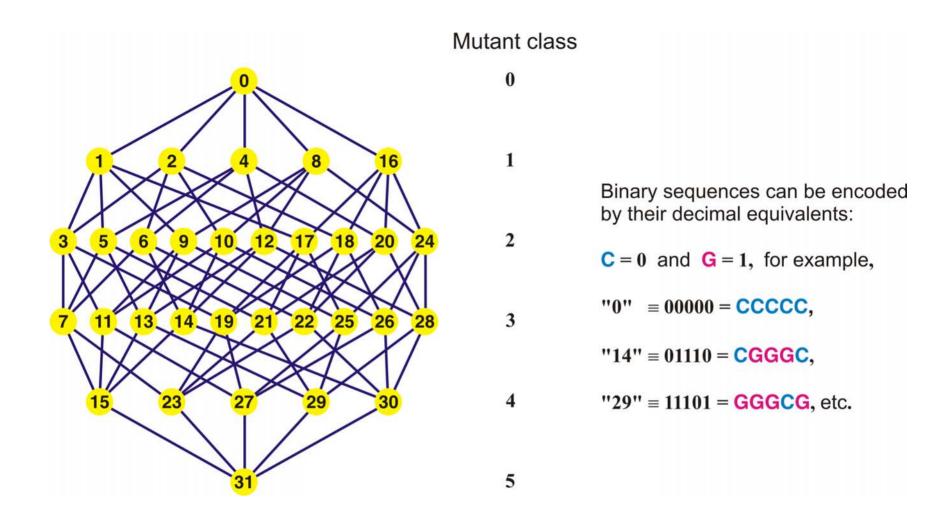
$$Q = (1-p)^n$$
 ... replication accuracy

$$\sigma = \frac{f_m}{(1 - x_m) \sum_{j \neq m} f_j} \dots \text{ superiority of master sequence}$$



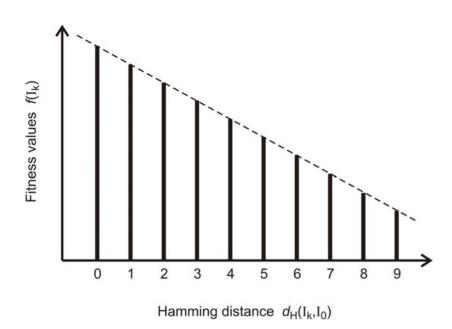
The error threshold in replication

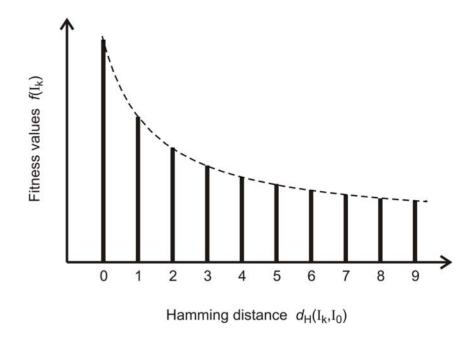
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- 5. Ruggedness of natural landscapes
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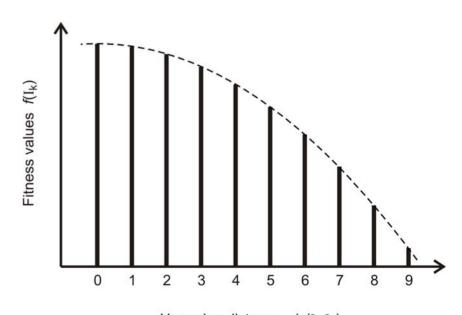


Every point in sequence space is equivalent

Sequence space of binary sequences with chain length n = 5

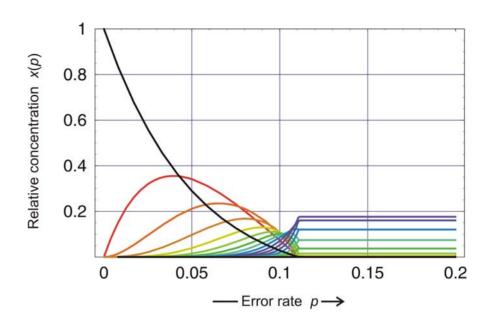


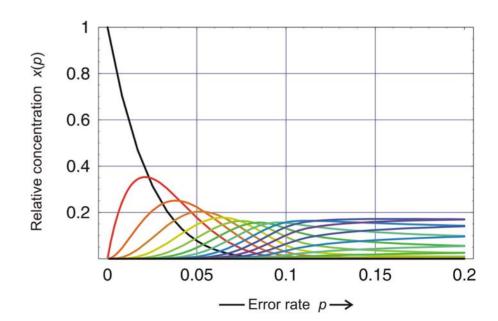




Fitness landscapes not showing error thresholds

Hamming distance $d_{H}(I_{k},I_{0})$





Error thresholds and gradual transitions

$$n = 20$$
 and $\sigma = 10$

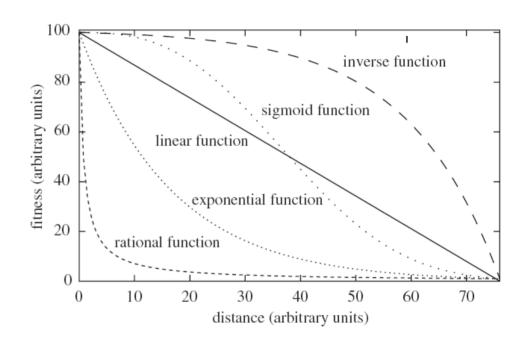
(1) linear
$$f_{scale}^1(d) = 100(1 - d/l)$$
,

(2) exponential
$$f_{scale}^{2}(d) = 100^{1-d/l}$$
,

(3) rational
$$f_{scale}^3(d) = \frac{1}{0.01 + d/l}$$
,

(4) sigmoid
$$f_{scale}^4(d) = 100^{1-(d/l)^{\sigma}}$$
,

(5) inverse
$$f_{scale}^{5}(d) = 100 - 100^{d/l} + 1$$
.



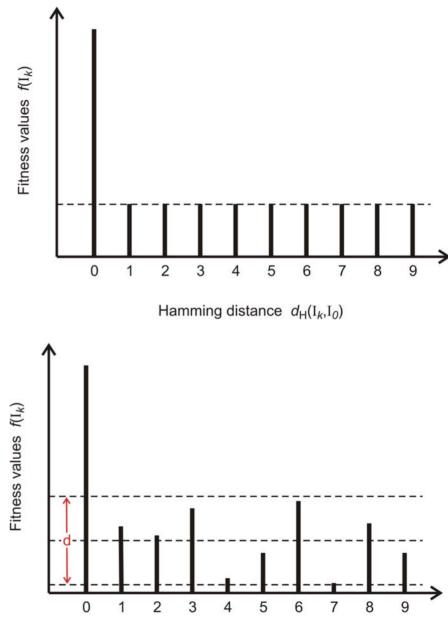
Anne Kupczok, Peter Dittrich, Determinats of simulated RNA evolution. J.Theor.Biol. **238**:726-735, 2006

Three sources of ruggedness:

- 1. Variation in fitness values
- 2. Deviations from uniform error rates
- 3. Neutrality

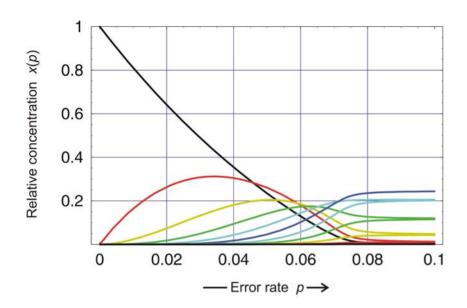
Three sources of ruggedness:

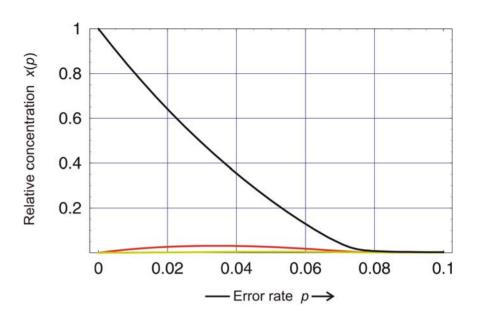
- 1. Variation in fitness values
- 2. Deviations from uniform error rates
- 3. Neutrality

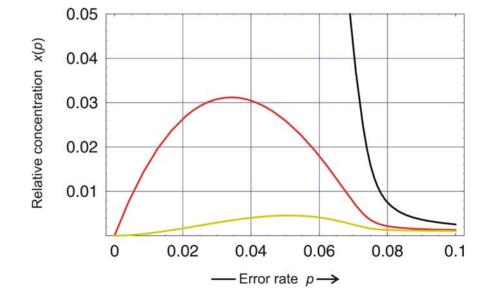


Fitness landscapes showing error thresholds

Hamming distance $d_H(I_k,I_0)$

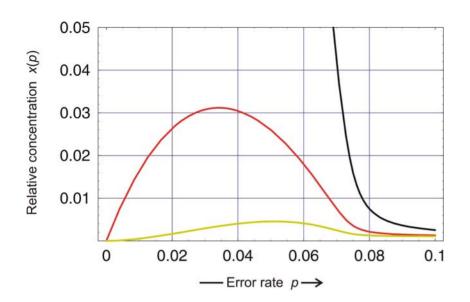


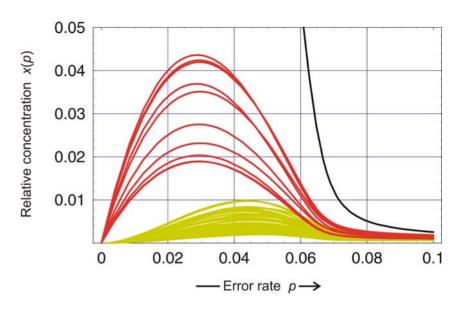


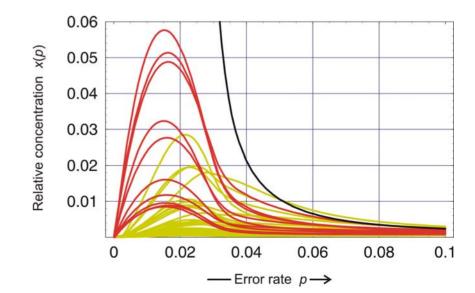


Error threshold: Error classes and individual sequences

$$n = 10$$
 and $\sigma = 2$

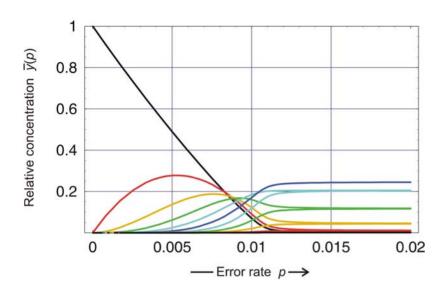


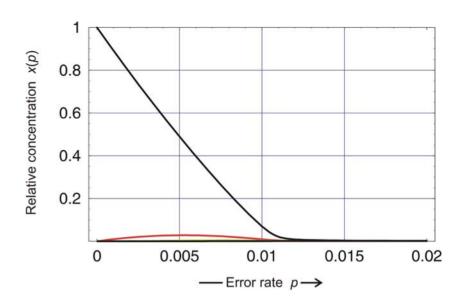


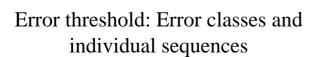


Error threshold: Individual sequences

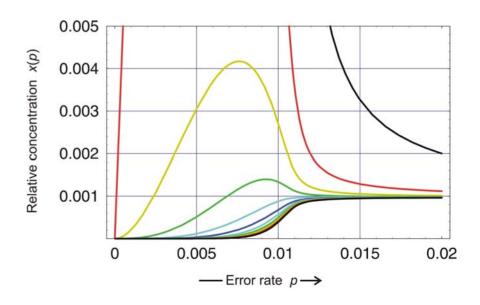
$$n = 10$$
, $\sigma = 2$ and $d = 0$, 1.0, 1.85

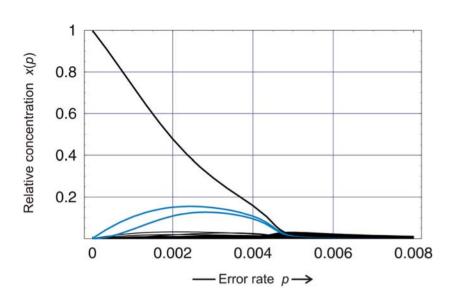


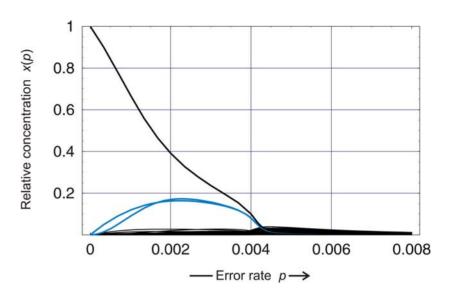


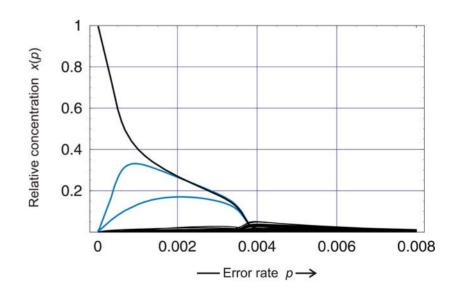


$$n = 10$$
 and $\sigma = 1.1$



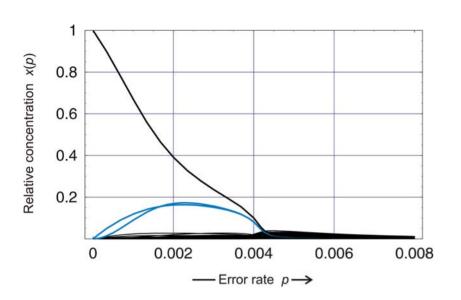


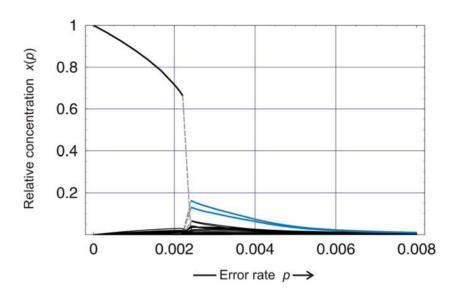


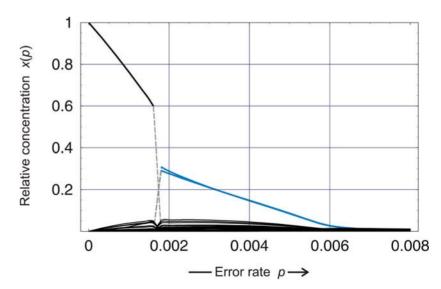


Error threshold: Individual sequences

n = 10, $\sigma = 1.1$, d = 1.95, 1.975, 2.00 and seed = 877







Error threshold: Individual sequences

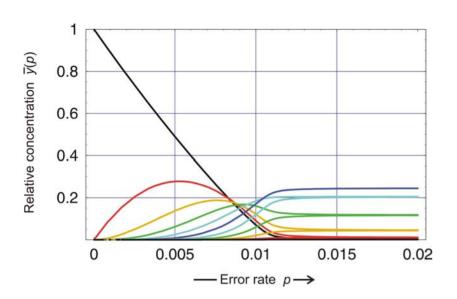
n = 10, $\sigma = 1.1$, d = 1.975, and seed = 877, 637, 491

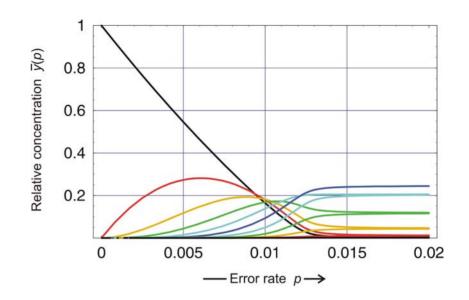
Three sources of ruggedness:

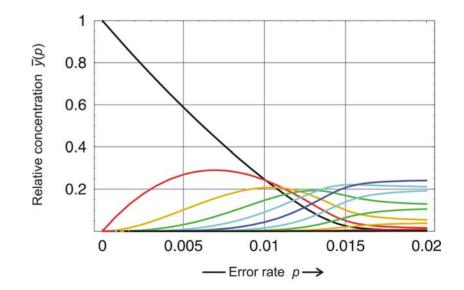
- 1. Variation in fitness values
- 2. Deviations from uniform error rates
- 3. Neutrality

Local replication accuracy pk:

$$p_k = p + 4 \delta p(1-p) (X_{rnd}-0.5), k = 1,2,...,2^{v}$$

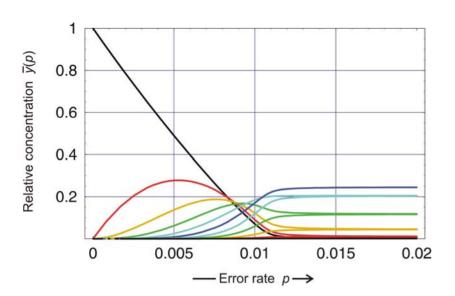


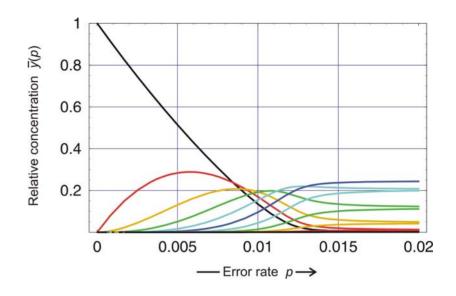


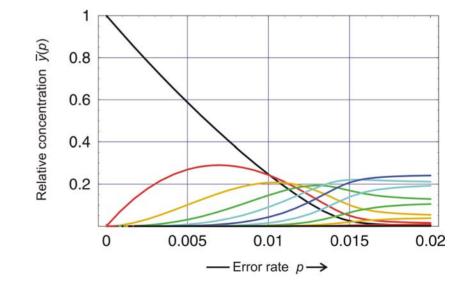


Error threshold: Classes

n = 10, $\sigma = 1.1$, $\delta = 0$, 0.3, 0.5, and seed = 877





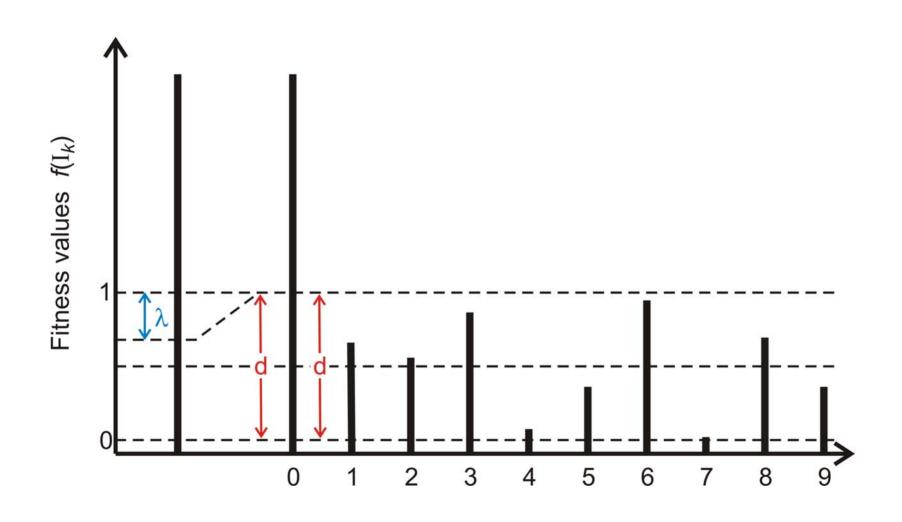


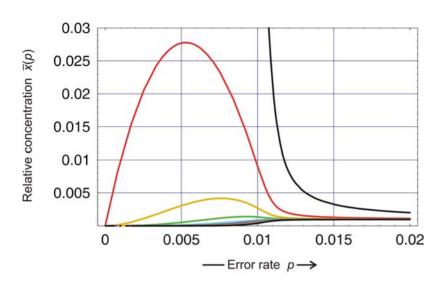
Error threshold: Classes

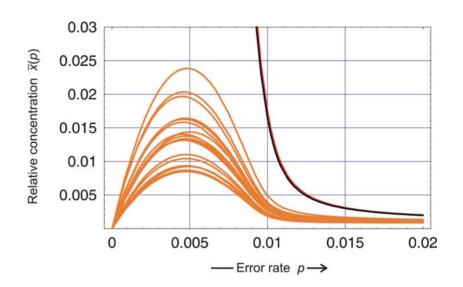
n = 10, $\sigma = 1.1$, $\delta = 0$, 0.5, and seed = 299, 877

Three sources of ruggedness:

- 1. Variation in fitness values
- 2. Deviations from uniform error rates
- 3. Neutrality







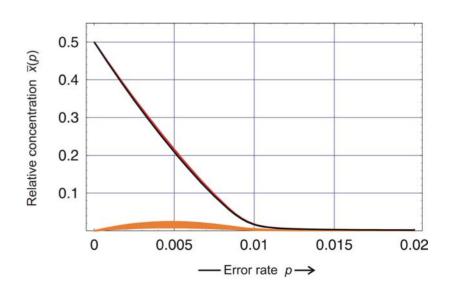


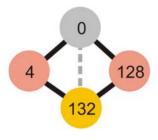
Neutral network

$$\lambda = 0.01$$
, s = 367

Error threshold: Individual sequences

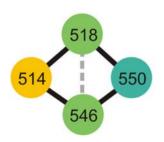
$$n = 10$$
, $\sigma = 1.1$, $d = 1.0$





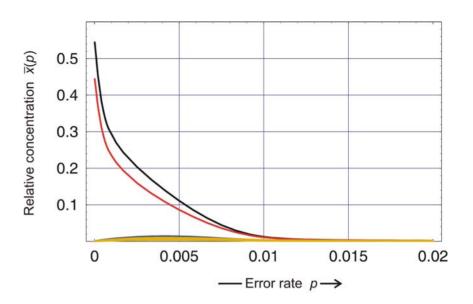
Neutral networks

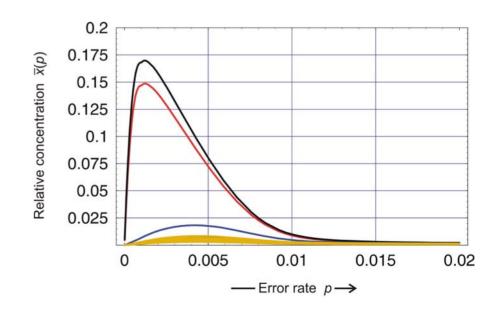
$$\lambda = 0.01$$
, s = 877



Error threshold: Individual sequences

$$n = 10$$
, $\sigma = 1.1$, $d = 1.0$





STATIONARY MUTANT DISTRIBUTIONS AND EVOLUTIONARY OPTIMIZATION

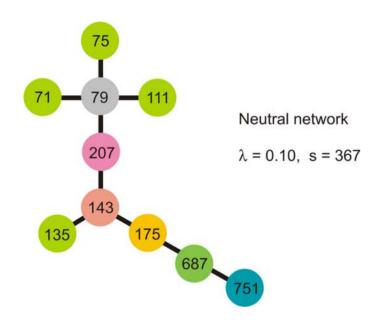
 PETER SCHUSTER and JÖRG SWETINA Institut für theoretische Chemie und Strahlenchemie der Universität Wien, Währingerstraße 17, A 1090 Wien, Austria

Molecular evolution is modelled by erroneous replication of binary sequences. We show how the selection of two species of equal or almost equal selective value is influenced by its nearest neighbours in sequence space. In the case of perfect neutrality and sufficiently small error rates we find that the Hamming distance between the species determines selection. As the error rate increases the fitness parameters of neighbouring species become more and more important. In the case of almost neutral sequences we observe a critical replication accuracy at which a drastic change in the "quasispecies", in the stationary mutant distribution occurs. Thus, in frequently mutating populations fitness turns out to be an ensemble property rather than an attribute of the individual.

In addition we investigate the time dependence of the mean excess production as a function of initial conditions. Although it is optimized under most conditions, cases can be found which are characterized by decrease or non-monotonous change in mean excess productions.

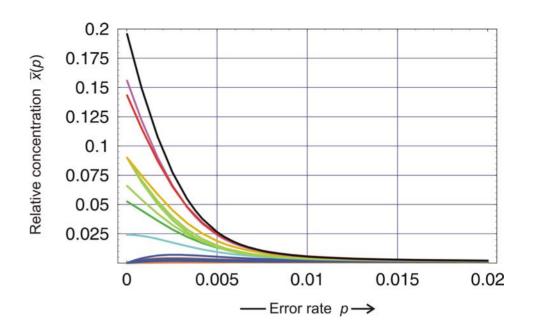
1. Introduction. Recent data from populations of RNA viruses provided direct evidence for vast sequence heterogeneity (Domingo et al., 1987). The origin of this diversity is not yet completely known. It may be caused by the low replication accuracy of the polymerizing enzyme, commonly a virus specific, RNA dependent RNA synthetase, or it may be the result of a high degree of selective neutrality of polynucleotide sequences. Eventually, both factors contribute to the heterogeneity observed. Indeed, mutations occur much more frequently than previously assumed in microbiology. They are by no means rare events and hence, neither the methods of conventional population genetics (Ewens, 1979) nor the neutral theory (Kimura, 1983) can be applied to these virus populations. Selectively neutral variants may be close with respect to Hamming distance and then the commonly made assumption that the mutation backflow from the mutants to the wilde type is negligible does not apply.

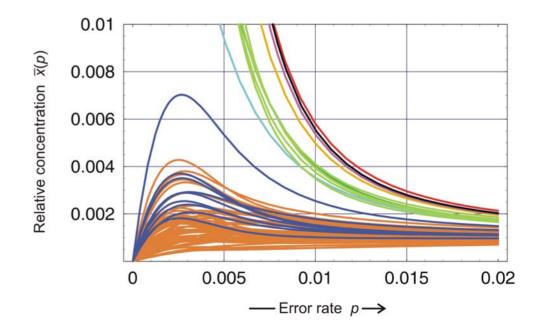
A kinetic theory of polynucleotide evolution which was developed during the past 15 years (Eigen, 1971; 1985; Eigen and Schuster, 1979; Eigen et al., 1987; Schuster, 1986); Schuster and Sigmund, 1985) treats correct replication and mutation as parallel reactions within one and the same reaction network

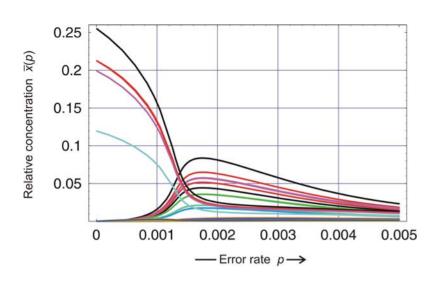


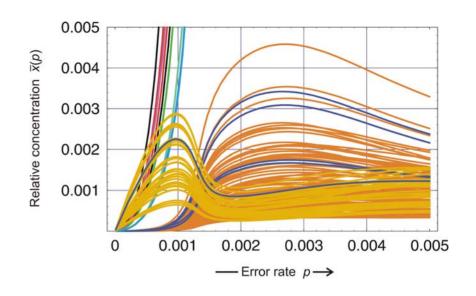
Error threshold: Individual sequences

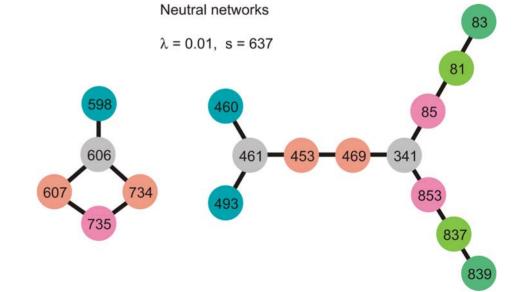
$$n = 10$$
, $\sigma = 1.1$, $d = 1.0$





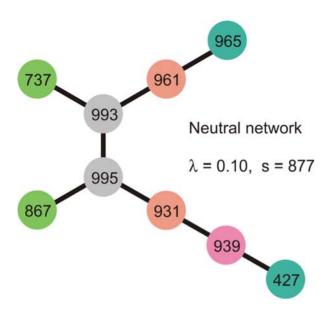


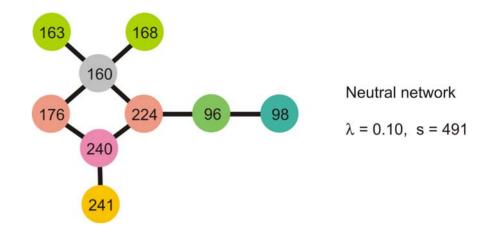


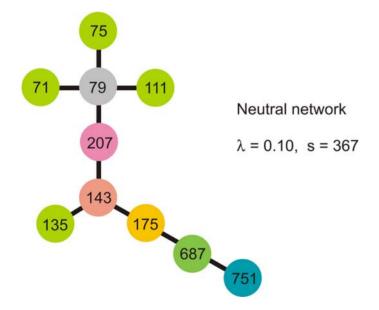


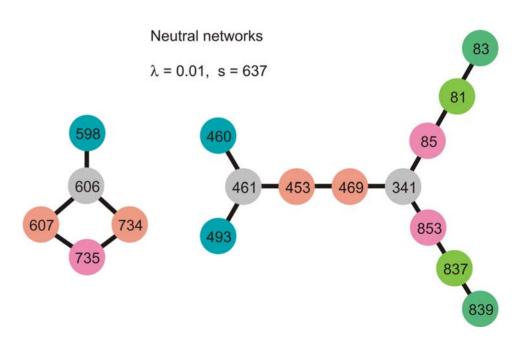
Error threshold: Individual sequences

$$n = 10$$
, $\sigma = 1.1$, $d = 1.0$

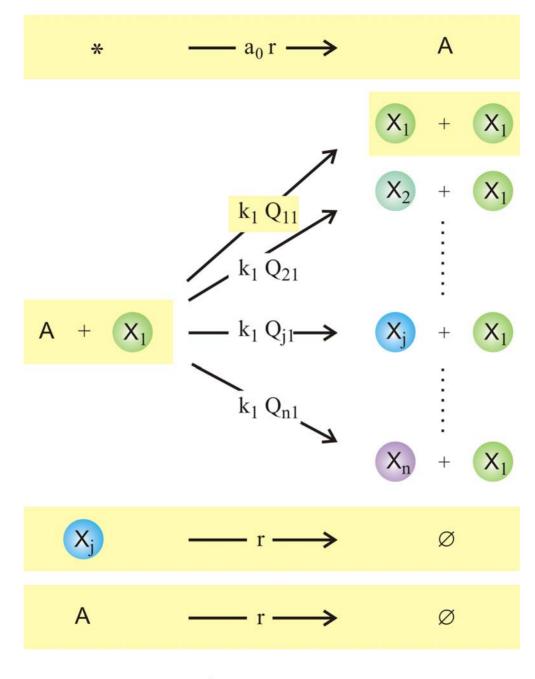








- 1. Replication and mutation
- 2. Quasispecies and error thresholds
- 3. Fitness landscapes and randomization
- 4. Lethal mutations
- 5. Ruggedness of natural landscapes
- 6. Simulation of stochastic phenomena
- 7. Biology in its full complexity



$$j = 1,2, ...,n$$

Lethal mutants and Frobenius theorem:

$$W = \begin{pmatrix} w_{11} & 0 & \dots & 0 \\ w_{21} & 0 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ w_{n1} & 0 & \dots & 0 \end{pmatrix} = w_{11} \begin{pmatrix} 1 & 0 & \dots & 0 \\ \frac{w_{21}}{w_{11}} & 0 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ \frac{w_{n1}}{w_{11}} & 0 & \dots & 0 \end{pmatrix}$$

$$W^{k} = w_{11}^{k} \begin{pmatrix} 1 & 0 & \dots & 0 \\ \frac{w_{21}}{w_{11}} & 0 & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ \frac{w_{n1}}{w_{11}} & 0 & \dots & 0 \end{pmatrix}$$

*
$$\xrightarrow{a_0 \cdot r}$$
 A : influx

$$\mathbf{A} + \mathbf{X}_1 \xrightarrow{k_1 Q_{11}} 2 \mathbf{X}_1;$$
 : replication

$$\mathbf{A} + \mathbf{X}_1 \xrightarrow{k_1 Q_{j1}} \mathbf{X}_1 + \mathbf{X}_j \quad j = 2, \dots, n$$
: mutation

$$A \xrightarrow{r} \emptyset$$
 : outflux

$$\mathbf{X}_{j} \xrightarrow{r} \emptyset \; ; \; j = 1, \dots, n$$
 : outflux

$$\frac{da}{dt} = -a \sum_{j=1}^{n} k_1 Q_{j1} x_1 + r (a_0 - a) = -a k_1 x_1 + r (a_0 - a)$$

$$\frac{dx_j}{dt} = a Q_{j1} x_1 - r x_j$$

Stationary solutions: 1. active state

$$r < k_1 Q_{11} a_0$$

$$\tilde{a} = \frac{r}{k_1 Q_{11}}$$

$$\tilde{x}_1 = Q_{11} (a_0 - \tilde{a}) = Q_{11} a_0 - \frac{r}{k_1}$$

$$\tilde{x}_j = Q_{j1} (a_0 - \tilde{a}) = Q_{j1} \left(a_0 - \frac{r}{k_1 Q_{11}} \right); \quad j = 2, 3, \dots, n$$

Stationary solutions: 2. extinction

$$r > k_1 Q_{11} a_0$$

$$\tilde{a} = a_0$$

$$\tilde{x}_j = 0; \ j = 1, 2, \dots, n$$

Find r(t) such that $a(t) = \bar{a} = const.$

$$\frac{da}{dt} = 0 = -\bar{a} \sum_{j=1}^{n} k_1 Q_{j1} x_1 + r(t) (a_0 - \bar{a})$$

$$r(t) = \frac{\bar{a}}{a_0 - \bar{a}} k_1 x_1; \ f_1 = k_1 \bar{a}; \ \sum_{i=1}^n x_i = c = a_0 - \bar{a}$$

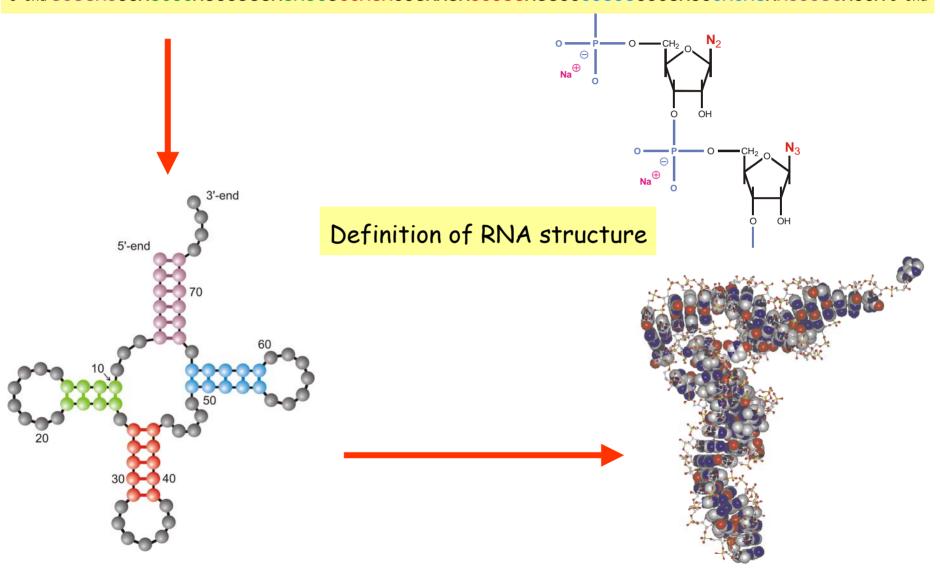
$$\frac{dx_j}{dt} = f_1 Q_{j1} x_1 - x_j \frac{f_1 x_1}{\sum_{i=1}^n x_i} = f_1 x_1 \left(Q_{j1} - \frac{x_j}{c} \right)$$

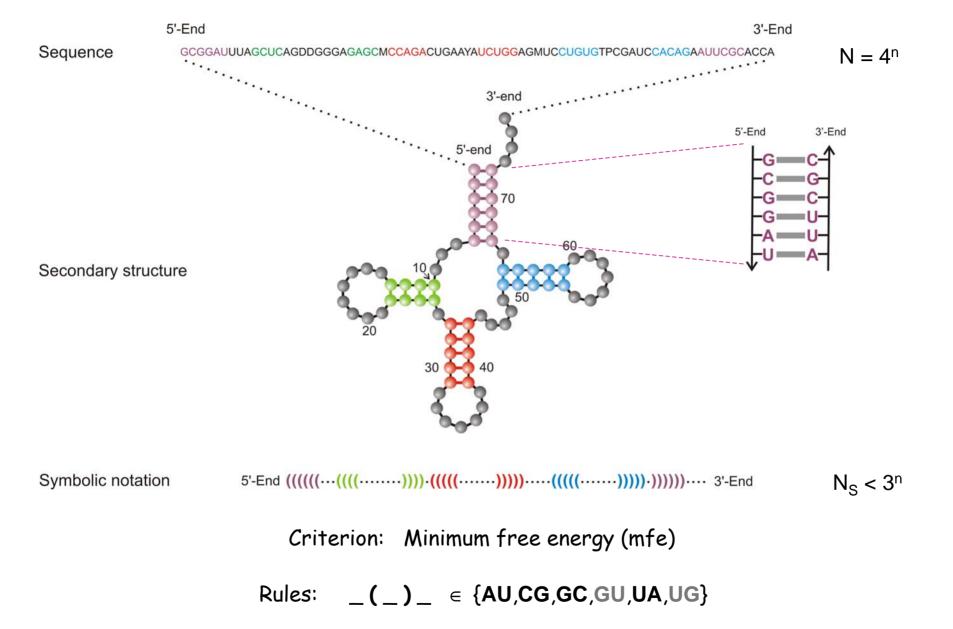
Stationary solutions:

$$\bar{x}_j = Q_{j1} \sum_{i=1}^n \bar{x}_i = Q_{ji} c$$

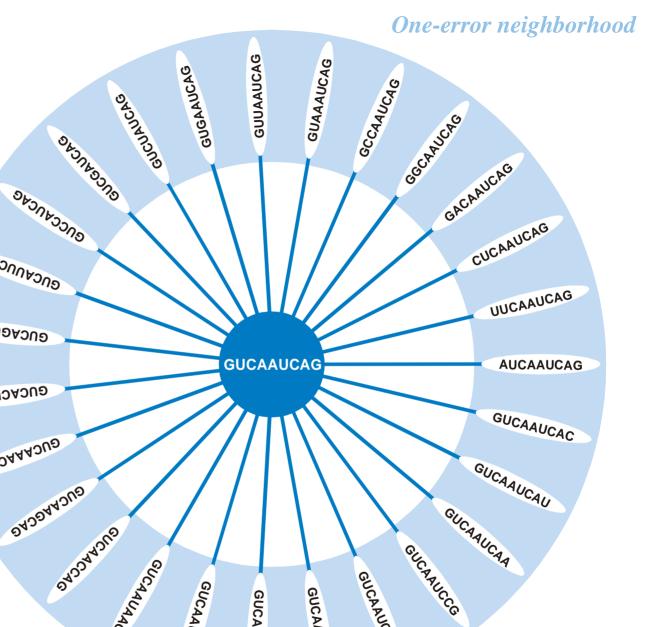
- 1. Replication and mutation
- 2. Quasispecies and error thresholds
- 3. Fitness landscapes and randomization
- 4. Lethal mutations
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- 6. Simulation of stochastic phenomena

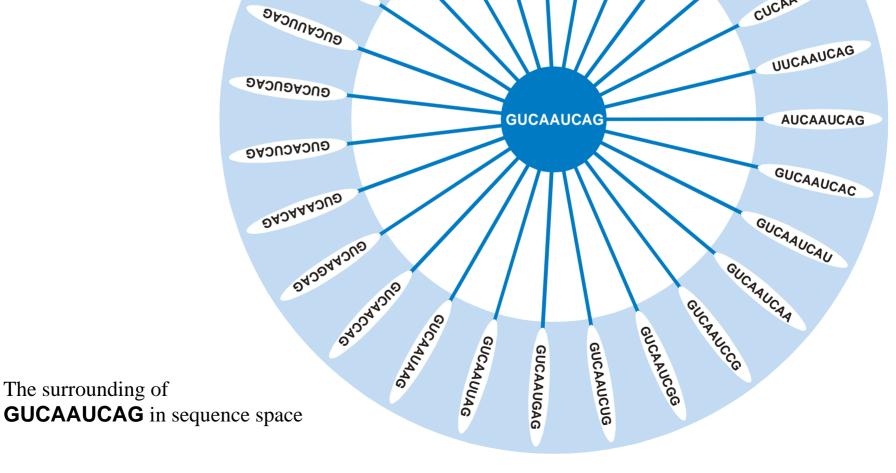
5'-end GCGGAUUUAGCUCAGUUGGGAGACCCCAGACUGAAGAUCUGGAGGUCCUGUGUUCGAUCCACAGAAUUCGCACCA 3'-end



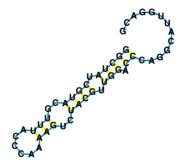


A symbolic notation of RNA secondary structure that is equivalent to the conventional graphs

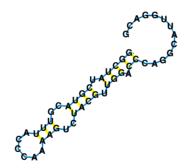


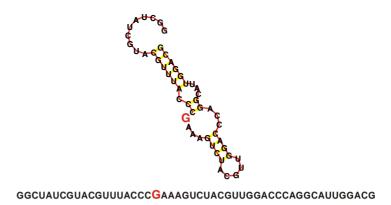


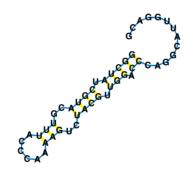


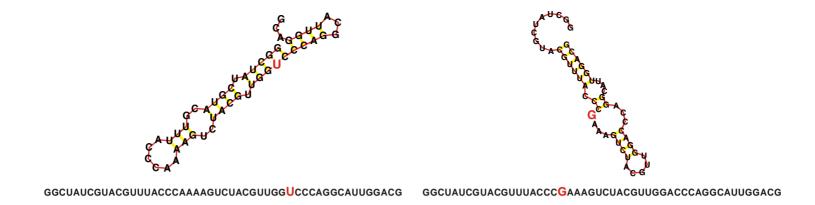


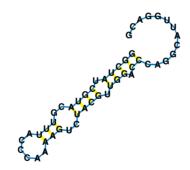
GGCUAUCGUACGUUUACCCAAAAGUCUACGUUGGACCCAGGCAUUGGACG

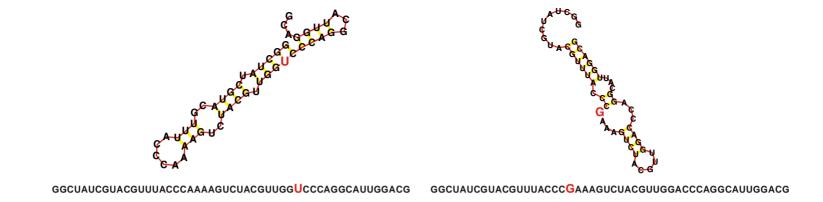


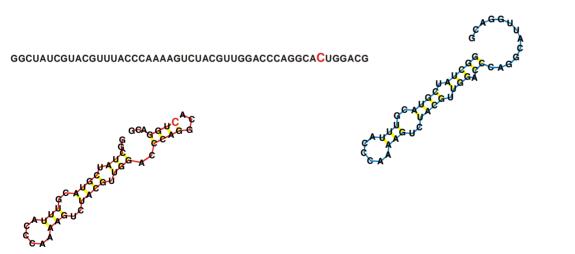


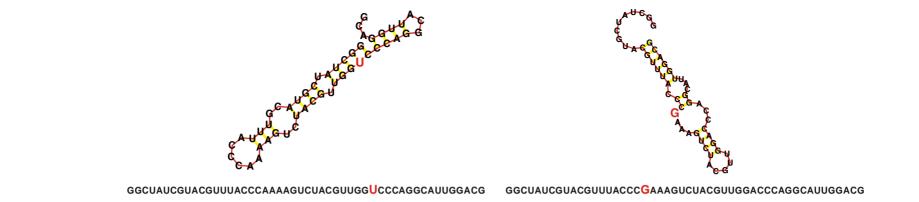


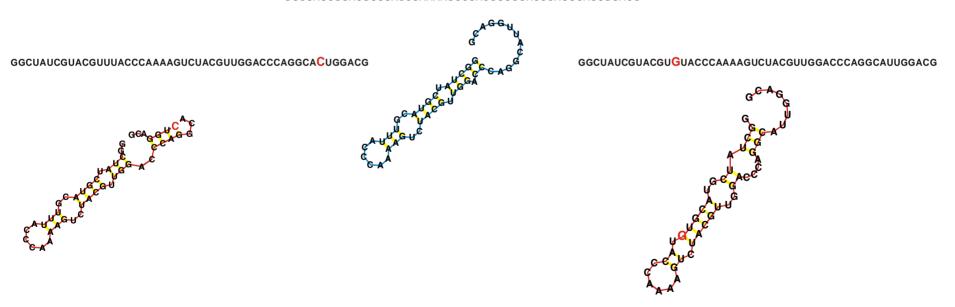










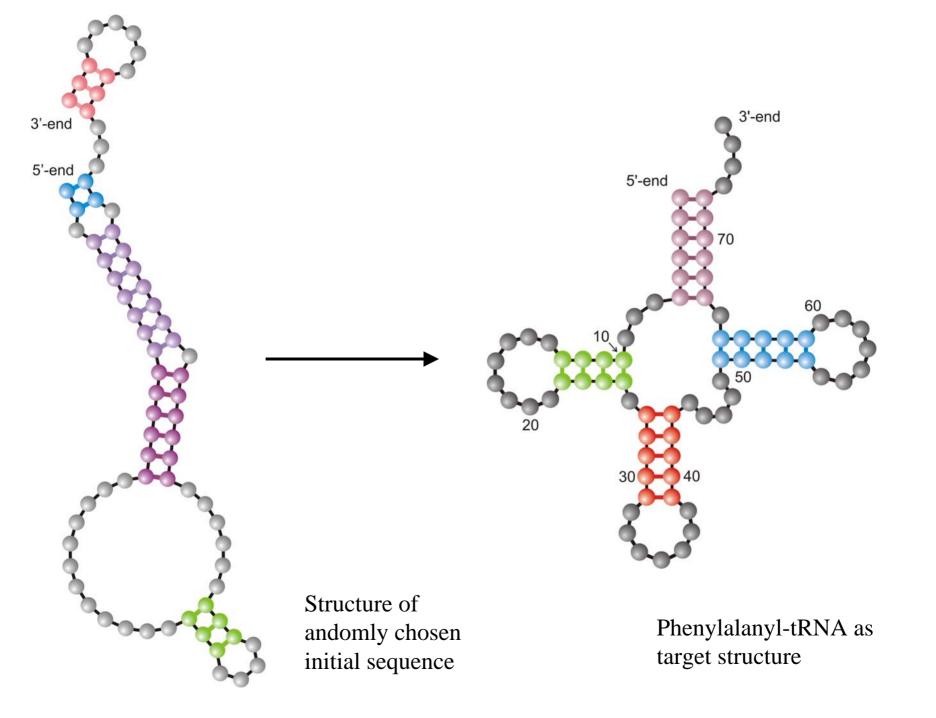


GGCUAUCGUAUGUUUACCCAAAAGUCUACGUUGGACCCAGGCAUUGGACG
GGCUAUCGUACGUUUACCCAAAAGUCUACGUUGGACCCAGGCAUUAGACG
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GGCUAUCGUACGCUUACCCAAAAGUCUACGUUGGACCCAGGCAUUGGACG
GGCCAUCGUACGUUUACCCAAAAGUCUACGUUGGACCCAGGCAUUGGACG
GGCUAUCGUACGUUUACCCAAAAGUCUACGUUGGACCCAGGCAUUGGACG
GGCUAUCGUACGUUUACCCAAAAGUCUACGUUGGACCCAGGCAUUGGACG
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CAGGCAUUGGACG
CAGGCAUUGGACG
CAGGCAUUGGACG
CAGGCAUUGGACG
CAGGCAUUGGACG

	Number	Mean Value	Variance	Std.Dev.	
Total Hamming Distance:	150000	11.647973	23.140715	4.810480	
Nonzero Hamming Distance:	99875	16.949991	30.757651	5.545958	
Degree of Neutrality:	50125	0.334167	0.006961	0.083434	
Number of Structures:	1000	52.31	85.30	9.24	
1 ((((((((((((()))))).))).))	50125	0.334167	
2(((.(((((()))))).)))	2856	0.019040	
3 ((((((((((()))))))))).))	2799	0.018660	
4 ((((((((((((((((((((((((((((((((((((()))).))).))	2417	0.016113	
5 (((((((((((((()).)))).))).))	2265	0.015100	
6 ((((((((((((().))))).))).))	2233	0.014887	
7 ((((((((()))))))).))	1442	0.009613	
8 ((((((()))))))))).))	1081	0.007207	
9 (((((((())))))).))	1025	0.006833	
10 (((((((()))))))))))))	1003	0.006687	
11 .(((((((()))))))))))	963	0.006420	
12 (((((((())))).))).))	860	0.005733	
13 ((((((((())))))))).)))	800	0.005333	
14 ((((((((())))))))))).))	548	0.003653	
15 ((((((())))))))).))	362	0.002413	
16 ((.((.(((((())			227	0.002247	0.0
17 (.(((.(((((())			241	0.001607	AGGU
18 ((((((((((()			231	0.001540	ر الم الم
19 (((((((()			225	0.001500	T E
20 ((((((())			202	0.001347	G G
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				A A A	
				G Y	
				A LIKE GUE	GAGGUNAC GGGGGAGG
				A-U X	
Shadow - Surrounding of an RNA st	tructure in s	hane snace – AUG	🕻 alphabet 🛮 🔥	T	

- 1. Replication and mutation
- 2. Quasispecies and error thresholds
- 3. Fitness landscapes and randomization
- 4. Lethal mutations
- 5. Ruggedness of natural landscapes
- 6. Simulation of stochastic phenomena



Evolution *in silico*

W. Fontana, P. Schuster, Science 280 (1998), 1451-1455

random individuals. The primer pair used for genomic phenotype such as short stature. Moreover, a few DNA amplification is 5'-TCTCCCTGGATTCT-SMS natients have sensorineural hearing loss, nos-CATTTA-3' (forward) and 5'-TCTTTGTCTTCTGT eibly because of a point mutation in MYO15 in trans TCCACC-3' (reverse). Reactions were performed in to the SMS 17n11.2 deletion.

35. R. A. Fridell, data not shown.

36. K. B. Avraham et al., Nature Genet. 11, 369 (1995); X-7 Liu et al. Thirl 17 268 (1997): E. Gibson et al. Nature 374, 62 (1995): D. Weil et al., ibid., p. 60.

37. RNA was extracted from cochlea (membranous labvrinths) obtained from human fetuses at 18 to 22 weeks of development in accordance with guidelines established by the Human Research Committee at the Brigham and Women's Hospital. Only samples without evidence of degradation were pooled for poly (A)+ selection over oligo(dT) columns. Firststrand cDNA was prepared using an Advantage RTfor-PCR kit (Clontech Laboratories). A portion of the first-strand cDNA (4%) was amplified by PCR with Advantage cDNA polymerase mix (Clontech Laboratories) using human MYO15-specific oligonucleotide primers (forward, 5'-GCATGACCTGCCGGCTAAT-GGG-3': reverse, 5'-CTCACGGCTTCTGCATGGT-GCTCGGCTGGC-31). Cycling conditions were 40 s at 94°C; 40 s at 66°C (3 cycles), 60°C (5 cycles), and 55°C (29 cycles): and 45 s at 68°C. PCR products were visualized by ethidium bromide staining after fractionation in a 1% agarose gel. A 688-bp PCR

product is expected from amplification of the human MYO15 cDNA. Amplification of human genomic DNA with this primer pair would result in a 2903-bn fragment.

REPORTS

38. We are grateful to the people of Bengkala, Bali, and the two families from India, We thank J. R. Lupski and K.-S. Chen for providing the human chromosome 17 cosmid library. For technical and computational assistance, we thank N. Dietrich, M. Fergusson A Guota E Sorbello B Torkzadeh C Varner. M. Walker, G. Bouffard, and S. Beckstrom-Sternberg (National Institutes of Health Intramural Se quencing Center). We thank J. T. Hinnant, I. N. Arhya, and S. Winata for assistance in Bali, and T. Barber, S. Sullivan, E. Green, D. Drayna, and J. Battey for helpful comments on this manuscript. Supported by the National Institute on Deafness and Other Communication Disorders (NIDCD) (Z01 DC 00035-01 and Z01 DC 00038-01 to T.B.F. and E.R.W. and R01 DC 03402 to C.C.M.), the National Institute of Child Health and Human Development (R01 HD30428 to S.A.C.) and a National Science Foundation Graduate Research Fellowship to F.J.P. This paper is dedicated to J. B. Snow Jr. on his retirement as the Director of the NIDCD.

9 March 1998; accepted 17 April 1998

Continuity in Evolution: On the **Nature of Transitions**

Walter Fontana and Peter Schuster

To distinguish continuous from discontinuous evolutionary change, a relation of nearness between phenotypes is needed. Such a relation is based on the probability of one phenotype being accessible from another through changes in the genotype. This nearness relation is exemplified by calculating the shape neighborhood of a transfer RNA secondary structure and provides a characterization of discontinuous shape transformations in RNA. The simulation of replicating and mutating RNA populations under selection shows that sudden adaptive progress coincides mostly, but not always, with discontinuous shape transformations. The nature of these transformations illuminates the key role of neutral genetic drift in their realization.

A much-debated issue in evolutionary biology concerns the extent to which the history of life has proceeded gradually or has been punctuated by discontinuous transitions at the level of phenotypes (1). Our goal is to make the notion of a discontinuous transition more precise and to understand how it arises in a model of evolutionary adaptation.

25 µl using 1 unit of Taq DNA polymerase with each

primer at 0.4 µM; 200 µM each dATP, dTTP, dGTP,

and dCTP; and PCR buffer [10 mM tris-HCl (pH 8.3)

50 mM KCl_a, 1.5 mM MgCl_a] in a cycle condition of

94°C for 1 min and then 35 cycles of 94°C for 30 s.

55°C for 30 s. and 72°C for 30 s followed by 72°C for

6 min. PCR products were purified (Qiagen), digested

result in degradation of the transcript (L. Maguat,

50 human tissues (The Human RNA Master Blot.

7770-1, Clontech Laboratories) was hybridized with

a probe from exons 29 to 47 of MYO15 using the

of 17p11.2 of various sizes, the smallest of which

includes MYO15 and perhaps 20 other genes (6):

K-S Chen, L. Potocki, J. R. Lupski, MRDD Res. Rev.

2 122 (1996)] MYO15 evergesion is easily detected

in the pituitary gland (data not shown). Haploinsuffi-

ciency for MYO15 may explain a portion of the SMS

with Xmn I, and senarated in a 2% agarose gel.

32. A nonsense mutation may affect mRNA stability and

33. Data not shown: a dot blot with poly (A)+ RNA from

same condition as Northern blot analysis (13).

34. Smith-Magenis syndrome (SMS) is due to deletions

Am. J. Hum. Genet. 59, 279 (1996)]

We focus on the narrow domain of RNA secondary structure, which is currently the simplest computationally tractable, yet realistic phenotype (2). This choice enables the definition and exploration of concepts that may prove useful in a wider context. RNA secondary structures represent a coarse level of analysis compared with the three-dimensional structure at atomic resolution. Yet, secondary structures are empir-

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ically well defined and obtain their biophysical and biochemical importance from being a scaffold for the tertiary structure. For the sake of brevity, we shall refer to secondary structures as "shapes." RNA combines in a single molecule both genotype (replicatable sequence) and phenotype (selectable shape), making it ideally suited for in vitro evolution experiments (3, 4).

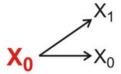
To generate evolutionary histories, we used a stochastic continuous time model of an RNA population replicating and mutating in a capacity-constrained flow reactor under selection (5, 6). In the laboratory, a goal might be to find an RNA aptamer binding specifically to a molecule (4). Although in the experiment the evolutionary end product was unknown, we thought of its shape as being specified implicitly by the imposed selection criterion. Because our intent is to study evolutionary histories rather than end products, we defined a target shape in advance and assumed the replication rate of a sequence to be a function of because, in contrast to sequences, there are

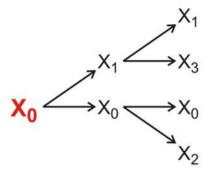
the similarity between its shape and the target. An actual situation may involve more than one best shape, but this does not affect our conclusions.

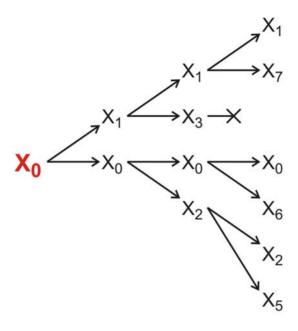
An instance representing in its qualitative features all the simulations we performed is shown in Fig. 1A. Starting with identical sequences folding into a random shape, the simulation was stopped when the population became dominated by the target, here a canonical tRNA shape. The black curve traces the average distance to the target (inversely related to fitness) in the population against time. Aside from a short initial phase, the entire history is dominated by steps, that is, flat periods of no apparent adaptive progress, interrupted by sudden approaches toward the target structure (7). However, the dominant shapes in the population not only change at these marked events but undergo several fitness-neutral transformations during the periods of no apparent progress. Although discontinuities in the fitness trace are evident, it is entirely unclear when and on the basis of what the series of successive phenotypes itself can be called continuous or discontinuous.

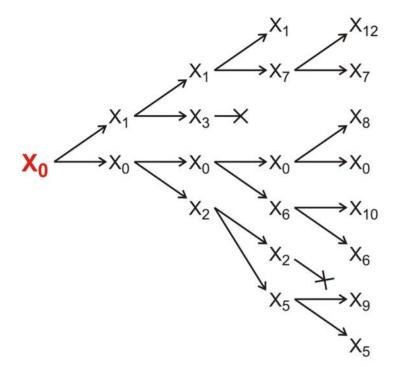
A set of entities is organized into a (topological) space by assigning to each entity a system of neighborhoods. In the present case, there are two kinds of entities: sequences and shapes, which are related by a thermodynamic folding procedure. The set of possible sequences (of fixed length) is naturally organized into a space because point mutations induce a canonical neighborhood. The neighborhood of a sequence consists of all its one-error mutants. The problem is how to organize the set of possible shapes into a space. The issue arises

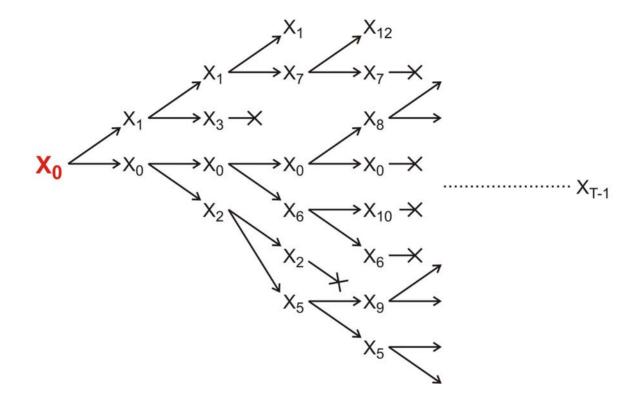


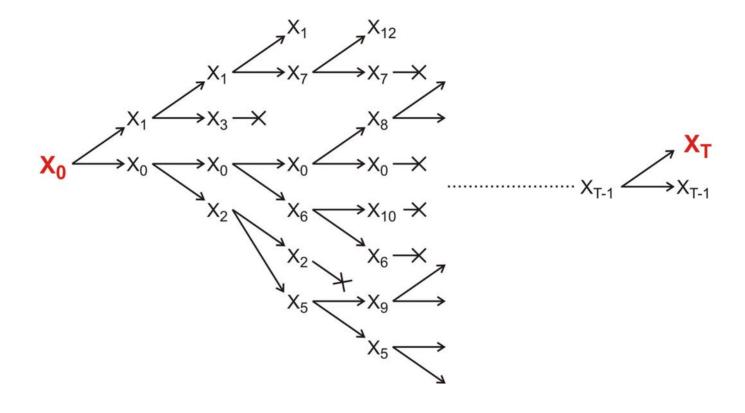


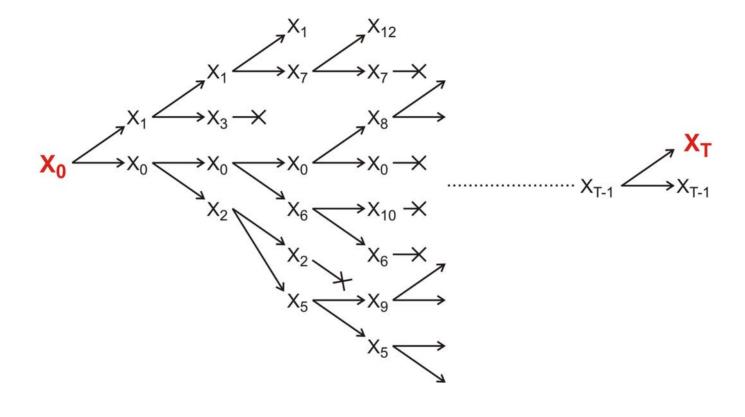




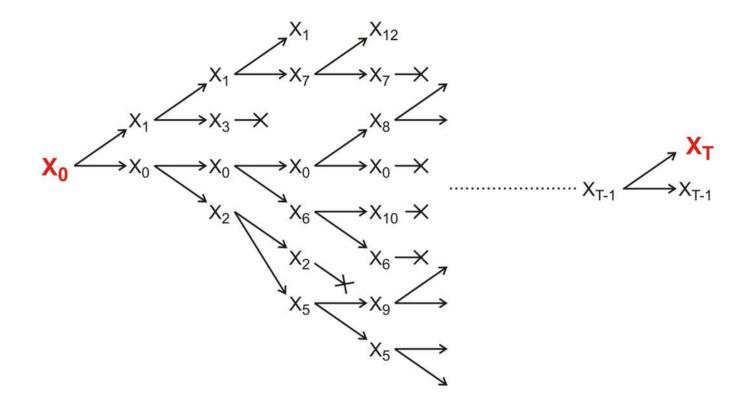




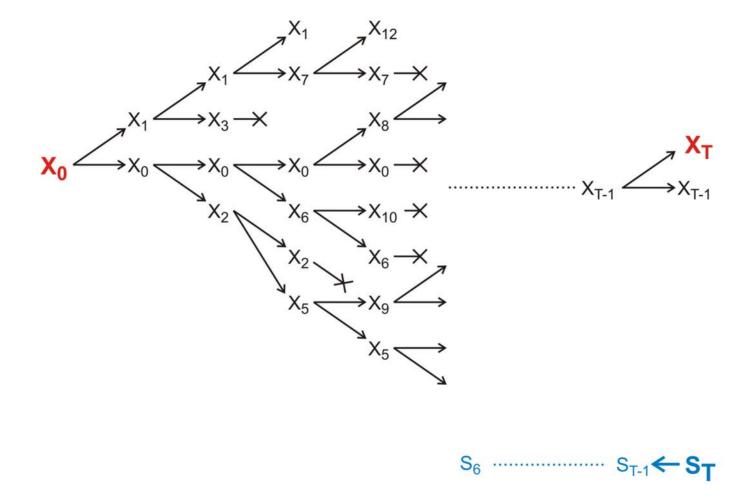


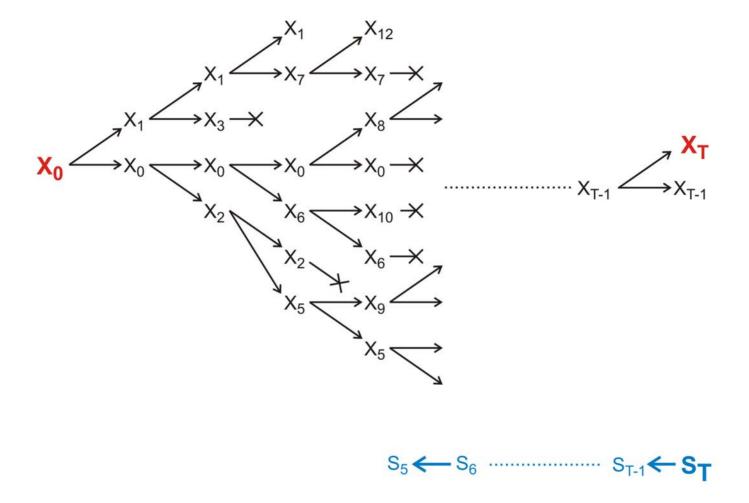


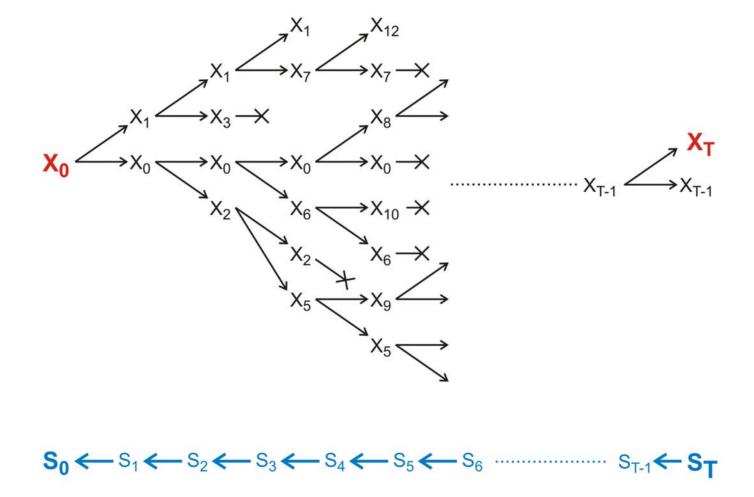
ST

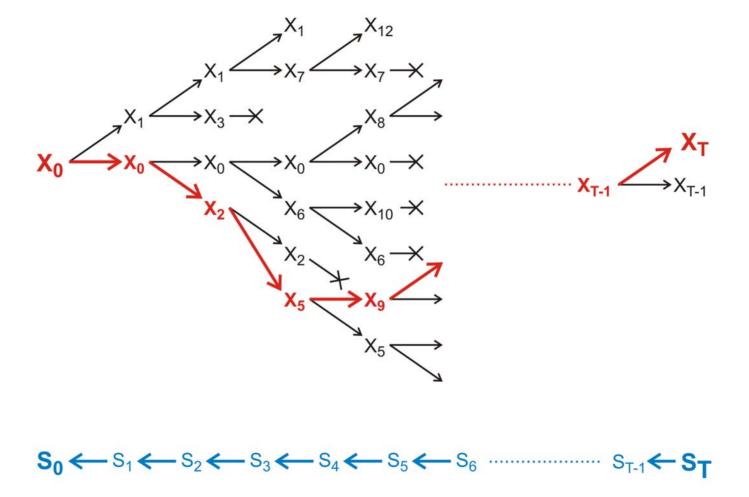


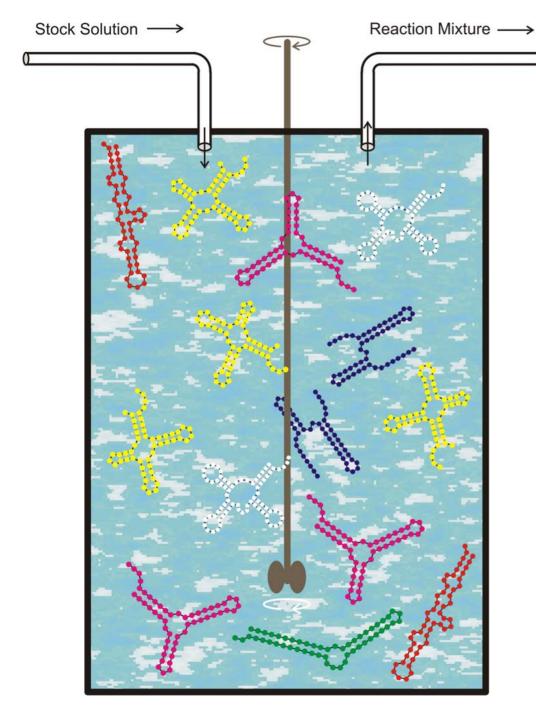
S_{T-1}← **S**_T











Replication rate constant

(Fitness):

$$f_k = \gamma / [\alpha + \Delta d_S^{(k)}]$$

$$\Delta d_S^{(k)} = d_H(S_k, S_{\tau})$$

Selection pressure:

The population size,

N = # RNA moleucles,

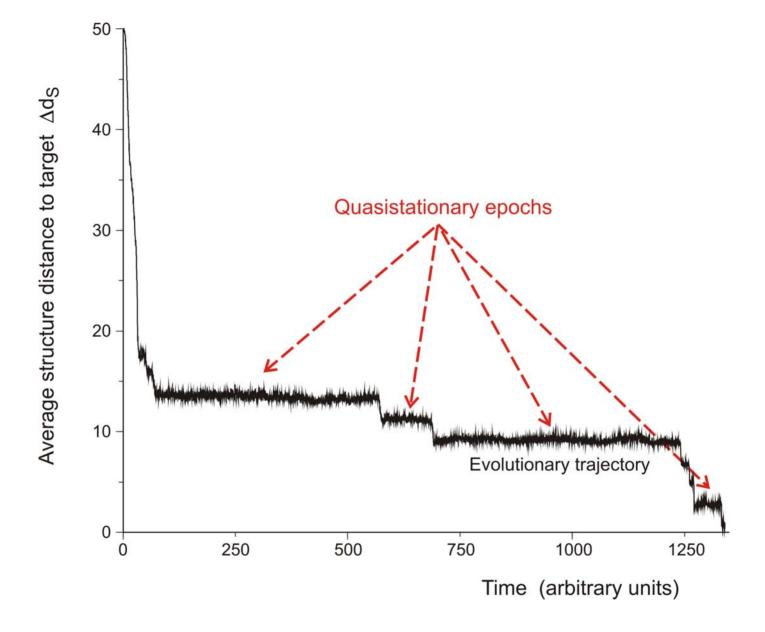
is determined by the flux:

$$N(t) \approx \overline{N} \pm \sqrt{\overline{N}}$$

Mutation rate:

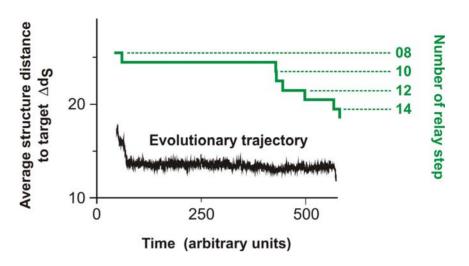
p = 0.001 / Nucleotide × Replication

The flow reactor as a device for studying the evolution of molecules *in vitro* and *in silico*.



In silico optimization in the flow reactor: Evolutionary Trajectory

28 neutral point mutations during a long quasi-stationary epoch

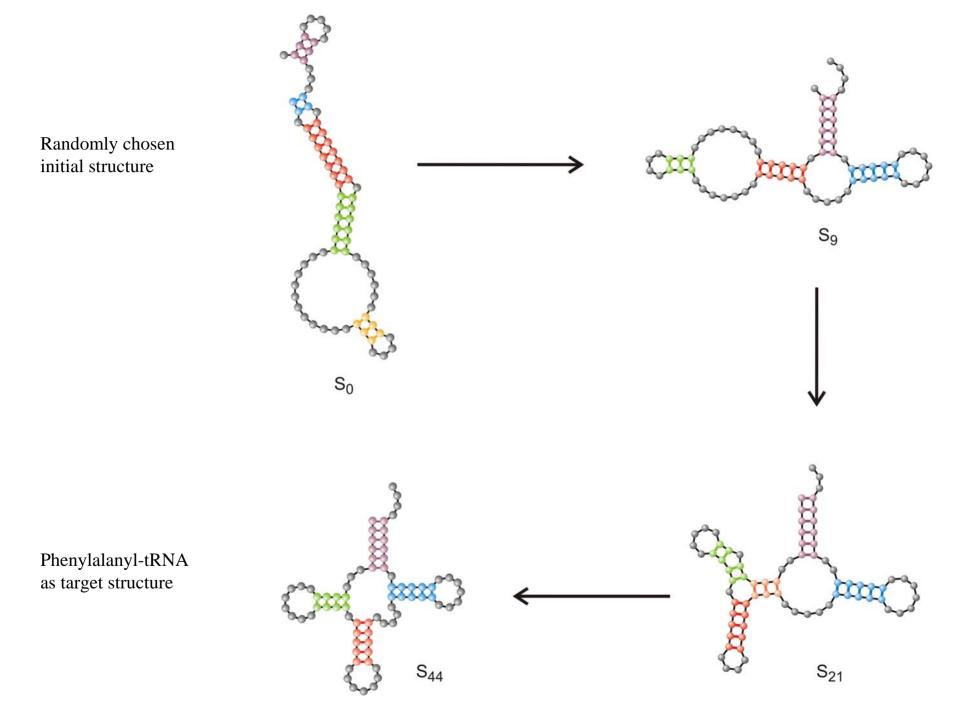


```
GGUAUGGGCGUUGA AUAGUAGGGUUUA A A CCA AUCGGCCA ACGAUCUCGUGUGCGCAUUUCAUAUCCCGUACA GA A
entry
   8
   GGUAUGGGCGUUGAAUAAUAGGGUUUAAACCAAUCGGCCAACGAUCUCGUGUGCGCAUUUCAUAUCCCAUACAGAA
exit
   GGUAUGGGCGUUGA AUA AUA GGGUUUA A A CCA AUCGGCCA A CGAUCUCGUGUGCGCAUUUCAUAUACCAUA CAGA A
entry
   9
   exit
   entry
   10
   UGGAUGGA CGUUGA AUA ACA AGGUAUCG<mark>A</mark>CCA A ACA ACCA ACGA GUA AGUGUGUA CGCCCCA CA CA GCGUCCCA A G
exit
```

Transition inducing point mutations change the molecular structure

Neutral point mutations leave the molecular structure unchanged

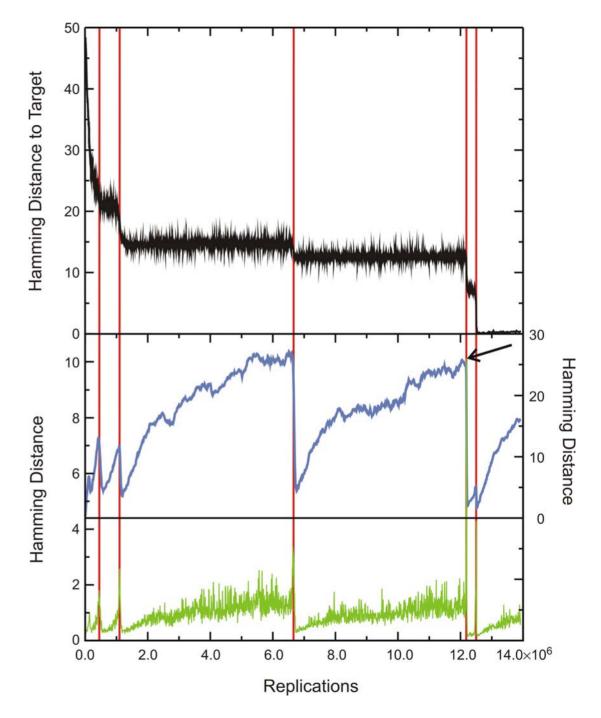
Neutral genotype evolution during phenotypic stasis

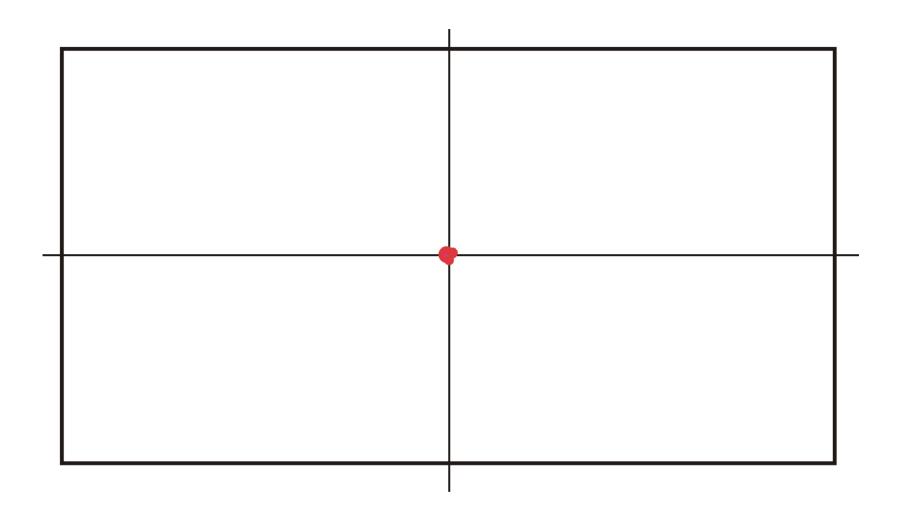


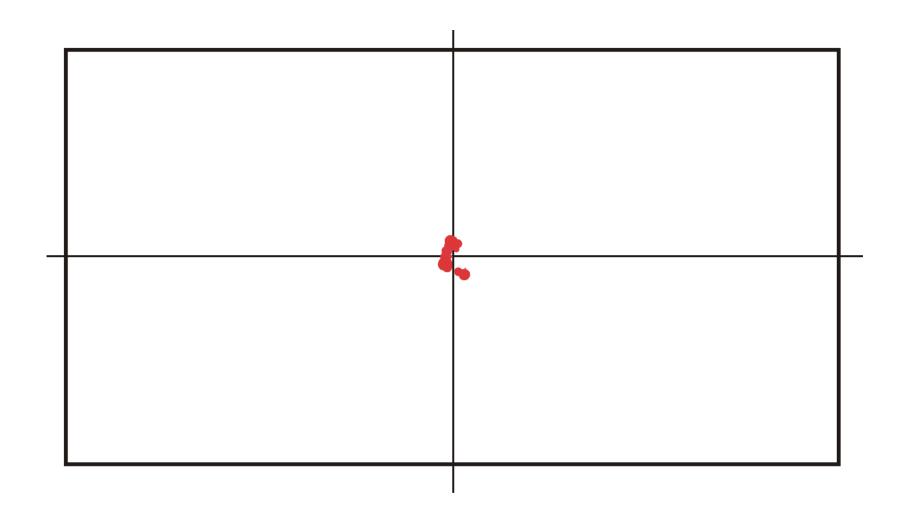
Evolutionary trajectory

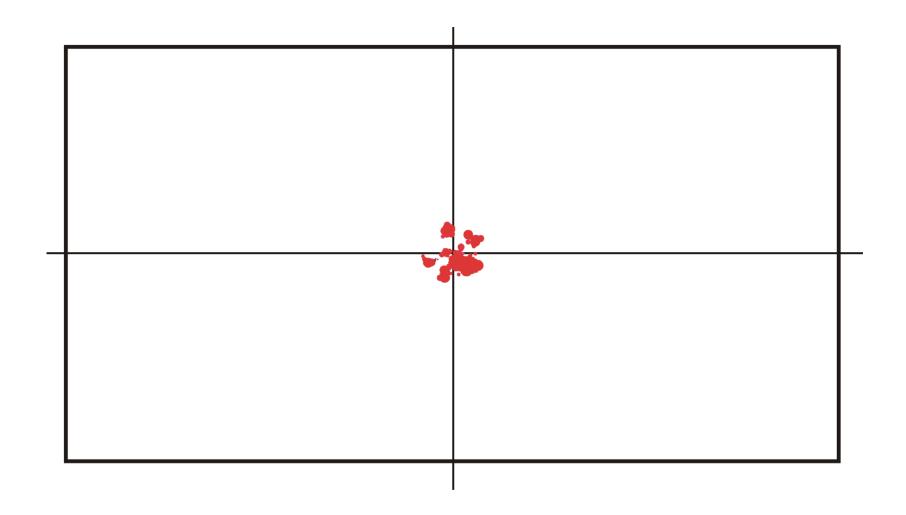
Spreading of the population on neutral networks

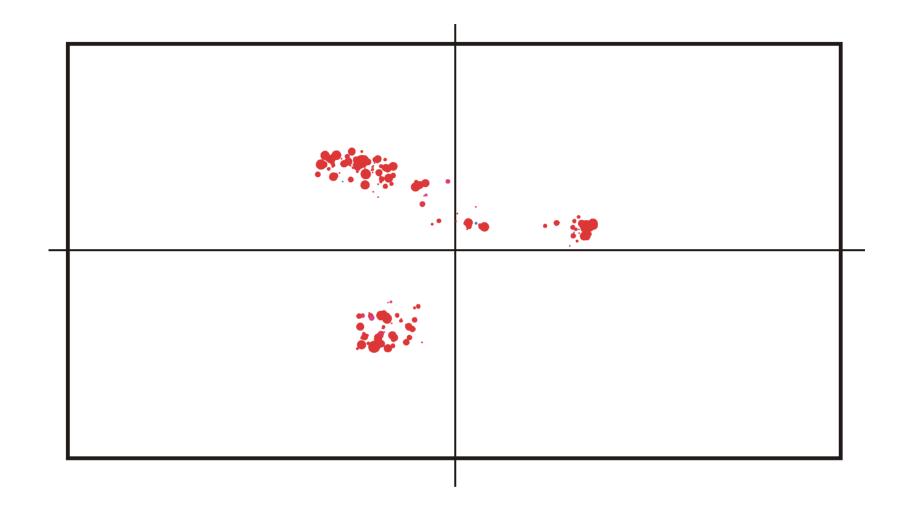
Drift of the population center in sequence space

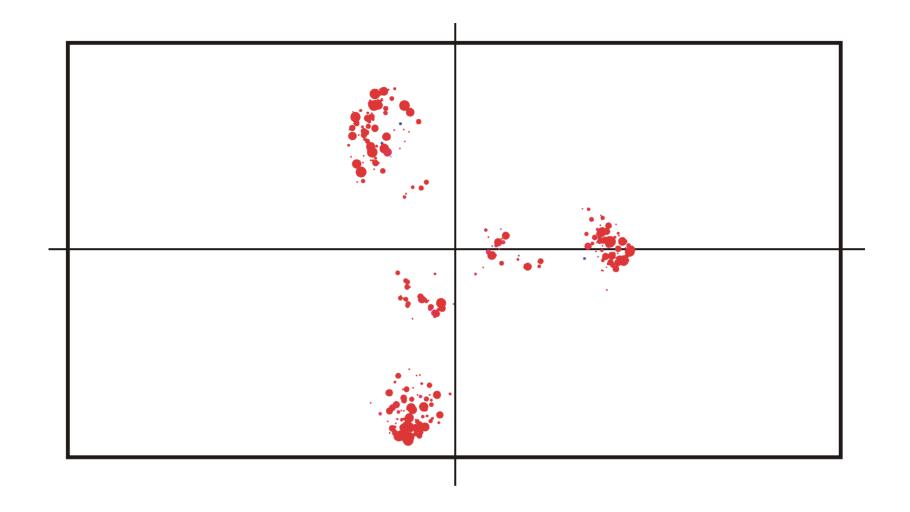


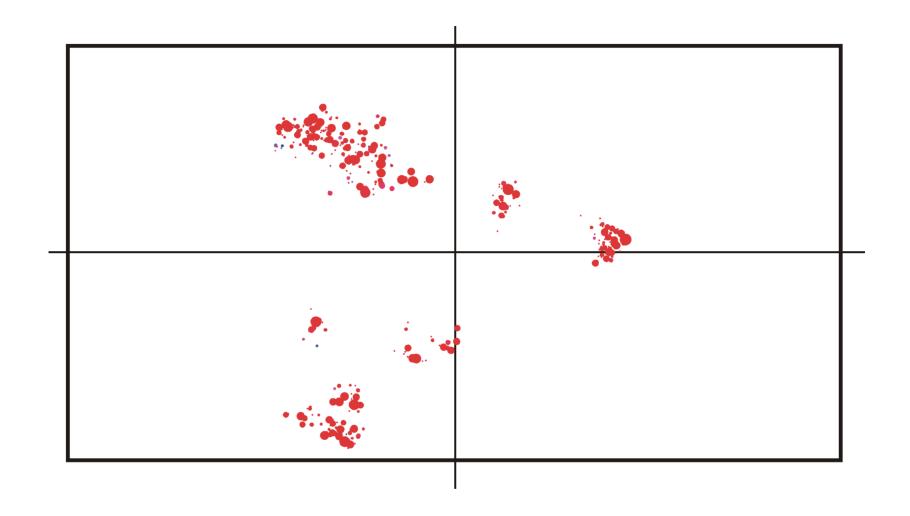


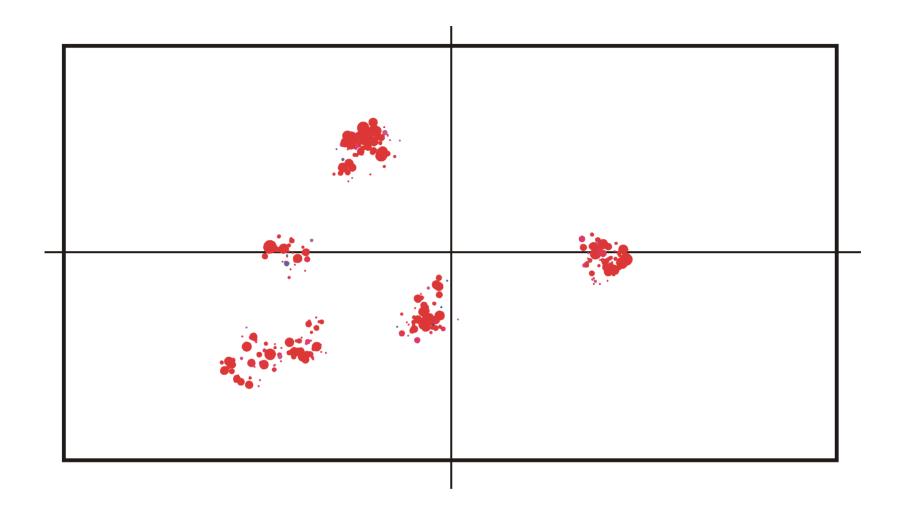


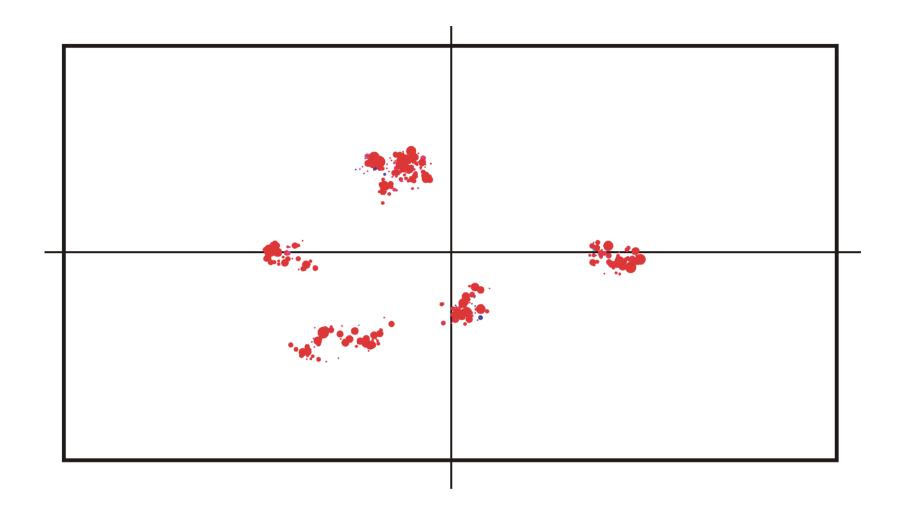


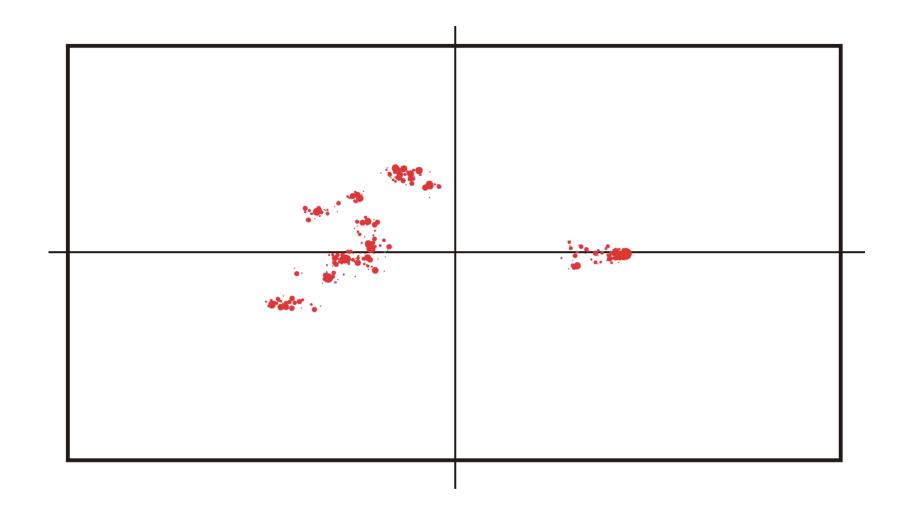


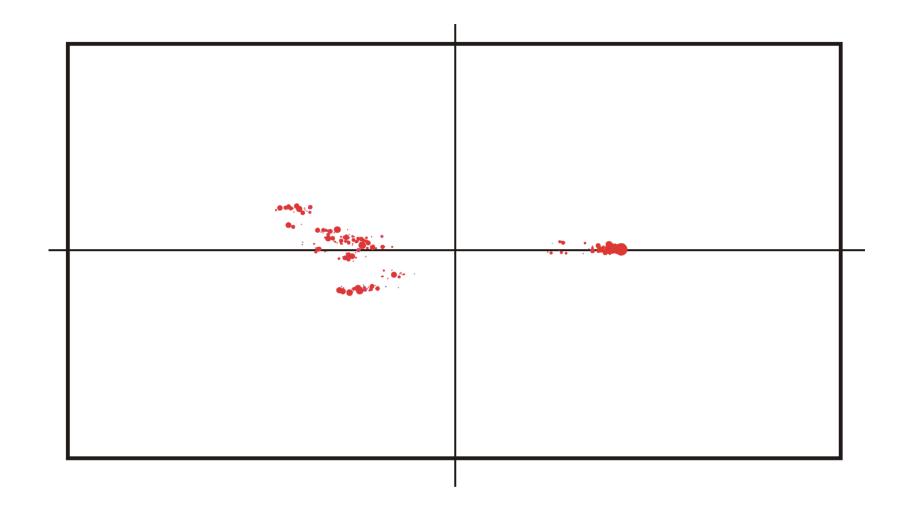


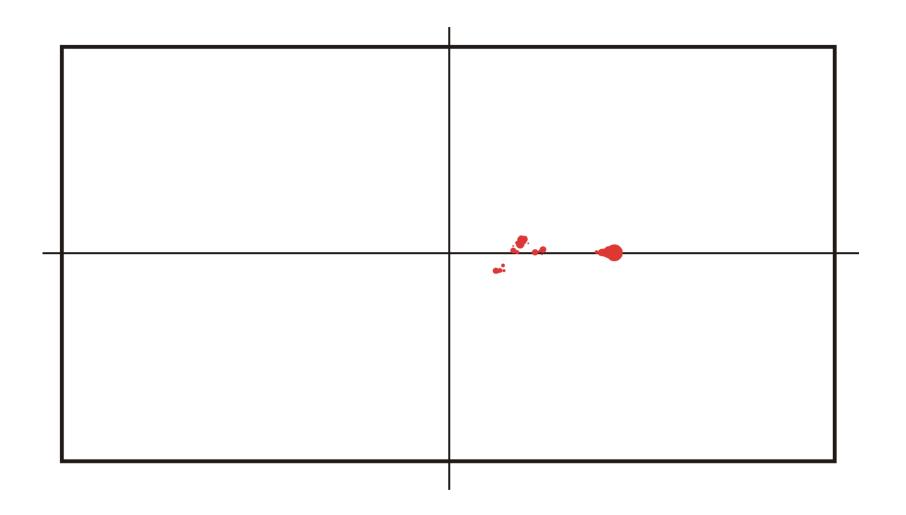


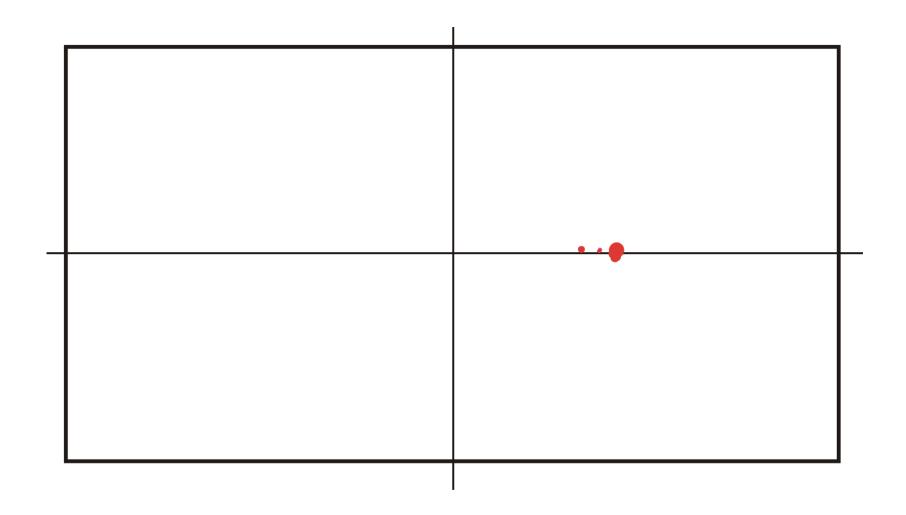


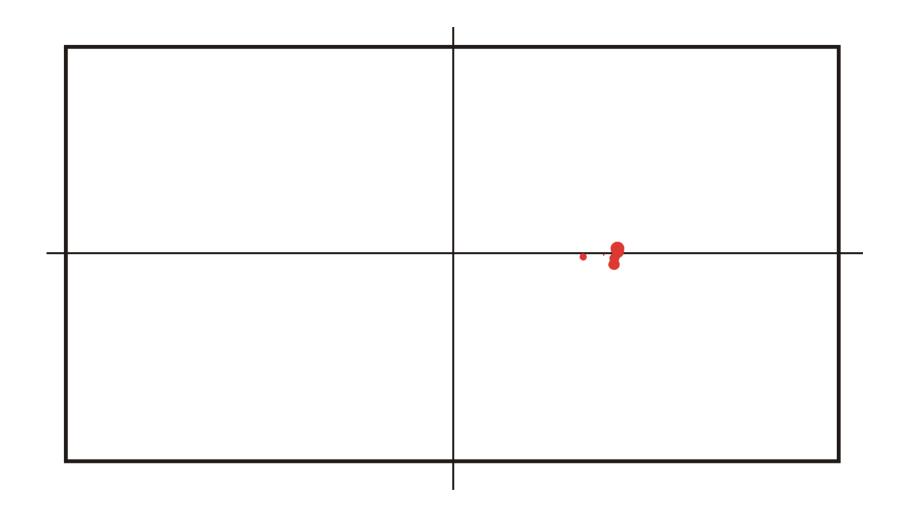


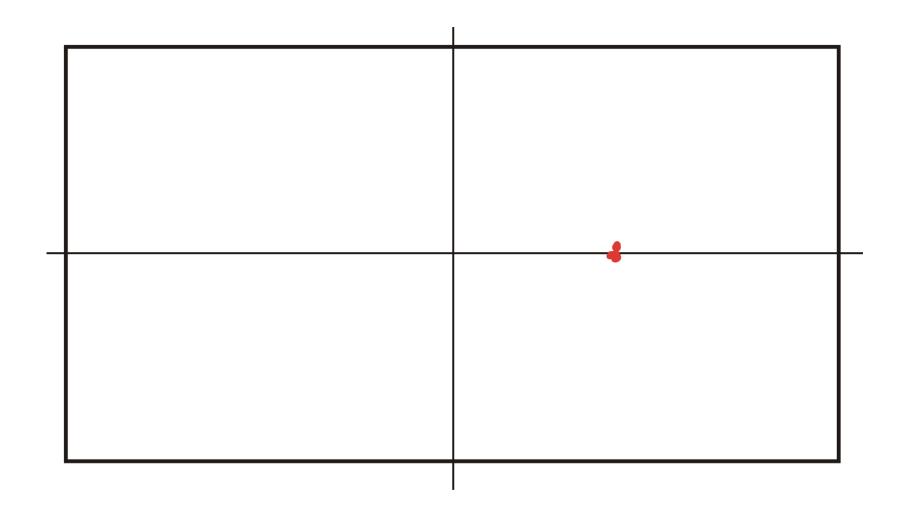


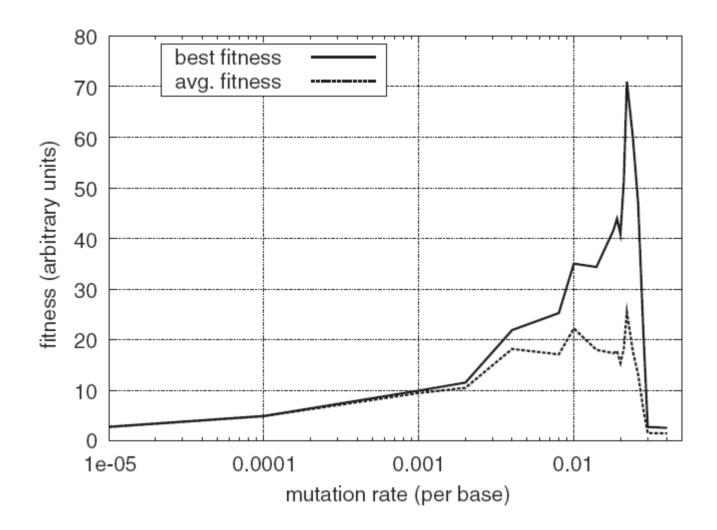




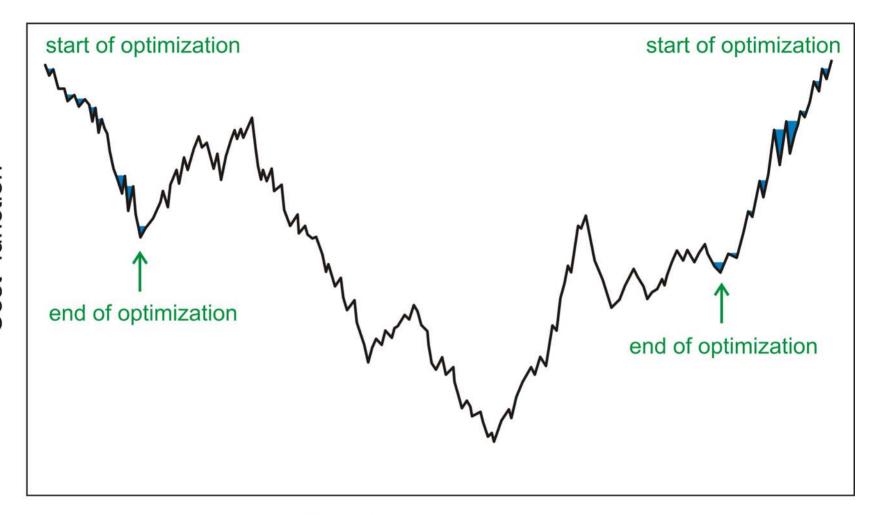






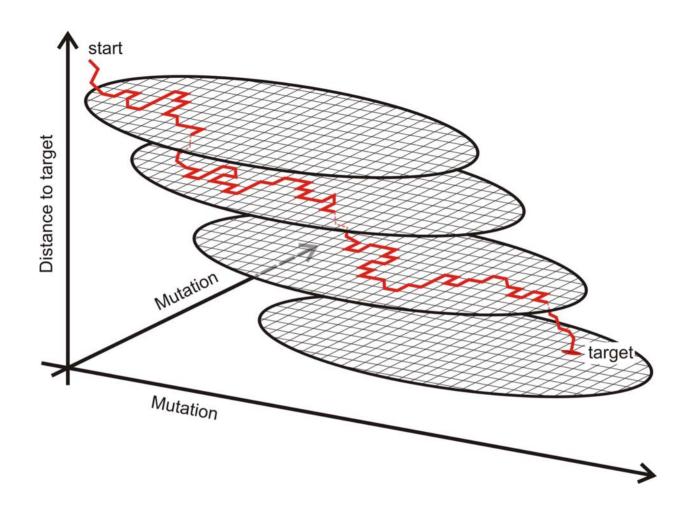


Anne Kupczok, Peter Dittrich, Determinats of simulated RNA evolution. J.Theor.Biol. **238**:726-735, 2006

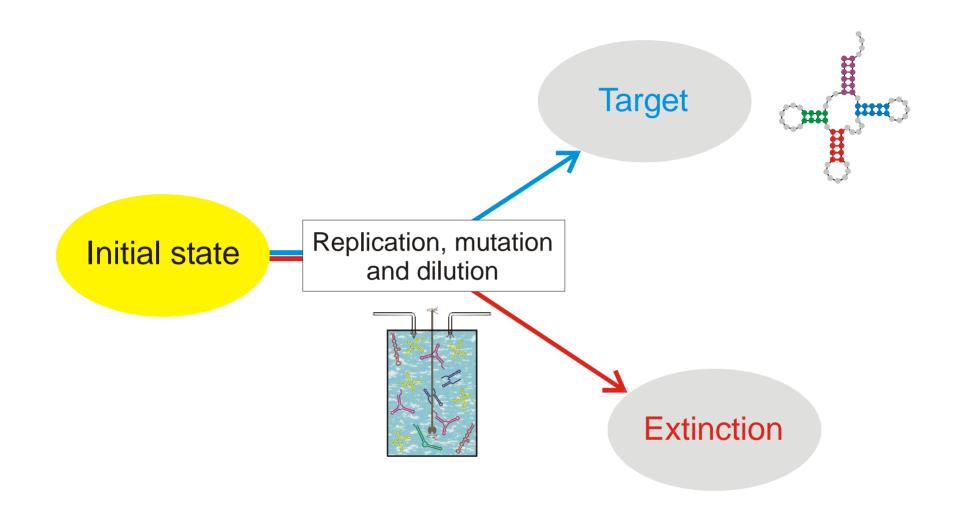


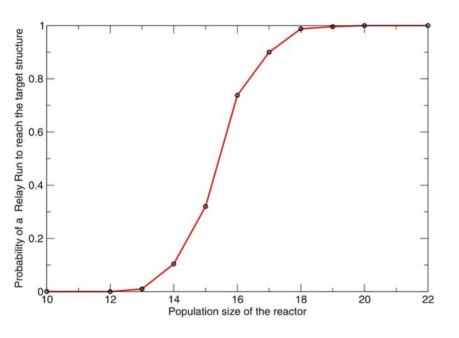
Genotype space

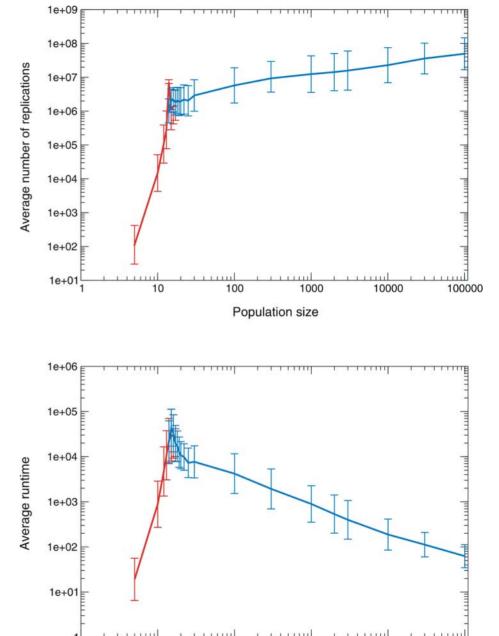
Genotype space



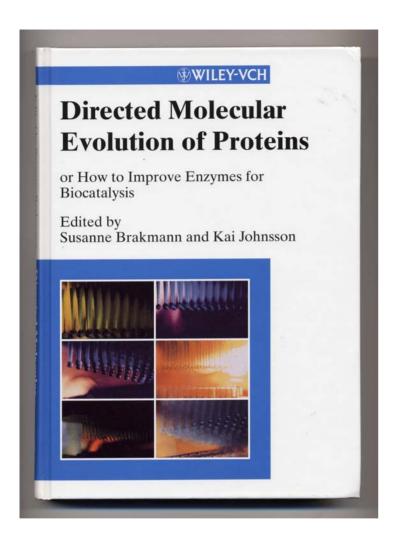
A sketch of optimization on neutral networks

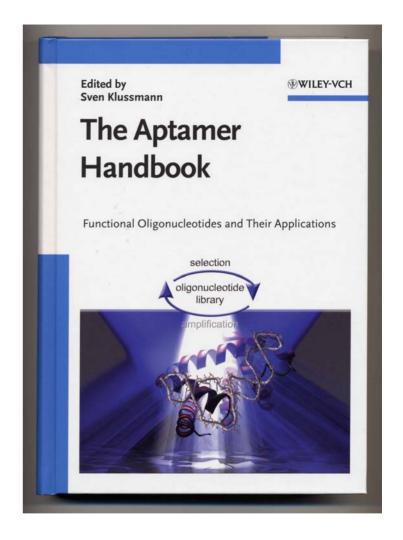






Population size





Application of molecular evolution to problems in biotechnology

Acknowledgement of support

Fonds zur Förderung der wissenschaftlichen Forschung (FWF) Projects No. 09942, 10578, 11065, 13093 13887, and 14898



Universität Wien

Wiener Wissenschafts-, Forschungs- und Technologiefonds (WWTF)
Project No. Mat05

Jubiläumsfonds der Österreichischen Nationalbank Project No. Nat-7813

European Commission: Contracts No. 98-0189, 12835 (NEST)

Austrian Genome Research Program – GEN-AU

Siemens AG, Austria

Universität Wien and the Santa Fe Institute

Coworkers

Walter Fontana, Harvard Medical School, MA

Christian Forst, Christian Reidys, Los Alamos National Laboratory, NM



Universität Wien

Peter Stadler, Bärbel Stadler, Universität Leipzig, GE

Jord Nagel, Kees Pleij, Universiteit Leiden, NL

Christoph Flamm, Ivo L.Hofacker, Andreas Svrček-Seiler, Universität Wien, AT

Kurt Grünberger, Michael Kospach, Andreas Wernitznig, Stefanie Widder, Michael Wolfinger, Stefan Wuchty, Universität Wien, AT

Stefan Bernhart, Jan Cupal, Lukas Endler, Ulrike Langhammer, Rainer Machne, Ulrike Mückstein, Hakim Tafer, Universität Wien, AT

Ulrike Göbel, Walter Grüner, Stefan Kopp, Jaqueline Weber, Institut für Molekulare Biotechnologie, Jena, GE Web-Page for further information:

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